# **Supplemental Materials**

# Exploring the magnetic phase diagram and Hall resistivity suppression in centrosymmetric GdOs<sub>2</sub>Si<sub>2</sub> single crystal

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### Magnetic susceptibility over a wide temperature range:

Additional data for magnetic susceptibility over a wide temperature range is presented in Fig. S1, depicting the  $\gamma$ -T curves for  $\mu_0 H = 1$  T with H/[100], [110], and [001]. Each curve displays Curie-Weiss behavior at higher temperatures, and a distinctive peak at  $T_1 = 26.6$  K signifies the antiferromagnetic ordering of the Gd<sup>3+</sup> moments. The Curie constant (C) and Weiss temperature ( $\Theta_{\rm w}$ ) were determined by analyzing the linear temperature dependence of the inverse magnetic susceptibility above 100 K. For H/[100] and H/[110], C was calculated to be 8.39(1) emu K mol<sup>-1</sup> with  $\Theta_{\rm w}$  of +24.9(1) K, while for H/[001], C was found to be 8.20(1) emu K mol<sup>-1</sup> with  $\Theta_{\rm w}$  of +25.4(5) K. The calculated effective magnetic moment derived from the Curie constant was  $8.19(1) \mu_B$  for H//[100] and [110], and  $8.01(1) \mu_B$  for H//[001]. These values slightly exceed the theoretical value of  $\mu_{\rm eff} = 7.94 \,\mu_{\rm B}$  for Gd<sup>3+</sup> ions, suggesting a well-localized nature of the 4f electrons of  $Gd^{3+}$  ions, with the itinerant 5d electrons of Os ions contributing to the spin moment [43]. Despite the antiferromagnetic ordering, analogous to GdRu<sub>2</sub>Si<sub>2</sub> [26,27], the dominant interaction between Gd<sup>3+</sup> moments is considered to be ferromagnetic due to the positive Weiss temperature. Moreover, while the paramagnetic state is nearly isotropic, the magnetic susceptibility below  $T_1$  is highly anisotropic, notably with the susceptibility for H/[001] significantly lower than that for H/[100] or [110]. This observation suggests that the Gd<sup>3+</sup> moments are ordered along the c-axis, in line with the magnetic structure of GdRu<sub>2</sub>Si<sub>2</sub> [24].

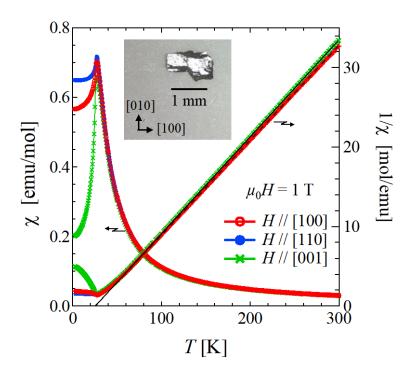


Fig. S1: Temperature dependence of magnetic susceptibility under a magnetic field of 1 T along [100], [110], and [001]. The solid black line represents the Curie-Weiss fitting. The inset shows the crystal structure of GdOs<sub>2</sub>Si<sub>2</sub> [35]. The inset is a photograph of the centrosymmetric GdOs<sub>2</sub>Si<sub>2</sub> single crystal. All measurements were carried out using the single crystal shown in this photograph.

### Supplemental Hall conductivity data:

Additional data for Hall conductivity are determined using the equation  $\sigma_{yx} = -\rho_{yx} / (\rho_{xx}^2 + \rho_{yx}^2)$  as presented in Fig. S2. The  $\sigma_{yx}$  increases linearly up to  $H_1$ , whereas the hump-like enhancement is identified in phase II. This enhancement is completely suppressed in phase II', leading to broad peak in phase III.

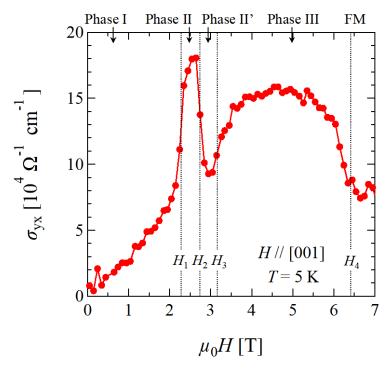


Fig. S2: Magnetic field dependence of  $\sigma_{yx}$  at 5 K for H//[001]. The gray and yellow regions correspond to the phases II and II', respectively.

### Supplemental Hall resistivity analysis:

We fitted the magnetic field dependence of Hall resistivity data  $(\rho_{yx})$  along with magnetization (M) and longitudinal resistivity  $(\rho_{xx})$  curves, as shown in Fig. S3. The calculated anomalous Hall component,  $\rho_{yx}^{A}$ , assuming intrinsic  $(\propto M\rho_{xx}^{2})$  and extrinsic  $(\propto M\rho_{xx})$  mechanisms, is plotted in the bottom panel of Fig. S3. As mentioned in the main text, adequate fitting could not be achieved; this analysis considers scattering of conduction electrons by relatively larger single skyrmions, whereas a short-period skyrmion lattice with smaller diameters is predicted in  $GdOs_2Si_2$ . The band folding resulting from the periodicity of the skyrmion lattice may contribute to increased resistivity. Therefore, a more appropriate approach is needed for analyzing the topological Hall effect.

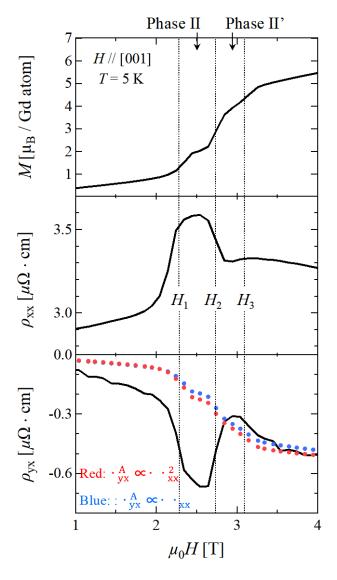


Fig. S3: Magnetic field dependence of magnetization (M), longitudinal resistivity ( $\rho_{xx}$ ), and Hall resistivity ( $\rho_{yx}$ ). The red and blue dots represent the anomalous Hall term calculated assuming intrinsic ( $\rho_{yx}^A \propto M \rho_{xx}^2$ ) and extrinsic ( $\rho_{yx}^A \propto M \rho_{xx}$ ) mechanisms, respectively.

### Supplemental electrical resistivity data:

Additional data for electrical resistivity are presented in Fig. S3. The  $\rho_{xx}$  vs T curves exhibit anomalies at characteristic temperatures of  $T_1$ ,  $T_2$ , and  $T_3$ , which correspond to the temperatures determined in the magnetization measurements. At  $\mu_0 H = 0$  and 1 T,  $\rho_{xx}$  decreases as the temperature is lowered below  $T_1$ . However, at  $\mu_0 H \ge 2$  T, a significant change in the temperature dependence of  $\rho_{xx}$  is observed. Specifically, at  $\mu_0 H = 2$  T,  $\rho_{xx}$  experiences an abrupt increase near  $T_2$  during cooling, followed by a subsequent decrease with further cooling. For  $\mu_0 H \ge 2.4$  T,  $\rho_{xx}$  shows a weak kink at  $T_1$  and a subsequent slight increase, followed by a further increase below  $T_2$ . Interestingly, as shown in the inset of Fig. S3, a negative magnetoresistance is observed not only below  $T_1$  but also at high temperatures, specifically below 40 K. This finding suggests the presence of the magnetic precursor effect, a phenomenon observed in isostructural Gd-based compounds [40,41].

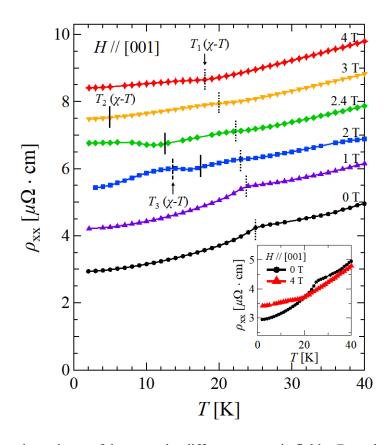


Fig. S4: Temperature dependence of the  $\rho_{xx}$  under different magnetic fields. Dotted, solid, and dashed lines denote the characteristic temperatures  $T_1$ ,  $T_2$  and  $T_3$ , respectively, determined from  $\chi$ -T measurements. The data have been shifted for clarity. The inset presents  $\rho_{xx}$ -T curves at  $\mu_0H=0$  T (black) and 4 T (red) without any offset.

# Supplemental $C_p$ data:

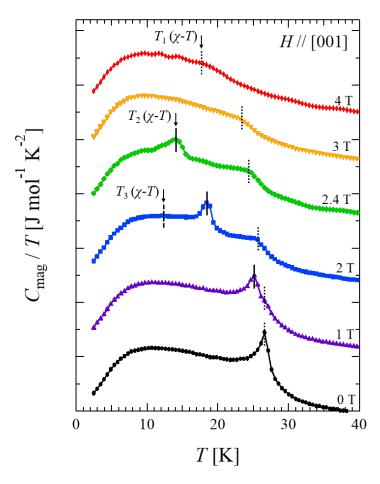


Fig. S5: Temperature dependence of  $C_p$  below 40 K under various magnetic fields. The magnetic transition temperatures at  $T_1$ ,  $T_2$ , and  $T_3$  determined from  $\chi$ -T measurements are indicated by dotted, solid, and dashed lines, respectively. The data have been shifted for clarity.

## Phase diagram obtained from an alternate crystal:

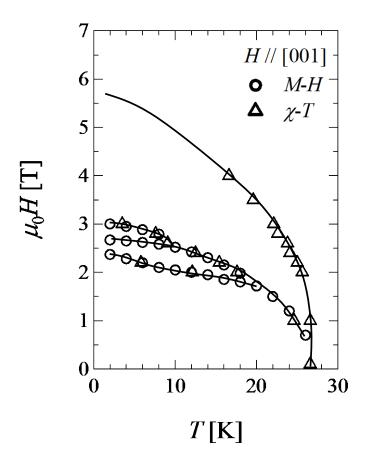


Fig. S6: Phase diagram obtained from an alternate crystal of  $GdOs_2Si_2$  for H//[001]. Circles and triangles represent the characteristic points observed in M-H and  $\chi$ -T measurements, respectively.