

Enhancing atomic ordering, magnetic and transport properties of Mn_2VGa Heusler alloy thin films toward negatively spin-polarized charge injection

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Abstract

Magnetic materials with negative spin polarization have attracted attention for their potential to increase the design freedom of spintronic devices. This study investigated the effects of off-stoichiometry on the atomic ordering, microstructure, and magneto-transport properties in $Mn_{2+x}V_{1-x}Ga$ ($x = -0.2, 0, +0.2, +0.4$) Heusler alloy films, which are predicted to have large negative spin polarization derived from a pseudo band gap in the majority spin channel. The $Mn_{2+x}V_{1-x}Ga$ films epitaxially grown on $MgO(001)$ substrates exhibits variations of $B2$ and $L2_1$ order with the Mn concentration. A high-quality $L2_1$ ordered film was achieved in the Mn-rich composition ($x = +0.2$) with $B2$ and $L2_1$ order parameters of 0.97 and 0.86, respectively, and a saturation magnetization of $1.4 \mu_B/f.u.$, which agrees the Slater-Pauling rule. Scanning transmission electron microscopy observations showed that $B2$ and $L2_1$ phases coexist in Mn-poor and stoichiometric films, while the $L2_1$ phase is dominant in the Mn-rich film with small amounts of Mn–V and Mn–Ga disorders, as revealed by laboratory and anomalous X-ray diffraction. Combined first-principles calculations and anisotropic magnetoresistance analysis confirm that the addition of excess Mn preserves the high spin polarization by suppressing the formation of detrimental antisites of V atoms occupying Mn sites. Therefore, the Mn-rich composition is promising for negatively spin-polarized charge injection in Mn_2VGa -based spintronic applications.

Keywords: Heusler alloy; Thin film; Atomic ordering; Magnetic properties; First-principles calculations.

1. Introduction

Owing to the unique energy band structure with a bandgap at the Fermi level (E_F) of one spin-channel, half-metallic Heusler alloys have attracted considerable attention for potential applications in spintronic devices such as magnetic random-access memories, read sensors and spin-torque oscillators for next-generation ultra-high density hard disk drives [1,2]. Among the Heusler alloy family, numerous studies have been conducted on Co-based Co_2YZ alloys ($Y = \text{Mn, Fe, Cr}$, and $Z = \text{Al, Si, Ga, Ge}$ etc.) to enhance their spin-dependent properties at room temperature (RT) because of the theoretically predicted 100% spin polarization and high Curie temperature (T_C) [3-9]. On the other hand, Mn-based Heusler alloys (Mn_2YZ), which are also expected to exhibit half-metallicity, have not been fully explored as alternative candidates [10-12]. The intrinsically low saturation magnetization of Mn-based alloys can reduce the critical current density for magnetization switching by spin-transfer torque, which may lead to low-energy operation in spintronic devices [13,14].

Mn_2VGa ferrimagnetic Heusler alloy has great potential as a spintronic material due to its sufficiently high T_C of ~ 784 K [10,12,15-19]. Mn and V atoms in the $L2_1$ ordered Mn_2VGa are antiferromagnetically coupled (Mn: $1.64 \mu_B/\text{f.u.}$, V: $-1.2 \mu_B/\text{f.u.}$), resulting in a smaller magnetic moment of $\sim 2 \mu_B/\text{f.u.}$ than those of Co-based alloys; $\sim 4-6 \mu_B/\text{f.u.}$ More interestingly, Mn_2VGa was predicted to have negative spin polarization ($P < 0$) [20], *i.e.*, the energy band structure has a gap in the majority-spin band at the E_F , and the spin direction of the spin-polarized current is opposite to the magnetization direction [21]. Magnetic materials with negative P have been demonstrated to significantly improve the design freedom of spintronic devices [22-24]. For example, giant magnetoresistance devices using FeCr magnetic layer showed inverse magnetoresistance, providing evidence of negative P [25-28]. Inverse magnetoresistance has also been measured in tunneling magnetoresistance devices [29-31]; Klewe *et al.* reported the inverse magnetoresistance for an epitaxial $\text{Mn}_2\text{VGa}/\text{MgO}/\text{Co}_{70}\text{Fe}_{30}$

magnetic tunnel junction, confirming the negative P in the Mn_2VGa alloy [31]. However, the magnitude of the observed magnetoresistance ratio (-2%) was much smaller than the theoretical value (-43%). Since the spin polarization of Heusler alloys is closely associated with atomic ordering [32,33], it is important to understand the relationship between negative P and atomic disorder in Mn_2VGa in order to improve spin-dependent properties.

The atomic disorder has been reported to impair the spin polarization of the Mn_2VGa alloy [20,31]. Theoretical calculations predict that the negative P of Mn_2VGa with $B2$ ordered structure (-69%) is lower than that of Mn_2VGa with $L2_1$ ordered structure (-84%) [31]. The Mn–V disorder can deteriorate the pseudo-gap in the majority spin band of $L2_1$ ordered Mn_2VGa alloy, leading to the degradation of negative P [31]. Compositional optimization is an efficient way to improve the atomic ordering in Heusler alloys [34–38]. For example, a stoichiometric $\text{Co}_2\text{Fe}(\text{Ga}_{0.5}\text{Ge}_{0.5})$ Heusler alloy film showed a low degree of $L2_1$ order; ~ 0.13 , which was significantly improved to ~ 0.86 by adding excess Ge to suppress deleterious Co_{Fe} antisite [38], where X_Y denotes that the atomic sites for element Y are replaced with X . The calculated band structure of the Ge-rich composition predicts the higher spin polarization than the stoichiometric composition, which is indicated by anisotropic magnetoresistance (AMR) analysis. Based on an extended two-current model developed by Kokado *et al.* [39], the AMR effect has been experimentally demonstrated to be closely related to the spin polarization of various Co-based Heusler alloy films [40–42]. Therefore, an in-depth investigation of the effects of composition tuning along with optimized thermal processing on the atomic ordering, microstructure, and magneto-transport properties of Mn_2VGa alloys is required to gain insights into the formation of antisite defects and their relationship with electronic structures.

In this study, we fabricated stoichiometric and off-stoichiometric $\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ (MVG) alloy thin films with nominal compositions of $x = -0.2, 0, +0.2, \text{ and } +0.4$ by the magnetron sputtering. The concentrations of Mn and V were tailored because these two elements mainly

determine the ferrimagnetic and spintronic properties of Mn_2VGa . Two heat treatments; elevated-temperature deposition and post-deposition annealing were carried out to obtain the optimum thermal processing parameters. The atomic ordering and antisite defects of the prepared MVG films were quantitatively evaluated using a combination of laboratory/synchrotron X-ray diffraction (XRD) analyses. Laboratory XRD (lab-XRD) cannot differentiate the site occupancies of Mn and V due to their close atomic numbers, whereas it can be distinguished by synchrotron XRD. Aberration-corrected scanning transmission electron microscopy (STEM) was performed to examine the uniformity of the films with Mn and V atoms being identified in real space. The revealed ordering and defects were then correlated with the magnetic and transport properties. Based on experimental results and first-principles calculations of electronic structure, the relationship between atomic ordering and spin polarization in MVG films is discussed.

2. Experimental and computational methods

$\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ ($x = -0.2, 0, +0.2, +0.4$) thin films were grown on (001)-oriented MgO single crystalline substrates using an automatic co-sputtering system with $\text{Mn}_{55}\text{Ga}_{45}$ and V targets. The Mn/Ga ratio was controlled by the Ar pressure, and the V content was controlled by the sputtering power. Elevated-temperature deposition and post-deposition annealing were performed on the stoichiometric samples ($x = 0$) at substrate temperatures (T_{sub}) of 300–600°C and $T_{\text{ann}} = 300$ –600°C for 30 min, respectively. The off-stoichiometric samples ($x = -0.2, +0.2,$ and $+0.4$) were prepared by post annealing at $T_{\text{ann}} = 500$ °C and 600°C. All films were capped by 2 nm-thick Al layers after cooling down to RT. **Table 1** summarizes the chemical compositions of $\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ films in at.% measured using X-ray fluorescence (XRF) analysis calibrated by the standard sample whose composition was analyzed by inductively coupled plasma mass spectrometry. The XRF measurements were repeated five times for each film, and

the standard deviations are listed as errors in Table 1. The errors are significantly smaller than the compositional variations between the films, indicating the reliability of the measured compositions. Note that the actual Mn concentration of the Mn-rich films ($x = +0.2$ and $+0.4$) are slightly lower than the nominal concentrations. The deviation may occur because the composition was adjusted by depositing the samples at RT, and the heat treatments caused slight evaporation of Mn atoms.

The crystal structure and atomic ordering of the prepared films were investigated using lab-XRD with a Cu- $K\alpha$ radiation source. The degree of $B2$ and $L2_1$ ordering, S_{B2} and S_{L2_1} were calculated based on $S_{B2} = \sqrt{\frac{I_{002}^{obs}/I_{004}^{obs}}{I_{002}^{sim}/I_{004}^{sim}}}$ and $S_{L2_1} = \sqrt{\frac{I_{111}^{obs}/I_{444}^{obs}}{I_{111}^{sim}/I_{444}^{sim}}}$, where I_{hkl}^{obs} and I_{hkl}^{sim} represent the observed and simulated hkl peak intensities, respectively [43-45]. The observed peak intensity was analyzed by fitting with split pseudo-Voigt function. The XRD pattern simulation was performed using the Visualization for Electronic and Structural Analysis (VESTA) software based on the XRF compositions. Given the close atomic scattering factors of Mn (f_{Mn}) and V (f_V) in the Cu- $K\alpha$ source, anomalous XRD (AXRD) measurements were performed using synchrotron-radiated X-rays (BL13XU, SPring-8) to evaluate the degree of Mn-V order as the anomalous dispersion term of f_{Mn} significantly changes around the Mn K -absorption edge (6.539 keV) [46,47]. X-ray magnetic circular dichroism (XMCD) measurements were performed at the Photon Factory of the High Energy Accelerator Research Organization (BL-7A, KEK) using the total electron yield (TEY) method with a magnetic field of ± 1 T applied along the incident X-ray beam. The magnetic properties were measured using vibrating sample magnetometer at RT. High-angle annular dark-field scanning transmission electron microscopy (HAADF-STEM) observations, nano-beam electron diffraction (NBED) and energy-dispersive X-ray spectroscopy (EDS) were performed using an FEI Titan G² 80-200 TEM with a probe aberration corrector operating at 200 kV. Thin foil specimens for STEM observations were prepared by the focused ion beam lift-out technique using an FEI Helios G4 UX.

Table 1 Chemical compositions of the $\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ films measured by XRF analysis.

Sample	Thermal treatment	Mn (at.%)	V (at.%)	Ga (at.%)	Composition ratio
$x = 0$	$T_{\text{sub}} = 600^\circ\text{C}$	48.62 ± 0.07	26.1 ± 0.05	25.28 ± 0.09	$\text{Mn}_{1.94}\text{V}_{1.04}\text{Ga}_{1.01}$
$x = -0.2$	$T_{\text{ann}} = 600^\circ\text{C}$	44.27 ± 0.09	29.61 ± 0.14	26.12 ± 0.12	$\text{Mn}_{1.77}\text{V}_{1.19}\text{Ga}_{1.04}$
$x = 0$	$T_{\text{ann}} = 600^\circ\text{C}$	48.95 ± 0.14	25.78 ± 0.08	25.27 ± 0.07	$\text{Mn}_{1.96}\text{V}_{1.03}\text{Ga}_{1.01}$
$x = +0.2$	$T_{\text{ann}} = 600^\circ\text{C}$	52.33 ± 0.07	20.56 ± 0.07	27.11 ± 0.03	$\text{Mn}_{2.09}\text{V}_{0.83}\text{Ga}_{1.08}$
$x = +0.4$	$T_{\text{ann}} = 600^\circ\text{C}$	58.25 ± 0.06	14.92 ± 0.02	26.82 ± 0.05	$\text{Mn}_{2.33}\text{V}_{0.6}\text{Ga}_{1.07}$

The density of states (DOS) of $B2$ and $L2_1$ ordered $\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ were calculated based on the density functional theory and the Korringa-Kohn-Rostoker method implemented in the Akai-KKR software package [48-50]. The generalized gradient approximation was used for the exchange correlation energy [51], and the disordered states were treated within the coherent potential approximation. For all these calculations, we used a lattice constant of $a = 5.905 \text{ \AA}$, which was reported in a previous bulk study [15]. The lattice constant of the films prepared in this study is close to the bulk value as measured by XRD. The Brillouin-zone integration was performed using $16 \times 16 \times 16$ k points, and the imaginary part of the energy was set to 0.001 Ry for the DOS calculations. The spin-orbit interaction was considered in the DOS calculations for analyzing the AMR effect.

For the AMR measurements, MVG films were patterned into strips with dimensions of $2.8 \text{ mm} \times 0.6 \text{ mm}$ using photolithography and Ar ion-milling. The electric resistivities, ρ , of stripes were measured by a four-terminal method using a physical property measurement system (PPMS DynaCool, Quantum Design) over a temperature range of $10\text{--}300 \text{ K}$. A current, I , of $500 \text{ }\mu\text{A}$ along the longitudinal direction of stripes ($[110]_{\text{MVG}}$ or $[100]_{\text{MVG}}$), and a magnetic field of 1 T , which is sufficient to saturate the magnetization, rotating within the film plane were applied during the measurements. The angle, ϕ , dependence of the AMR ratio was defined as $(\rho(\phi) - \rho_{\perp})/\rho_{\perp} \times 100 \%$, where ϕ represent the relative angle between the current and magnetic field directions, and $\rho(\phi)$ (ρ_{\perp}) is the resistivity of films at ϕ ($\phi = 90^\circ$).

3. Results

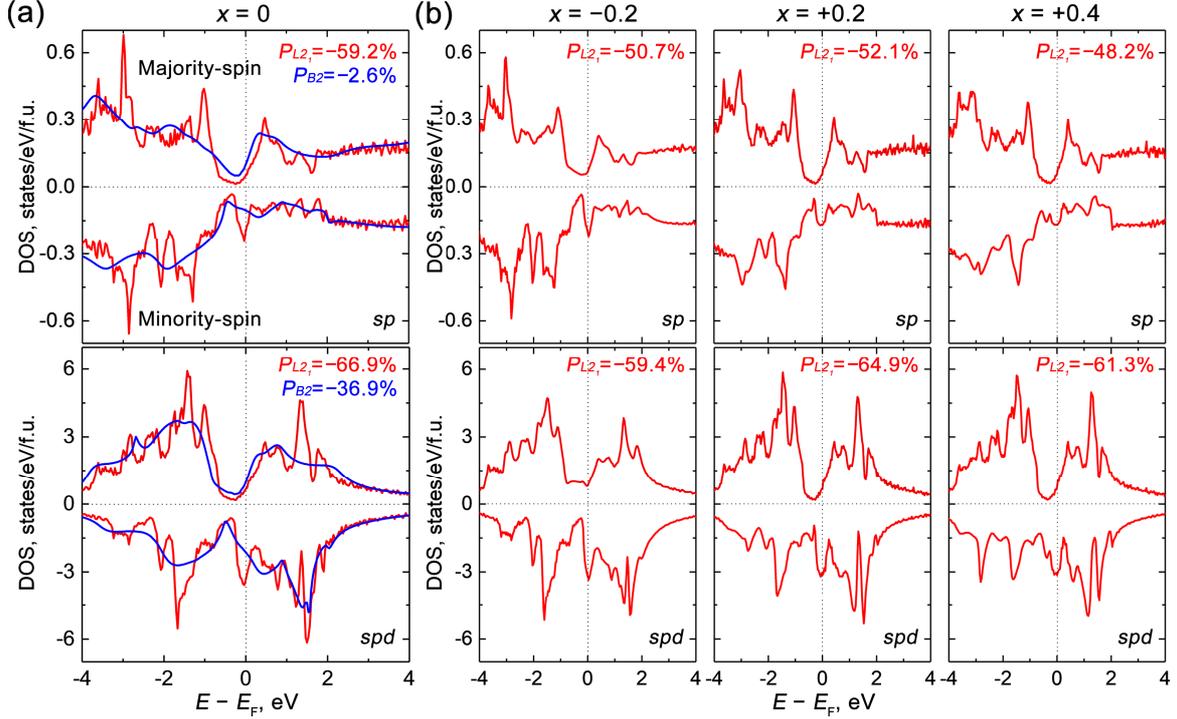


Fig. 1. First-principles calculations of the spd -total and sp -orbital DOSs for $L2_1$ and $B2$ ordered $Mn_{2+x}V_{1-x}Ga$ with (a) $x = 0$ (stoichiometric), and (b) $x = -0.2, +0.2, +0.4$ (off-stoichiometric), respectively.

Figures 1a and b show the calculated energy dependence of the sp -orbital and spd -total DOSs for perfect $L2_1$ and $B2$ ordered $Mn_{2+x}V_{1-x}Ga$ ($x = 0, -0.2, +0.2, +0.4$) alloys with nominal compositions. Note that in the calculation model for Mn-poor (Mn-rich) composition, excess V (Mn) atoms occupy the sites of deficient Mn (V) atoms. The DOS of the stoichiometric Mn_2VGa ($x = 0$) exhibits a pseudo-gap around the E_F in the majority-spin band, resulting in negative P , **Fig. 1a**. The values of P at the E_F of $L2_1$ ordered state are calculated to be -59.2% and -66.9% for the sp -orbital and spd -total DOSs, respectively. The sp -orbital DOS is a representative parameter for the spin polarization of conduction electrons due to the small effective mass of sp -electrons. The $B2$ ordered state significantly deteriorates the P value to -2.6% (sp -orbital) and -36.9% (spd -total), indicating that a structure with high $L2_1$ ordering is desirable for achieving high negative spin polarization. In the Mn-poor composition ($x = -0.2$), the gap structure was disturbed by the increased DOS in the majority-spin pseudo-gap, leading

to a decrease in P value to -50.7% (sp -orbital). On the other hand, the gap structure is maintained in the Mn-rich compositions, $x = +0.2$ and $+0.4$. Despite the maintained pseudo-gap, P becomes smaller than that of the stoichiometric composition, because the E_F exists at the edge of the pseudo-gap and is sensitive to the small change in the DOS. These calculations indicate that excess V atoms in the Mn-site, *i.e.*, V_{Mn} antisites are detrimental to P by inducing the fundamental change in DOS, **Fig. 1b**.

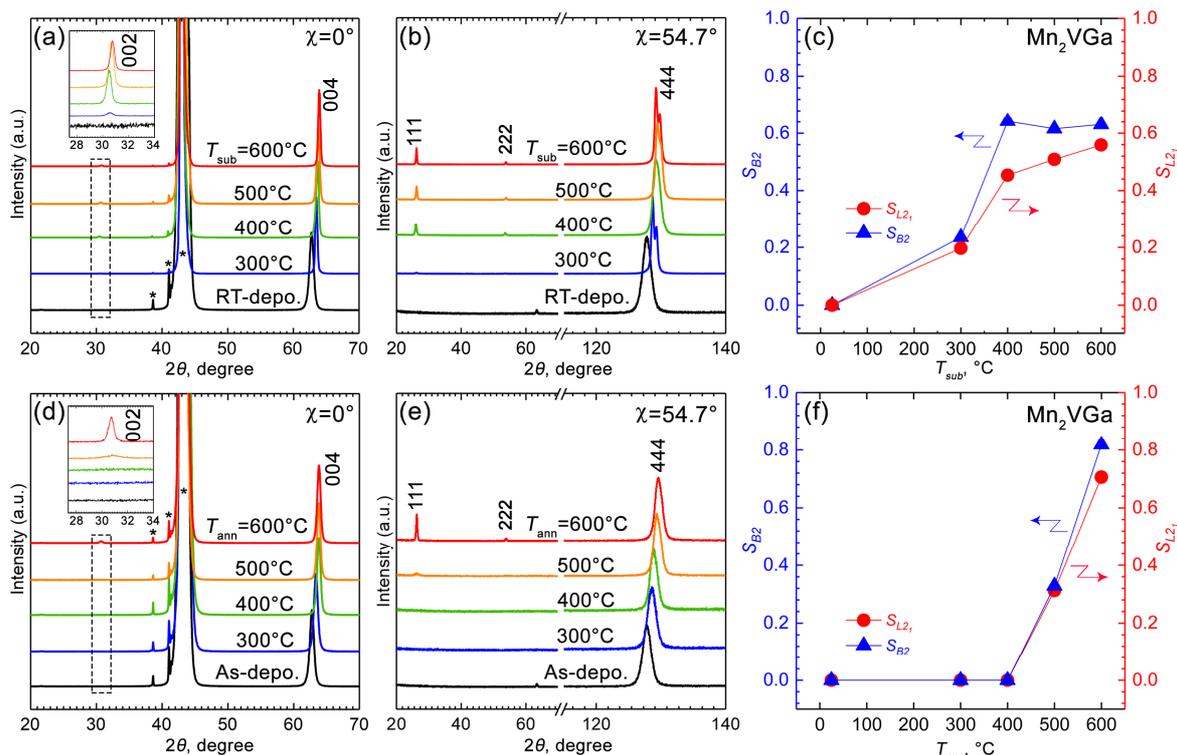


Fig. 2. Lab-XRD profiles measured from the out-of-plane ($\chi = 0^\circ$) and $\langle 111 \rangle$ directions ($\chi = 54.7^\circ$), and temperature dependence of S_{B2} and S_{L21} for the Mn_2VGa films (a–c) deposited at various T_{sub} , and (d–f) deposited at RT and post-annealed at various T_{ann} . Note that the insets in (a) and (d) shows enlarged (002) peaks, and the peaks labeled with * are from the MgO substrate.

Figure 2a shows the lab-XRD profiles of the Mn_2VGa ($x = 0$) films deposited at RT and $T_{sub} = 300$ – $600^\circ C$ with scattering vectors set to the out-of-plane ($\chi = 0^\circ$). All films exhibit diffraction peaks only from the $\{00l\}$ plane, indicating 001-oriented epitaxial growth of the Mn_2VGa films over the entire range of T_{sub} . The 004 peak position shifts toward a higher angle with increasing T_{sub} , which suggests lattice shrinkage along the $[001]$ direction. The 002

superlattice peak is not detected at RT and appears as the T_{sub} increased above 300°C, indicating the formation of a $B2$ ordered structure. **Fig. 2b** shows XRD profiles measured along the [111] direction of the Mn_2VGa films ($\chi = 54.7^\circ$). Similar to the 002 peak, the 111 superlattice peak becomes visible at T_{sub} above 300°C, indicating an $L2_1$ ordered structure in the samples. The shoulders in the 444 peaks are due to the contributions from Cu $K\alpha_1$ and $K\alpha_2$ lines with a small difference in wavelength [52]. **Fig. 2c** shows the variations of the degree of $B2$ and $L2_1$ order *i.e.*, S_{B2} and S_{L2_1} as a function of T_{sub} . The typical errors in the calculated S_{B2} and S_{L2_1} were less than 0.02 as estimated from the errors in the fitting. The value of S_{B2} increases to a maximum of 0.64 at 400°C and remains almost constant from 400 to 600°C. In contrast, S_{L2_1} increases monotonically with increasing T_{sub} , reaching a maximum value of 0.56 at 600°C. In the case of post-annealed Mn_2VGa films, 002 and 111 peaks are not observed below $T_{\text{ann}} = 500^\circ\text{C}$, as shown in **Fig. 2d and e**. However, the S_{B2} and S_{L2_1} values at $T_{\text{ann}} = 600^\circ\text{C}$; 0.82 and 0.71, respectively, are even larger than those of the film deposited at $T_{\text{sub}} = 600^\circ\text{C}$, indicating that a higher degree of $B2$ and $L2_1$ order can be obtained by post-annealing at high temperatures.

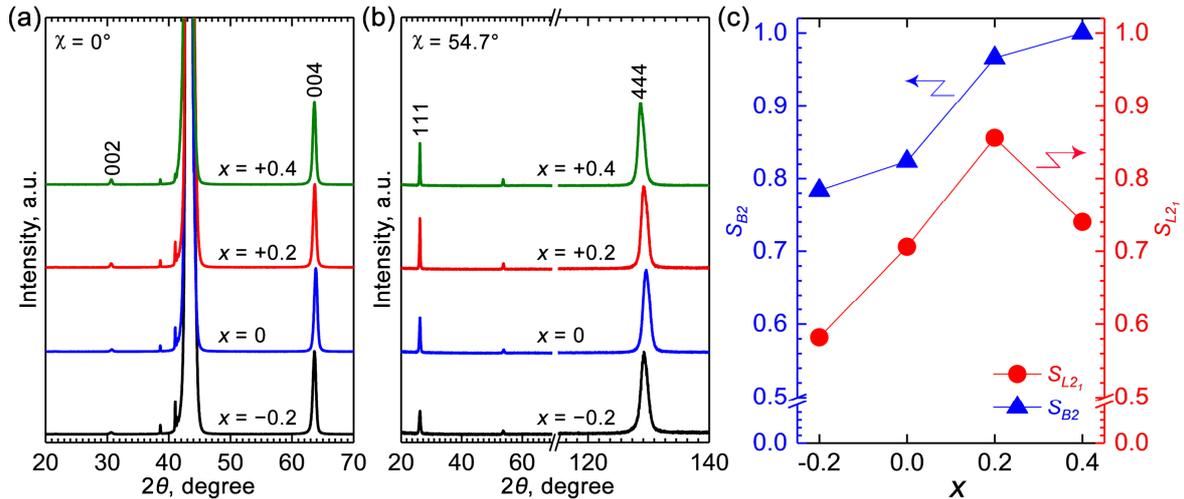


Fig. 3. Lab-XRD profiles for MVG films post-annealed at $T_{\text{ann}} = 600^\circ\text{C}$ measured from the (a) out-of-plane ($\chi = 0^\circ$) and (b) $\langle 111 \rangle$ directions ($\chi = 54.7^\circ$). (c) The x dependence of S_{B2} and S_{L2_1} .

Figure 3a shows the out-of-plane XRD profiles of $\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ ($x = -0.2, 0, +0.2, +0.4$) films post-annealed at 600°C . The observed peaks of 002 and 004 indicate the 001-oriented epitaxial growth and the presence of $B2$ ordering in all the compositions. Similarly, the 111 superlattice peak is detected from the $\langle 111 \rangle$ -direction patterns of all MVG films, **Fig. 3b**, indicating the formation of $L2_1$ -ordered structure. **Fig. 3c** shows the variations in S_{B2} and S_{L2_1} as functions of x . For the Mn-poor sample ($x = -0.2$), the values of S_{B2} and S_{L2_1} are 0.78 and 0.58, which are lower than those for $x = 0$. In contrast, the values of S_{B2} and S_{L2_1} significantly increase to 0.97 and 0.86, respectively at $x = +0.2$, indicating that the addition of Mn of $x = +0.2$ can achieve near-perfect S_{B2} and high S_{L2_1} . Further increasing the Mn concentration to $x = +0.4$ results in a slight increase in S_{B2} , but a decrease in $L2_1$ to 0.74.

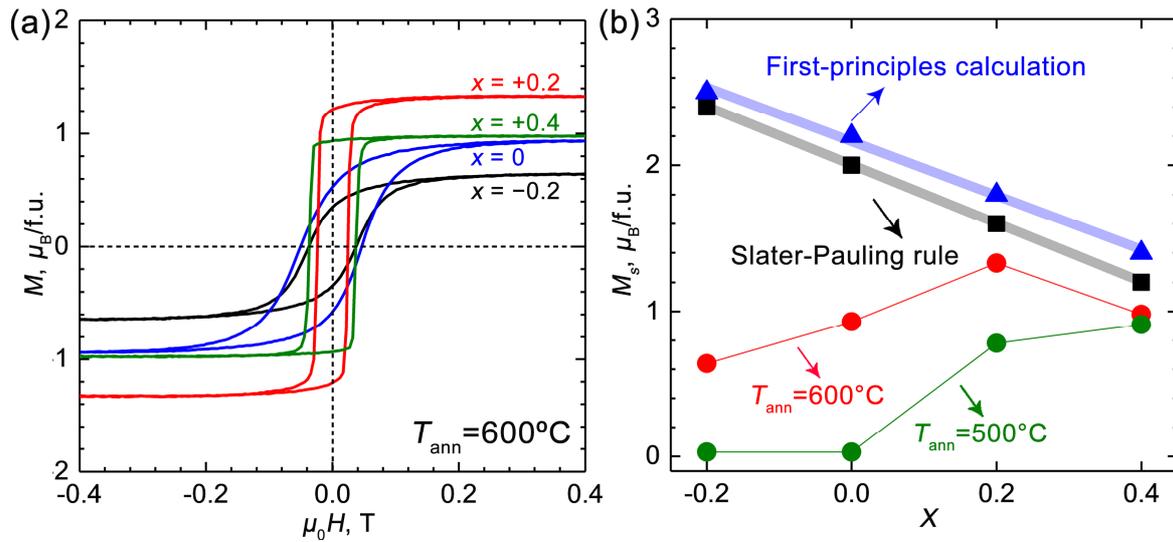


Fig. 4. (a) In-plane magnetization curves. (b) Measured and theoretical saturation magnetization, M_s as a function of x for MVG films measured at RT.

Figure 4a shows the in-plane magnetization curves for $\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ ($x = -0.2, 0, +0.2,$ and $+0.4$) films at $T_{\text{ann}} = 600^\circ\text{C}$. All MVG films reach magnetic saturation in the field range of ± 0.4 T. The saturation magnetization, M_s is $0.6 \mu_{\text{B}}/\text{f.u}$ for the Mn-poor sample with $x = -0.2$, and increases to 0.9 and $1.3 \mu_{\text{B}}/\text{f.u}$ at $x = 0$ and $+0.2$, respectively. Further increasing the Mn concentration to $+0.4$ leads to a decrease in M_s . The squareness of the magnetization curves

increased for the Mn-rich compositions. Note that the bulk M_s of Mn_2VGa was reported to be $1.7 \mu_B/\text{f.u}$ [11]. **Fig. 4b** shows the x dependence of M_s at $T_{\text{ann}} = 500$ and 600°C together with the values predicted by first-principles calculations and the Slater-Pauling (S-P) rule [53], $M_s = Z_t - 24$, where Z_t is the total number of valence electrons based on the nominal compositions in **Table 1**. The first-principles calculations show a decrease in M_s as x increases, which agrees with the S-P rule. However, the experimental M_s at $T_{\text{ann}} = 600^\circ\text{C}$ shows the opposite trend from $x = -0.2$ to $+0.2$, and the deviation between the experimental and calculation values decreases with increasing x , implying the improved atomic ordering for the Mn-rich films. The experimental trend of $x = +0.2$ and $+0.4$ follows the first-principles calculations and the S-P rule, reflecting that these two compositions have similarly high ordering. At $T_{\text{ann}} = 500^\circ\text{C}$, the Mn-poor and stoichiometric samples show no magnetization, which is consistent with the XRD results that atomic ordering is poor at this temperature. In contrast, the Mn-rich samples are well magnetized; the M_s value at 500°C for $x = +0.2$ is smaller than that at 600°C , whereas $x = +0.4$ has almost the same M_s value at 500 and 600°C . These results indicate that the Mn-rich compositions lower the ordering temperature in addition to the improved atomic ordering. Considering that highest $L2_1$ ordering and M_s close to the theoretical value are achieved in the Mn-rich sample with $x = +0.2$, we treat the $x = +0.2$ sample as representative of the Mn-rich compositions. The following detailed characterizations were performed on the samples with $x = -0.2, 0$, and $+0.2$.

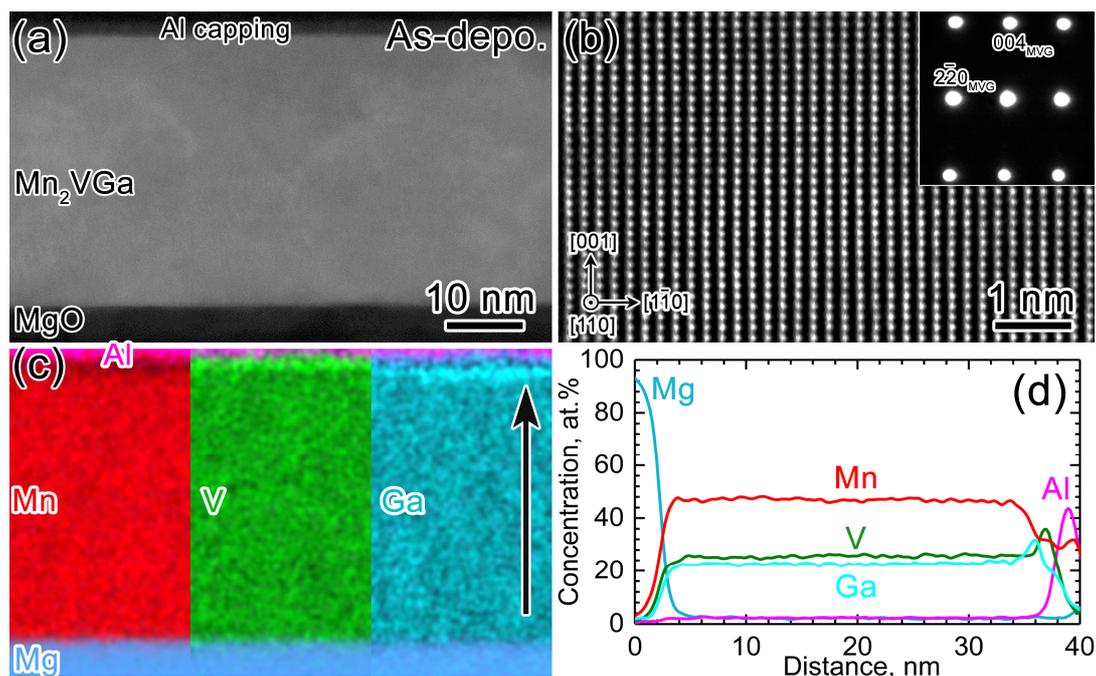


Fig. 5. (a) Low-magnification cross-sectional HAADF-STEM image of a MgO sub./Mn₂VGa/Al structure. (b) Atomic-resolution HAADF-STEM image and the corresponding NBED pattern of the Mn₂VGa layer. (c) EDS elemental maps for Al, Mn, V, Ga, and Mg, respectively, and (d) the corresponding line compositional profile along the direction indicated by the arrow in (c). Note that electron beam is parallel to the [110]_{MVG}.

Figure 5a shows a low-magnification cross-sectional HAADF-STEM image of the Mn₂VGa/Al films deposited at RT without post annealing. Note that the image was taken along the zone axis of [110]_{Mn₂VGa}. The imaging contrast within the Mn₂VGa layer is nearly homogeneous, indicating uniform growth of the film without pronounced phase separation. The atomic resolution HAADF-STEM image of the as-deposited Mn₂VGa shows uniform atomic column intensity, which suggests a random distribution of Mn, V, and Ga atoms, *i.e.*, disordered A2 structure, **Fig. 5b**. Accordingly, only the fundamental A2 reflections of 220 and 004 are detected in the NBED pattern. **Fig. 5c** shows the EDS elemental maps of Al, Mn, V, Ga, and Mg. The constituent elements exhibit a uniform distribution within the Mn₂VGa layer. The corresponding EDS line compositional profile analyzed along the direction indicated by the arrow in **Fig. 5c** reveals a nearly stoichiometric composition of Mn_{1.97}V_{1.08}Ga_{0.95}, **Fig. 5d**. In addition, slight V and Ga segregation is detected near the Mn₂VGa/Al interface.

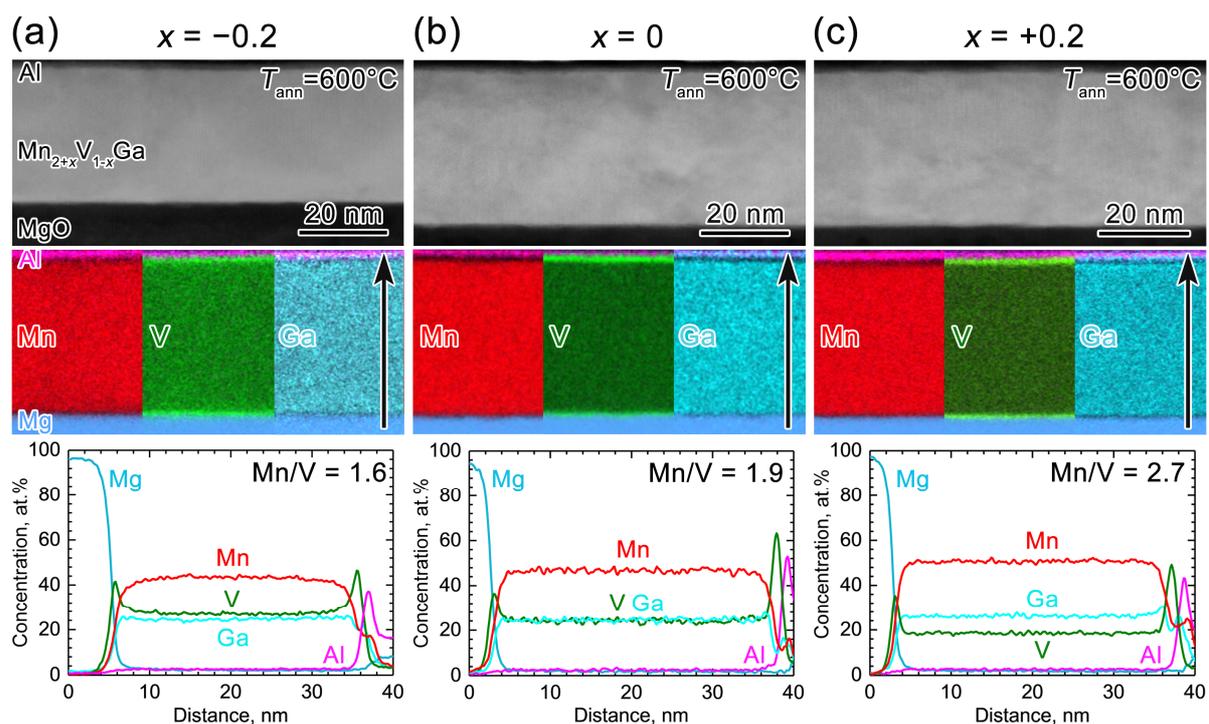


Fig. 6. Low-magnification cross-sectional HAADF-STEM images, EDS elemental maps, and compositional line profiles for post-annealed $\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ films with $x =$ (a) -0.2 , (b) 0 , and (c) $+0.2$, respectively.

Figures 6a–c show cross-sectional HAADF-STEM images and EDS elemental maps of $\text{MgO sub./Mn}_{2+x}\text{V}_{1-x}\text{Ga/Al}$ films post-annealed at 600°C . All MVG layers show homogeneous imaging contrast and sharp interfaces with Al capping layers, indicating the uniform growth. Cross-sectional EDS elemental maps and corresponding line compositional profiles show homogeneous distributions of Mn, V, and Ga elements in all MVG layers. The compositions for $x = -0.2$, 0 , and $+0.2$ are measured to be $\text{Mn}_{1.83}\text{V}_{1.14}\text{Ga}_{1.03}$ ($\text{Mn/V} = 1.6$), $\text{Mn}_{1.96}\text{V}_{1.03}\text{Ga}_{1.01}$ ($\text{Mn/V} = 1.9$) and $\text{Mn}_{2.13}\text{V}_{0.78}\text{Ga}_{1.09}$ ($\text{Mn/V} = 2.7$), respectively, which agree well with the XRF results. Compared with the RT-deposited Mn_2VGa film, **Fig. 6**, all post-annealed MVG films show the V segregation at both MgO/MVG and MVG/Al interfaces. Close inspection of the MgO/MVG interface shows that the V segregation is due to the formation of an epitaxial pure V phase with a thickness of ~ 1 nm, **Fig. S1**. Considering the paramagnetic nature of V, the V segregation has little influence on the magnetic properties of the MVG layers.

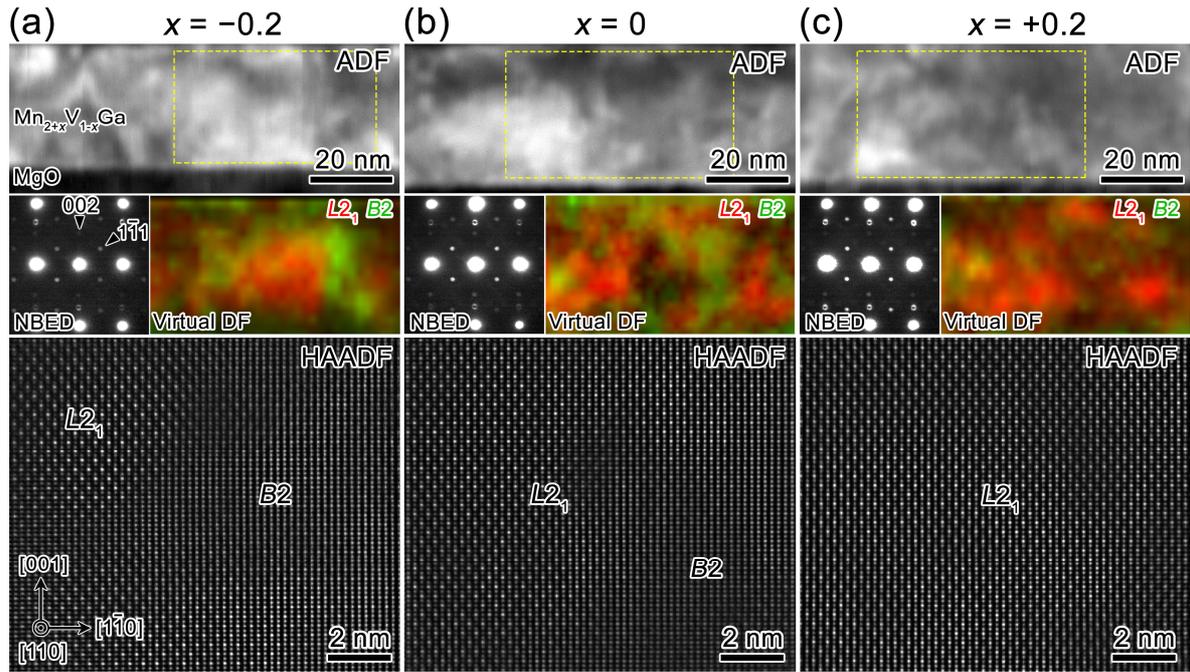


Fig. 7. Low-magnification ADF-STEM images, NBED patterns, VDF images of $L2_1$ and $B2$ structures, and atomic resolution HAADF-STEM images for post-annealed $Mn_{2+x}V_{1-x}Ga$ films with $x =$ (a) -0.2 , (b) 0 , and (c) 0.2 , respectively. Note that ADF/HAADF images and NBED patterns were taken along the $[110]_{MVG}$ zone axis, and $L2_1$ and $B2$ phases in the VDF images were reconstructed with a virtual aperture on the 111 and 002 superlattice spots in NBED patterns, respectively.

Figures 7a–c show ADF/HAADF-STEM images, NBED patterns, and virtual dark-field (VDF) images of post-annealed $Mn_{2+x}V_{1-x}Ga$ ($x = -0.2, 0, +0.2$) films. The NBED patterns were obtained by scanning the yellow dashed-box areas in the ADF images, and the VDF images illustrate the intensity distributions of 111 and 002 reflections in the same areas. The $L2_1$ ordered structure was colored in both red and green, while the $B2$ ordered structure was colored in green only. All MVG films show 002 and 111 superlattice spots in the NBED patterns, which confirms the formation of $B2$ and $L2_1$ structures in the whole range of x . The intensity of 111 and 002 superlattice reflections increases with increasing x , indicating the enhancement of both $B2$ and $L2_1$ ordering by the Mn addition. The VDF images show a coexistence of $B2$ (green) and $L2_1$ (red) structures in the Mn-poor ($x = -0.2$) and stoichiometric ($x = 0$) samples, **Figs. 7a and b**, which are further revealed by atomic resolution HAADF-STEM images in different contrast modulations along the $[001]$ direction; the $L2_1$ structure

shows a periodic arrangement of brightly imaged Ga-rich columns separated by three darkly imaged Mn/V columns, while only one-column interval is observed between two neighboring Ga-rich columns in the $B2$ structure. In contrast, the Mn-rich sample ($x = +0.2$) shows the predominance of the $L2_1$ phase, **Fig. 7c**, suggesting the improved atomic ordering due to the excess Mn addition.

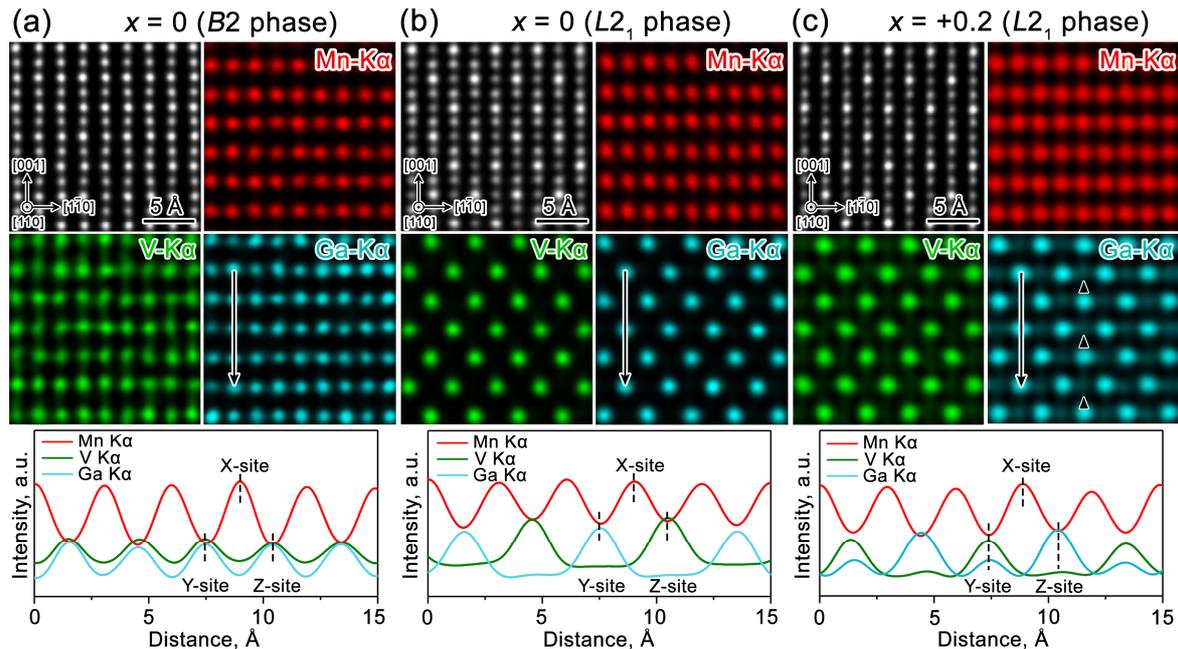


Fig. 8. Atomic resolution HAADF-STEM images, EDS elemental maps, and compositional line profiles of Mn, V, and Ga for post-annealed $\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ films with (a,b) $x = 0$ and (c) $x = +0.2$ acquired along $[110]_{\text{MVG}}$ zone axis.

Figures 8a-c show magnified HAADF-STEM images and the corresponding atomic-resolution EDS elemental maps obtained from stoichiometric ($x = 0$) and Mn-rich ($x = +0.2$) samples. Note that EDS elemental maps were processed using radial Wiener filtering to enhance the imaging contrast and signal-to-noise ratio of elemental line profiles. The site occupancy of each element in ideal and disordered $B2/L2_1$ structural models is summarized in **Table 2**. For the stoichiometric sample ($x = 0$), the $B2$ phase shows alternating Mn and V-Ga atomic layers along the $[001]$ direction, **Fig. 8a**. The same elemental occupancy in the V-Ga layer suggests an intermixing of V and Ga atoms (Model I), as evidenced by the EDS line composition profile along the arrow direction. On the other hand, Mn, V, and Ga elements in

the $L2_1$ phase periodically occupy individual atomic columns, **Fig. 8b**, which is consistent with the ideal $L2_1$ structure in Model II. In contrast, the Mn-rich sample ($x = +0.2$) shows faint Ga signals (indicated by arrows) in the V sites, respectively, in addition to an ordered atomic arrangement similar to the $L2_1$ phase in the stoichiometric sample. Combined with EDS line scan analysis, weak Ga intensity peaks are clearly observed in the original V sites (Y-site), indicating the intermixing between V and Ga atoms, which is consistent with the ideal structure in model III. In addition, Mn is also expected to partially occupy the V sites based on the XRF composition of $\text{Mn}_{2.09}\text{V}_{0.8}\text{Ga}_{1.08}$, however, no obvious Mn signal or intensity peak is detected from EDS results.

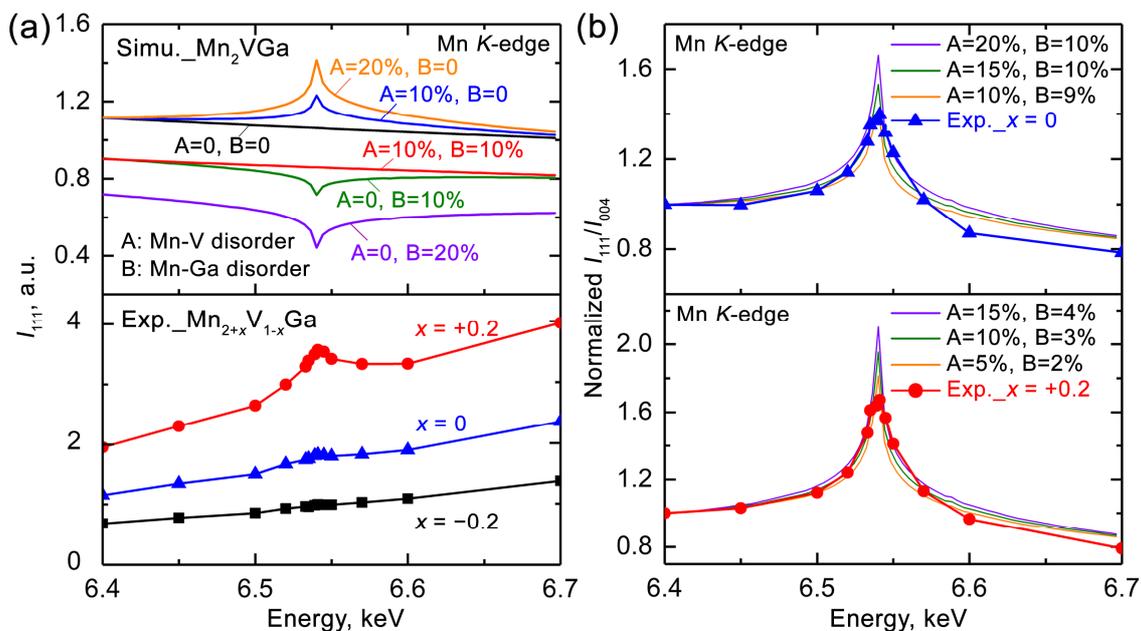


Fig. 9. Simulated and experimental X-ray energy dependence of (a) I_{111} for post-annealed MVG films and $L2_1$ -structure Mn_2VGa , and (b) normalized I_{111}/I_{004} for $x = 0$ and $+0.2$ samples with various Mn-V (A) and Mn-Ga (B) disorders, respectively, near the Mn K -edge. Note that the increased background slope with increasing x in (a) is due to the X-ray absorption by air.

Table 2 Site occupancy of Mn, V, and Ga for ideal $L2_1$, $B2$, and disordered structures in stoichiometric ($x = 0$, $\text{Mn}_{1.96}\text{V}_{1.03}\text{Ga}_{1.01}$) and Mn-rich ($x = +0.2$, $\text{Mn}_{2.09}\text{V}_{0.83}\text{Ga}_{1.08}$) samples.

Model No.	Structure	X-site (0, 0, 0),			Y-site (1/4, 1/4, 1/4)			Z-site (3/4, 3/4, 3/4)		
		Mn	V	Ga	Mn	V	Ga	Mn	V	Ga
		(1/2, 1/2, 1/2)								

I	$x = 0$ (ideal $B2$)	96	3	1	0	50	50	0	50	50
II	$x = 0$ (ideal $L2_1$)	96	3	1	0	100	0	0	0	100
III	$x = +0.2$ (ideal $L2_1$)	100	0	0	9	83	8	0	0	100
IV	$x = 0$ (with disorders)	81	10	9	10	80	10	9	10	81
V	$x = +0.2$ (with disorders)	96.5	2.5	1	14	73	13	2	5	93

Considering that the site occupancy revealed by atomic STEM-EDS maps is localized, the average information of atomic ordering in MVG films was further determined by combined lab-XRD and AXRD analysis. **Figure 9a** shows the simulated and experimental X-ray energy dependence of I_{111} for the MVG around the Mn K -absorption edge. The I_{111} profiles of Mn_2VGa ($x = 0$) were simulated with various fractions of Mn-V (A) and Mn-Ga (B) disorders based on $F_{111}^{L2_1} = |\{A f_{Mn} + (1-A) f_V\} - \{B f_{Mn} + (1-B) f_{Ga}\}|$, where f_x is the atomic scattering factor of element x . The simulated I_{111} profile exhibits a flat shape for the same amount of Mn-V and Mn-Ga disorders ($A = B = 0$ and 10%) due to the absence of f_{Mn} in $F_{111}^{L2_1}$, whereas an increase in Mn-V or Mn-Ga disorder changes the profile to be convex or concave, respectively. A comparison between experimental and simulated results suggests that stoichiometric ($x = 0$) and Mn-poor ($x = -0.2$) samples have almost the same amount of Mn-V and Mn-Ga disorders, respectively due to the flat-shape I_{111} profiles. However, the disorder in the Mn-rich sample ($x = +0.2$) cannot be determined solely from the shape of the I_{111} profile because even the ideal $L2_1$ ordered $Mn_{2.09}V_{0.83}Ga_{1.08}$ ($A = B = 0$) shows a peak near the Mn K -edge as the excess Mn atoms (9%) intrinsically occupying the V sites. Instead, we simulated the X-ray energy dependence of normalized I_{111}/I_{004} for stoichiometric and Mn-rich samples, as shown in **Fig. 9b**. In the simulation of the stoichiometric sample, A and B were set to 20% and 10%, 15% and 10%, and 10% and 9%, respectively, to reproduce the S_{B2} obtained by lab-XRD. The stoichiometric sample ($x = 0$) exhibits well-matched shapes and intensity between the simulated and experimental profiles by inducing nearly the same amount of Mn-V ($\sim 10\%$) and Mn-Ga ($\sim 9\%$) disorders, which agrees with the inference from the I_{111} simulations. Recalling $S_{L2_1} =$

0.71 and $f_{\text{Mn}} \approx f_{\text{V}}$ from lab-XRD, **Fig. 3c**, the V-Ga disorder (C) is calculated to be $\sim 10\%$ based on $|(f_{\text{V}} - f_{\text{Ga}})|S_{L2_1} = |\{(0.1f_{\text{Mn}} + (0.9-C)f_{\text{V}} + Cf_{\text{Ga}})\} - \{(0.09f_{\text{Mn}} + Cf_{\text{V}} + (0.91-C)f_{\text{Ga}})\}|$. In contrast, the Mn-rich sample ($x = +0.2$) has much lower disorders of $\sim 5\%$ Mn-V and 2% Mn-Ga from the AXRD analysis, as well as $\sim 5\%$ V-Ga disorder calculated by XRD. The average site-occupancy models for stoichiometric and Mn-rich samples are summarized in **Table 2**, denoted as Models IV and V, respectively.

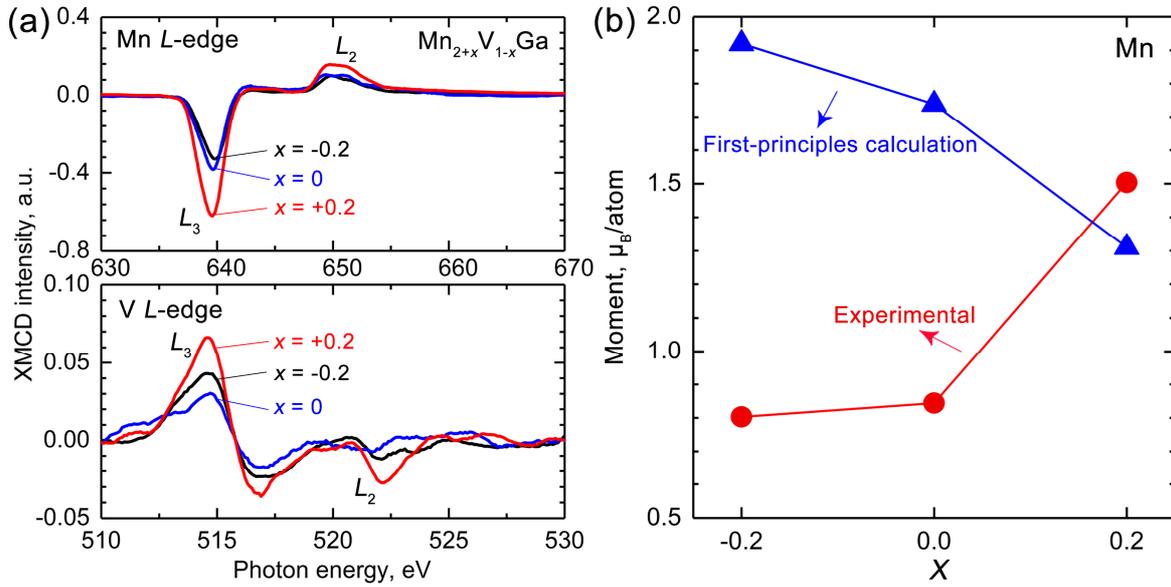


Fig. 10. (a) XMCD spectra around Mn and V $L_{3,2}$ -edges, and (b) experimental magnetic moments of Mn as a function of x for MVG films measured at RT. Note that the calculated Mn moments based on the L_{2_1} -order structural model are also shown for reference.

Figure 10a shows the XMCD spectra at the L -absorption edges of Mn and V obtained from $\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ ($x = -0.2, 0, +0.2$) films. Note that the probing depth of the TEY method is limited to $\sim 2\text{-}3$ nm from the surface [54], the XMCD results, especially the V moments, are significantly affected by the V segregation on the surface of annealed MVG films, **Fig. 6**. For all films, Mn shows a negative signal at the L_3 edge and a positive signal at the L_2 edge that are opposite to those of V, confirming the antiferromagnetic coupling between Mn and V sites [10,31]. The signal intensity at the Mn $L_{3,2}$ -edges increases with increasing the x , which suggests an increase in the Mn moment. The V L -edge intensity does not vary monotonically

with x due to the surface V segregation. **Fig. 10b** shows the x dependence of the Mn moment determined by the sum rule analysis [55], and the theoretical calculations based on $L2_1$ -ordered structure are also provided for reference. The experimental Mn moment slightly increases from $0.8 \mu_B/\text{atom}$ at $x = -0.2$ to $0.84 \mu_B/\text{atom}$ at $x = 0$, and then significantly rises to $1.5 \mu_B/\text{atom}$ with x increasing to $+0.2$. This trend is consistent with that of M_s , supporting the highest of atomic order for the Mn-rich sample. In contrast, a monotonic decrease of the calculated Mn moment with increasing the x is attributed to the antiferromagnetic coupling of increased Mn atoms at the V-site with those at the Mn-site, which partially counteracts the Mn moment.

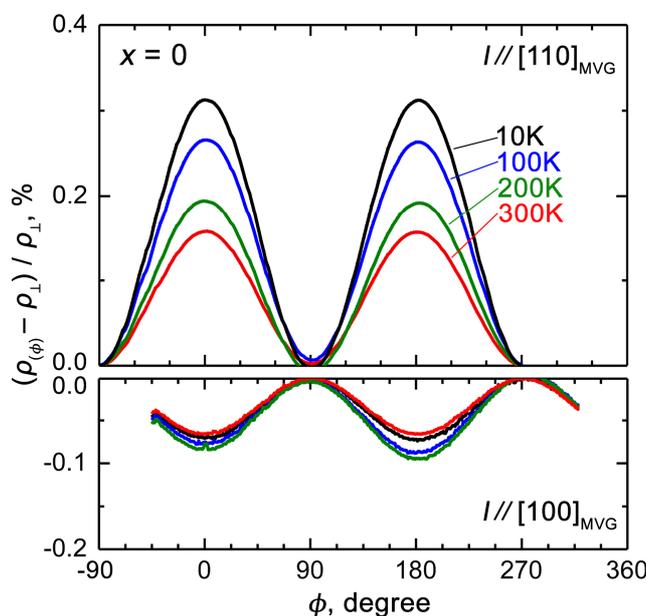


Fig. 11. The AMR ratio of the stoichiometric sample ($x = 0$) as a function of ϕ . Note that the current directions were aligned along $[110]_{\text{MVG}}$ and $[100]_{\text{MVG}}$, respectively, and the measurement temperature varied from 10 to 300 K.

We performed the AMR analysis to confirm the predictions obtained by the DOS calculations from the viewpoint of transport properties. **Figures 11** shows the ϕ dependence of the AMR ratio for the stoichiometric sample ($x = 0$) measured from 10 to 300 K. The composition dependence of the AMR ratio for $\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ ($x = -0.2, 0, +0.2$) films are provided in the Supplementary Materials, **Fig. S.2**. The sign of AMR ratio for Mn_2VGa is positive in the current direction along the $[110]_{\text{MVG}}$ and negative along $[100]_{\text{MVG}}$, as opposed

to those for Co_2MnGa , which shows positive and negative values for $I \parallel [110]$ and $I \parallel [100]$, respectively [56]. The AMR values of Mn_2VGa lie between -0.1% and $+0.3\%$, which is similar to the reported Co_2FeZ and Co_2MnZ with $Z = (\text{Al}, \text{Si}, \text{Ge}, \text{Ga})$ Heusler alloy films with AMR values typically well below 1% [38,40-42].

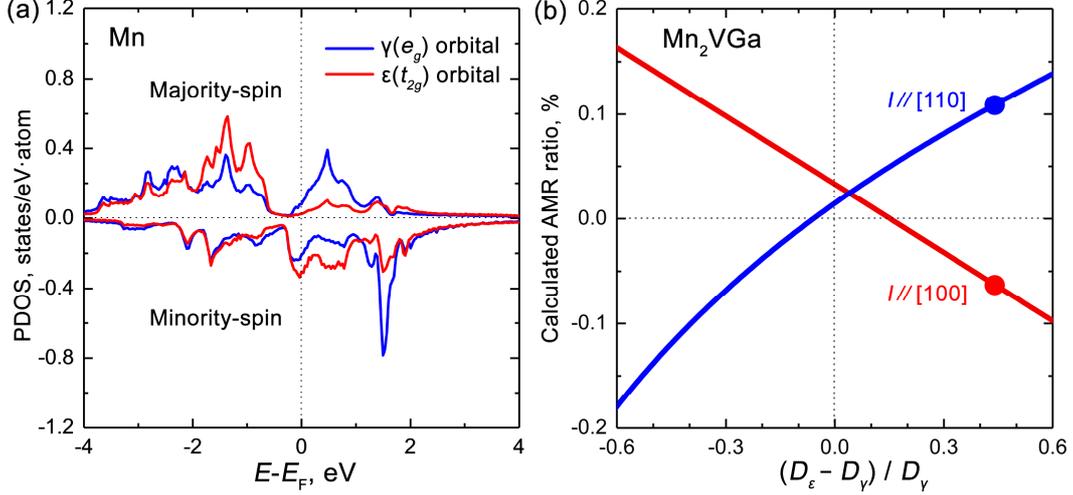


Fig. 12. (a) Partial DOS of γ and ϵ orbitals of Mn d state, and (b) calculated AMR ratio for $L2_1$ -ordered Mn_2VGa with the current directions aligned along $[110]_{\text{MVG}}$ and $[100]_{\text{MVG}}$, respectively. Solid circles in (b) indicate the calculated AMR ratios at the E_F .

The AMR ratios for the $L2_1$ ordered Mn_2VGa were theoretically analyzed by combining first-principles calculations and the developed Kokado's theory [40], which considers the s - d scattering of conduction electrons from s to d orbitals under a two-current model, **Figure S.3 and S.4**. **Figure 12a** shows the partial d -DOS of γ and ϵ orbitals of Mn atoms in $L2_1$ ordered Mn_2VGa . Here, only the Mn contribution is used due to the dominant spin-down d -DOS at E_F . According to the expressions given in Eqs. (S1) to (S4), the AMR ratios for two current directions, *i.e.*, $[110]_{\text{MVG}}$ and $[100]_{\text{MVG}}$ can be described as a function of $(D_{\epsilon,-}^{(d)} - D_{\gamma,-}^{(d)}) / D_{\gamma,-}^{(d)}$, where $D_{\epsilon,-}^{(d)}$ and $D_{\gamma,-}^{(d)}$ are the spin-down d -DOS of ϵ - and γ -orbitals, respectively, **Fig. 12b**. Based on the value of $(D_{\epsilon,-}^{(d)} - D_{\gamma,-}^{(d)}) / D_{\gamma,-}^{(d)}$ at the E_F for Mn_2VGa ; ~ 0.435 , the AMR ratio is calculated to be positive (negative) for the $[110]_{\text{MVG}}$ ($[100]_{\text{MVG}}$), which agrees well with the experimental results (Fig. 11), indicating that the sign reversal of the AMR ratio by the current

direction arises from the crystal field of MVG films affecting the s - d scattering process. The consistency between the experimental and calculated AMR results also demonstrates the rationality of the DOS calculations for predicting the P of MVG films.

4. Discussion

The present work reports an approach to achieve the high $B2$ and $L2_1$ ordering and saturation magnetization, M_s close to the theoretical value in the Mn_2VGa -based Heusler alloy films. The degree of $B2$ and $L2_1$ order and M_s of the MVG films were significantly improved by the addition of excess Mn. The Mn-rich sample ($x = +0.2$) at 600°C post-deposition annealing exhibits a predominant $L2_1$ phase with the highest values of S_{B2} and S_{L2_1} , 0.97 and 0.86, respectively, and a maximum M_s of 1.4 μ_B /f.u., which is close to the theoretical value. In addition, the excess Mn addition has no detrimental effect on spin polarization as predicted by the DOS calculations. Therefore, the Mn-rich composition with a high degree of $L2_1$ order is promising for MVG-based spintronic devices with excellent spin-dependent properties.

The stoichiometric Mn_2VGa sample shows improved $B2$ and $L2_1$ ordering with increasing annealing temperature, **Figures 2c and f**. The values of S_{B2} and S_{L2_1} by substrate-annealing are higher than those by post-annealing from 300 to 500°C, which is due to the enhanced mobility of adsorbed atoms at elevated substrate temperatures [57,58]. The excess Mn addition further improves the S_{L2_1} of the MVG films, **Fig. 3c**. The large S_{L2_1} ; ~ 0.86 for the Mn-rich sample at 600°C post-deposition annealing is mainly due to the predominant formation of the $L2_1$ phase, **Fig. 7c**, whereas the stoichiometric sample shows the co-existence of $B2$ and $L2_1$ phases, **Fig. 8c**. Because the order–disorder transition temperature from the $L2_1$ to the $B2$ phase, $T_t^{L2_1/B2}$, in Mn-based Heusler alloys tends to increase with increasing the number of valence electrons [59,60], the Mn-rich sample with $Z_t = 22.02$ is expected to have a higher $T_t^{L2_1/B2}$, *i.e.*, a higher driving force for the $L2_1$ -order than the stoichiometric sample, $Z_t = 21.9$. In addition, atomic

disorders are reduced by the addition of excess Mn, **Fig. 9**. The decrease in Mn-V and Mn-Ga disorders with increasing Mn concentration is attributed to the preferential occupation of Mn atoms in the Mn-site, resulting in lower V and Ga occupancy, **Table 2**. The addition of excess Mn can also reduce V-Ga disorders by increasing the chemical potential between V- and Ga-sites [61]. Therefore, the improved $B2$ and $L2_1$ ordering by the excess Mn addition is attributed to the increase in $T_t^{L2_1/B2}$ and the suppression of chemical disorders.

The M_s of $Mn_{2+x}V_{1-x}Ga$ films at $T_{ann} = 600^\circ C$ increases with increasing Mn concentration, from $x = -0.2$ to $+0.2$, **Figure 4a**. However, the trend of M_s varying with Mn concentration contradicts the Slater-Pauling rule and first-principles calculations, **Figure 4b**, suggesting that factors other than the valence electron count may be responsible for the M_s of $Mn_{2+x}V_{1-x}Ga$ films. Considering the antiferromagnetic coupling between Mn- and V-site atoms, **Fig. 10**, the increase in M_s is a result of competition arising from the simultaneously increased magnetic moments of Mn and V with increasing x . Because the atomic disorder strongly alters the magnetic interaction between the nearest neighboring atoms [62], the increase in the Mn moment can be explained by decreased Mn-V and Mn-Ga disorders, leading to reduced antiferromagnetic coupling between the Mn atoms of original Mn-site and both Mn_V and Mn_{Ga} antisites. Likewise, the large deviations between the experimental and calculated values for $x = -0.2$ and 0 can be attributed to a large amount of Mn-V and Mn-Ga disorders formation in the Mn-poor and stoichiometric samples, **Fig. 9**. For Mn-rich samples ($x = +0.2$ and $+0.4$), the experimental M_s trend agreed the trend of the Slater-Pauling rule and first-principles calculations, reflecting that these two compositions have similarly high ordering. At $T_{ann} = 500^\circ C$, the stoichiometric and Mn-poor samples ($x = 0$, and -0.2) show no magnetization, In contrast, the Mn-rich samples ($x = +0.2$, and $+0.4$) show magnetization, indicating that the Mn-rich compositions can not only improve the ordering but also lower the ordering temperature. In addition to the structural disorder, other factors such as secondary phase and finite

temperature effects may also influence the accuracy of the theoretical calculations. Nevertheless, since the variation of M_s is small below the Curie temperature, ~ 784 K and no secondary phase was observed by TEM analysis, the deviation between experimental and calculated M_s is mainly attributed to the atomic disorder in the MVG films.

The DOS calculations for the Mn_2VGa revealed that the spin polarization of the $L2_1$ ordered structure is much higher than that of the $B2$ ordered structure, **Figure 1**, indicating that atomic disorder can significantly deteriorate the spin polarization by smearing the band dispersion [45,63]. Compared with the stoichiometric composition ($x = 0$), the pseudo-gap around the E_F is preserved in the Mn-rich composition ($x = +0.2$) but is degraded in the Mn-poor composition ($x = -0.2$), suggesting that the formation of V_{Mn} rather than Mn_{V} antisites is detrimental to spin polarization. This finding is in contrast to that reported for Co-based Heusler alloy (Co_2YZ), where Co_{Y} rather than Y_{Co} destroys the half-metallic gap, leading to a substantial decrease in spin polarization [4,38,64]. HAADF-STEM observations showed that the $L2_1$ phase increases with increasing Mn concentration, and dominates the Mn-rich sample, **Fig. 7**. Based on the lab-XRD and AXRD analyses, **Figs. 3 and 9**, the average amount of V_{Mn} antisites in the Mn-poor and stoichiometric samples is determined to be $\sim 10\%$, which is four times larger than that in the Mn-rich sample; $\sim 2.5\%$. These results imply that the Mn-rich composition is superior for achieving higher spin polarization because excess Mn addition can readily lead to a high degree of $L2_1$ order while inhibiting the formation of V_{Mn} antisites. Furthermore, the sign reversal of the AMR ratio by the current direction in the stoichiometric sample is consistent with the theoretical calculations, **Figs. 11 and 12**, indicating that the DOS predictions obtained from first-principles calculations is reasonable for the fabricated MVG films.

5. Summary

This study has clarified the effects of off-stoichiometry on the atomic ordering, magnetic and transport properties for $\text{Mn}_{2+x}\text{V}_{1-x}\text{Ga}$ ($x = -0.2, 0, +0.2, +0.4$) films using a combination of (A)XRD, HAADF-STEM, and first-principles calculations. A high degree of $B2$ and $L2_1$ order in the Mn-rich sample ($x = +0.2$) leads to M_s close to the theoretical value, which indicates that the Mn-rich composition is promising for potential spintronic applications. The main conclusions are as follows:

1. The addition of Mn significantly improves S_{B2} and S_{L2_1} of MVG films from 0.78 and 0.58 ($x = -0.2$) to 0.97 and 0.86 ($x = +0.2$), respectively, which is attributed to the predominant formation of the $L2_1$ phase and the suppression of atomic disorder.
2. The increase in M_s with increasing Mn concentration is associated with the competition arising from the simultaneous increase in magnetic moments of Mn and V. The decreased Mn–V and Mn–Ga disorders reduces the antiferromagnetic coupling between the Mn- and V-site atoms, leading to the increase in the Mn and V moments.
3. First-principles calculations indicate that the Mn-rich composition with the $L2_1$ structure exhibits high spin polarization because of the inhibition of deleterious V_{Mn} antisites by the excess Mn addition.

Declaration of Competing Interest

The authors declare that they have no known competing financial interests or personal relationships that could have influenced the work reported in this paper.

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Supplementary Materials

Supplementary materials associated with this article can be found in the online version.

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