

1 **Simultaneous achievement of large anomalous Nernst effect and reduced thermal**
2 **conductivity in sintered polycrystalline topological Heusler ferromagnets**

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4 Koichi Oyanagi^{a,b,c,*}, Hossein Sepehri-Amin^{b,*}, Kenta Takamori^a, Terumasa Tadano^b, Takumi
5 Imamura^{a,b,d}, Ren Nagasawa^{b,d}, Krishnan Mahalingam^{b,1}, Takamasa Hirai^b, Fuyuki Ando^b,
6 Yuya Sakuraba^{b,d}, Satoru Kobayashi^a, and Ken-ichi Uchida^{b,d,e,*}

7

8 *a. Faculty of Science and Engineering, Iwate University, Morioka 020-8551, Japan.*

9 *b. National Institute for Materials Science, Tsukuba 305-0047, Japan.*

10 *c. Center for Sustainable Materials and Interfacial Science, Iwate University, Morioka 020-*
11 *8550, Japan*

12 *d. Graduate School of Science and Technology, University of Tsukuba, Tsukuba 305-8573,*
13 *Japan.*

14 *e. Department of Advanced Materials Science, Graduate School of Frontier Sciences, The*
15 *University of Tokyo, Kashiwa 277-8561, Japan.*

16

17 *Corresponding authors.

18 Email addresses: k.0yanagi444@gmail.com (K. Oyanagi), H.SEPEHRIAMIN@nims.go.jp (H.
19 Sepehri-Amin), UCHIDA.Kenichi@nims.go.jp (K. Uchida).

20 ¹ Prsent address: Sreenidhi University, Hyderabad, 501301, India.

21 Thermoelectric conversion based on the anomalous Nernst effect (ANE) is promising for
22 energy harvesting as its transverse geometry enables the design of large-scale thermoelectric
23 devices with simple structures. While topological ferromagnets, typically single crystals,
24 exhibit large ANE, achieving high conversion performance remains challenging because it also
25 requires high electric conductivity and low thermal conductivity. Here, we report enhanced
26 transverse thermoelectric conversion performance in polycrystalline topological ferromagnet
27 Co_2MnGa (CMG) prepared by spark plasma sintering. Optimization of the sintering conditions
28 for CMG leads to the anomalous Nernst coefficient of $7.5 \mu\text{V K}^{-1}$ at room temperature,
29 comparable to the highest value reported for the single crystals, and simultaneously reduces its
30 thermal conductivity by 34% compared to that of the single crystals without affecting the
31 electric conductivity. Owing to the transport properties that overcome conventional trade-off
32 relations, our optimized CMG slab shows the record-high value of the dimensionless figure of
33 merit for ANE at room temperature. Detailed nano/microstructure characterizations and first-
34 principles phonon calculations clarify the unconventional dependence of the transport
35 properties on the degree of crystalline ordering and morphology of crystal-domain boundaries.
36 The results reveal the potential of polycrystalline topological materials for transverse
37 thermoelectric applications and suggest alternative strategies to nanostructuring for enhancing
38 thermoelectric performance.

39 Keywords: Anomalous Nernst effect, Heusler alloy, Microstructure characterization,
40 Thermoelectric materials, First-principles phonon calculation.

41 **1. Introduction**

42 The anomalous Nernst effect (ANE) refers to the conversion of a longitudinal heat current
43 into a transverse electric field in a magnetic material with spontaneous magnetization. Because
44 of the transverse geometry of the thermoelectric conversion, ANE enables the construction of
45 thermoelectric devices with convenient scalability and easy fabrication [1-4]. The output
46 voltage of ANE increases simply by increasing a length of the device perpendicular to the
47 applied temperature gradient, realizing a large-scale and junction-less thermoelectric module,
48 which cannot be achieved by the Seebeck effect used in conventional thermoelectric modules.
49 However, low thermoelectric conversion performance of ANE prohibits practical applications
50 for thermoelectric devices.

51 Heusler alloys have been studied for several applications including spintronic devices
52 with high Curie temperatures and tunable half-metallicity [5], the conventional thermoelectric
53 devices with large Seebeck coefficients [6], and solid-state refrigeration with large
54 magnetocaloric effects and magneto shape memory alloys with giant magnetic-field-induced
55 strain effects [7]. Recently, magnetic Heusler alloys have been getting much attention for the
56 transverse thermoelectric applications requiring larger ANE. For instance, a ferromagnetic Weyl
57 semimetal Co_2MnGa (CMG) with the $L2_1$ fully ordered Heusler structure, one of topological
58 magnets exhibiting large anomalous Nernst coefficient S_{ANE} due to non-trivial band structures
59 [8-36], shows the largest S_{ANE} value around room temperature [13,14,18,19,23]. However, ANE
60 in CMG has been measured mostly in single crystals [13,18,19] ($S_{\text{ANE}} = 6.0 \sim 7.9 \mu\text{V K}^{-1}$) and
61 epitaxial thin films [14,23] ($S_{\text{ANE}} \sim 6.2 \mu\text{V K}^{-1}$), which are not compatible to scalability and
62 mass production.

63 For applications, polycrystalline slabs with large S_{ANE} are promising to construct low-
64 cost and large-scale devices based on ANE [37-42]. Owing to small anisotropy in the transport
65 properties along the crystal orientation [13] and robustness to the grain boundary scattering [38],
66 giant ANE has been reported not only in the polycrystalline films [29,34] but also in the
67 polycrystalline slabs made by using a spark plasma sintering (SPS) method [37,38,41]. SPS is
68 a versatile pressure-assisted sintering method in short time and low energy cost, and thus useful
69 for controlling the microstructure in polycrystalline thermoelectric materials to improve their
70 thermoelectric performance [43-45]. Furthermore, Ravi et al. demonstrated the remarkable
71 change of S_{ANE} in Fe-based alloys by microstructure engineering [46]. Therefore, the
72 comprehensive understanding of the transport properties and detailed microstructure is crucial
73 for the improvement of the performance of ANE in polycrystal materials for thermoelectric
74 applications based on ANE.

75 In this study, we prepared polycrystalline CMG slabs with various sintering conditions
76 using the SPS method and investigated their transport properties to optimize thermoelectric
77 conversion performance of ANE, which is often evaluated by the dimensionless figure of merit
78 [47-49]:

$$79 \quad z_{\text{ANE}}T = \frac{S_{\text{ANE}}^2 \sigma}{\kappa} T, \quad (1)$$

80 where σ is the electric conductivity and κ the thermal conductivity at absolute temperature T .
81 The CMG slab sintered at a high temperature and high pressure exhibits $S_{\text{ANE}} \sim 7.5 \mu\text{V K}^{-1}$,
82 which is comparable to the best value in the single- and poly-crystalline CMG slabs at room
83 temperature. We also achieved the decrease of κ with maintaining sufficiently large σ and S_{ANE} ,
84 resulting in a record-high value of $z_{\text{ANE}}T$ around room temperature among all the bulk magnetic
85 materials reported so far. We then performed detailed nano/microstructure analysis on the
86 samples to clarify the influence of the nano/microstructure on the transport properties.
87 Transmission electron microscopy (TEM) results revealed the importance of the crystal growth
88 of the $L2_1$ ordered phase within the samples for showing large S_{ANE} even if its existence cannot
89 be detected by the X-ray diffraction (XRD). In addition to the conventional $L2_1$ and $B2$ phases
90 in CMG, we found an unknown crystal phase with a size of ten nanometers. This length scale
91 coincides with the scale of mean free paths for phonons which mainly contribute to the thermal
92 conductivity obtained by a first-principles calculation, suggesting that the nanometer-scale
93 crystal boundaries increase the phonon scattering and cause small κ . Our results provide an
94 insight into the correlation between the transport properties and nano/microstructures within
95 the sample, which is important for the simultaneous optimization of ANE, electric conductivity,
96 and thermal conductivity.

97 **2. Experimental**

98 The polycrystalline CMG slabs were prepared under various sintering conditions from
99 powder of CMG ingots. The detailed recipe for the preparation of CMG ingots is described in
100 Supplementary Information and Ref. 37. We crushed the CMG ingots using a mortar and
101 planetary ball mill, followed by sieving the ball-milled CMG powder through a 63 μm mesh.
102 An inductively coupled plasma optical emission spectrometer determined the composition of
103 the CMG powder to be $\text{Co}_{52.1}\text{Mn}_{23.1}\text{Ga}_{24.8}$. We loaded the CMG powder into a graphite die with
104 a diameter of 10 mm and sintered it under various conditions. We examined nine sintering
105 conditions combining three sintering temperatures of $T_{\text{sinter}} = 600, 700, \text{ and } 800^\circ\text{C}$ with three
106 maximum sintering pressures of $p_{\text{max}} = 30, 60, \text{ and } 90 \text{ MPa}$. We kept T_{sinter} and p_{max} for 10 min
107 in all the conditions. In the following, we define the sample name as $\text{CMG}(T_{\text{sinter}}, p_{\text{max}})$ for each
108 sintering condition. The sintered CMG slabs were cut into a rectangular shape with a length of

109 9-10 mm, width of 2 mm, and thickness of 0.4-0.9 mm for measuring the transport properties
110 and magnetization M , and into a disc with a diameter of 10 mm and thickness of 1 mm for
111 measuring the thermal diffusivity, using a diamond wire saw. Note that the variation in the
112 shape of the rectangular samples does not affect the measurement results.

113 We measured ANE at room temperature and atmospheric pressure using a homemade
114 sample holder (Fig. 1a). The sample holder consists of two anodized Al plates. The large one
115 works as a thermal bath. The small one is equipped with a chip heater and is attached to the
116 large one but thermally isolated from it by inserting a Bakelite board to create a temperature
117 difference between the two plates. A sample was bridged between the plates and fixed with a
118 high-thermal conductivity adhesive sheet. A uniform temperature difference along the x
119 direction was generated using the chip heater. Because of the thermal resistance between the
120 sample and plates due to the presence of adhesive sheets, the temperature differences between
121 the ends of the sample and between the plates are different [50]. To accurately determine S_{ANE} ,
122 we estimated the actual value of the temperature gradient in the x direction $\nabla_x T$ directly from a
123 temperature-profile image at the surface of the sample coated with black ink using an infrared
124 camera. We measured the thermoelectric voltage along the y direction V_y , i.e., the sample width
125 direction, with the magnetic field \mathbf{H} along the out-of-plane direction and converted V_y into the
126 transverse electric field $E_y = V_y/w = S_{ANE}\nabla_x T$, where w is the sample width. The anomalous Hall
127 effect was measured in the same setup for the ANE measurement, where a charge current was
128 applied instead of the thermal gradient. The Seebeck coefficient and longitudinal electric
129 conductivity were measured using a Seebeck Coefficient/Electric Resistance Measurement
130 System (ZEM-3, Advance Riko, Inc.), which is similar to the system used in Ref. 51. The
131 sample is clamped by two metallic blocks and is attached by two R-type (PtRh-Pt)
132 thermocouple probes with the distance of 6 mm in a furnace under a He atmosphere. To measure
133 the Seebeck coefficient, a temperature gradient is applied to the sample by heating one metallic
134 block, and the resultant temperature difference and thermoelectric voltage at the same positions
135 were measured simultaneously using the probes. By applying a charge current to the sample
136 through the metallic blocks and measuring the voltage between the probes, we performed the
137 standard direct current four-terminal method for measuring the longitudinal electric
138 conductivity. The longitudinal resistivity of our samples is in the range from 1 $\mu\Omega$ m to 4 $\mu\Omega$
139 m (see Fig. S1a). The thermal conductivity was estimated by multiplying the thermal diffusivity,
140 specific heat, and density. The disc shaped samples coated with black ink were used for the
141 laser flash method (LFA1000, Linseis Messgeraete GmbH) to measure the thermal diffusivity.

142 The specific heat and density were measured using differential scanning calorimetry (DSCvesta,
143 Rigaku Holdings Corp.) and Archimedes method, respectively. Note that the measurement
144 results are not affected by the direction in which the transport properties were measured on the
145 sample because of the homogeneity of the polycrystal slab [38]. The magnetization as a function
146 of temperature was measured in the range from 300 K to 850 K using a superconducting
147 quantum interference device equipped with a vibrating sample magnetometer (SQUID-VSM,
148 Quantum Design) and from 5 K to 350 K using a superconducting quantum interference device
149 (SQUID) magnetometer (MPMS-5L, Quantum Design), respectively. Scanning electron
150 microscopy (SEM) was performed using a Carl Zeiss CrossBeam 1540EsB microscope
151 equipped with an energy-dispersive spectroscopy (EDS) detector. Scanning transmission
152 electron microscopy (STEM) was conducted using a Titan G2 80-200 (FEI) with a probe
153 aberration corrector. The lift-out method was used to prepare the TEM specimens using a
154 focused ion beam system Helios G4-UX DualBeam (FEI). The surfaces of the samples were
155 observed using an ultra-low voltage SEM JSM-7800F Prime (Jeol Ltd.).

156 3. Results and discussion

157 Figure 1b shows the H dependence of E_y for CMG(800, 60) at different $\nabla_x T$ values. Clear
158 E_y signals appear by applying $\nabla_x T$ and H . The magnitude of the E_y signal increases by increasing
159 $\nabla_x T$ and its sign reverses with respect to the sign of H . By increasing $|H|$, the E_y signal is
160 saturated at around $|\mu_0 H| \sim 0.8$ T, which is consistent with the saturation field of M (see the
161 inset to Fig. 1b), indicating that ANE mainly generates the E_y signal. In this setup, an H -linear
162 signal due to the ordinary Nernst effect also appears. We subtracted the ordinary Nernst
163 component by linear extrapolation for the results above the saturation field, represented as the
164 colored dashed lines in Fig. 1b, and obtained the ANE component E_{ANE} at $H = 0$ (see the colored
165 dots). We estimated $S_{\text{ANE}} = E_{\text{ANE}}/\nabla_x T$ to be $\sim 7.5 \mu\text{V K}^{-1}$ for CMG(800, 60) by a linear fit to the
166 $\nabla_x T$ dependence of E_{ANE} in Fig. 1c. We obtained S_{ANE} for all the samples through the same
167 procedure.

168 We show the H dependence of E_y for CMG(600, p_{max}), CMG(700, p_{max}), and CMG(800,
169 p_{max}) in Figs. 2a, 2b, and 2c, respectively. We found clear anomalous Nernst signals appear in
170 all the samples and summarized their estimated S_{ANE} values in the left panel of Fig. 2d at room
171 temperature. S_{ANE} monotonically increases by increasing T_{sinter} , and the relationship of S_{ANE} at
172 the same T_{sinter} value is $\text{CMG}(T_{\text{sinter}}, 30) < \text{CMG}(T_{\text{sinter}}, 60) \sim \text{CMG}(T_{\text{sinter}}, 90)$. All the samples
173 show relatively large S_{ANE} ($> 2 \mu\text{V K}^{-1}$), and the maximum S_{ANE} value of $7.5 \mu\text{V K}^{-1}$ in
174 CMG(800, 60) is the largest among all the values previously reported in polycrystalline magnets

175 29,30,32,34,36-38,46,48,49,52-54] including topological materials. More importantly, the
176 maximum S_{ANE} value in the polycrystalline CMG slab is comparable to or even larger than that
177 in the single-crystalline CMG slabs [13,18,19] (see the blue and red dashed lines in the left
178 panel of Fig. 2d).

179 To further investigate large ANE in the polycrystalline CMG slabs, we estimated the
180 anomalous Nernst conductivity α_{xy} . The left panel of Fig. 2e shows the obtained α_{xy} values in
181 all the samples using the formula $S_{ANE} = \rho_{xx}\alpha_{xy} - (\rho_{AHE}S_{SE}/\rho_{xx})$ with the measured longitudinal
182 resistance ρ_{xx} , anomalous Hall resistivity ρ_{AHE} , and Seebeck coefficient S_{SE} (see Fig. S1). α_{xy}
183 depends on the sintering condition and its trend is similar to that of S_{ANE} , while both S_{ANE} and
184 α_{xy} are independent of the saturation magnetization M_s (see the right panels in Figs. 2d and 2e).
185 The maximum value of $\sim 3 \text{ A m}^{-1} \text{ K}^{-1}$ is comparable to that in the single-crystalline CMG
186 samples [13,18,19]. This indicates the crucial role of the Berry curvature and electronic band
187 structure at the Fermi level even in the polycrystals in showing large S_{ANE} , consistent with the
188 recent findings [29,30,32-38,40,41].

189 We next focus on $z_{ANE}T$ to discuss the transverse thermoelectric performance of the
190 polycrystalline CMG slabs. σ and κ , which is obtained using the density, specific heat, and
191 thermal diffusivity (see Fig. S2), for all the samples are summarized in Figs. 3a and 3b. We
192 found that σ and κ of the samples prepared at $T_{\text{sinter}} = 700^\circ\text{C}$ and 800°C are larger than those of
193 the sample prepared at $T_{\text{sinter}} = 600^\circ\text{C}$. Although σ of the samples prepared at $T_{\text{sinter}} = 700^\circ\text{C}$ and
194 800°C is comparable to that of the single-crystalline CMG samples, κ is maximally $\sim 34\%$
195 smaller than that of the single crystal [19]. This indicates that we successfully reduced κ without
196 decrease of σ and S_{ANE} , which is important for improving $z_{ANE}T$ (see Eq. 1). Fig. 3c shows the
197 sintering condition dependence of $z_{ANE}T$ for all the samples, which is estimated from the results
198 in Figs. 2d, 3a, and 3b. The overall trend is determined primarily by S_{ANE} . The CMG(800, 60)
199 sample shows the maximum value of $\sim 8.0 \times 10^{-4}$, which is surprisingly greater than that for the
200 single-crystalline CMG slab ($z_{ANE}T \sim 2.0 \times 10^{-4}$ in Ref. 13 and $\sim 6.6 \times 10^{-4}$ in Ref. 19 shown as
201 the red and blue dashed lines, respectively). Furthermore, this value is much larger than $z_{ANE}T$
202 in other magnetic materials [12,13,18,19,21,27,46,48,49,52-54] exhibiting large ANE, such as
203 the single-crystalline Fe_3Ga slab [21] and the polycrystalline SmCo_5 -type permanent magnets
204 [48], summarized in Fig. 3d.

205 Now, we consider the origin of the high-performance of ANE in the sintered CMG slabs.
206 We found that the samples sintered at $T_{\text{sinter}} = 600^\circ\text{C}$ and 700°C have a lower relative density,
207 the ratio of the measured density to the theoretical density, than that of the samples sintered at
208 800°C (see Fig. S2) and a rough surface with remaining pores and microparticles (characterized

209 by ultra-low voltage SEM as shown in Fig. S3). These indicate that the samples sintered at
210 lower T_{sinter} are insufficiently densified, resulting in small S_{ANE} in CMG(600, p_{max}) and
211 CMG(700, 30). In fact, the CMG ingot annealed at 600°C with the relative density nearly of
212 100% exhibits S_{ANE} of $5.4 \mu\text{V K}^{-1}$, which is much larger than that of the insufficiently densified
213 CMG(600, p_{max}) ($S_{\text{ANE}} = 2 \sim 4 \mu\text{V K}^{-1}$), suggesting the correlation between S_{ANE} and the relative
214 density, rather than the exposed temperature. On the other hand, although both CMG(800, 30)
215 and CMG(800, 90) show the relative density of nearly 100% and dense morphology, CMG(800,
216 90) shows larger S_{ANE} than CMG(800, 30), indicating that the difference in the sample density
217 cannot explain large ANE in CMG(800, 90). Therefore, to understand the origin of large S_{ANE}
218 in CMG(800, 90), we performed the micro- and nano-scale structure analysis, i.e., SEM, energy
219 dispersive X-ray spectrometry (EDS), and high-resolution high-angle annular dark field
220 (HAADF) scanning transmission electron microscopy (STEM), on two samples.

221 Figures 4a and 4b show the SEM-EDS maps of Co, Mn, and Ga for the CMG(800, 90)
222 and CMG(800, 30) slabs. We found an inhomogeneous distribution of Mn in both samples
223 where Mn segregation can be seen at the surface of particles close to the grain boundary region.
224 In both samples, the typical grain size is comparable (a few to several tens of micrometers).
225 This grain size is consistent with the size of the initial powder of CMG, which was sieved
226 through a $63 \mu\text{m}$ mesh.

227 Figures 5a, 5b, and 5c show high resolution HAADF-STEM images and nano-beam
228 electron diffraction patterns obtained from CMG(800, 90) and CMG(800, 30). Although the
229 bulk XRD patterns show only fundamental diffraction peaks of the $A2$ phase (see Fig. S4), the
230 nano-beam diffraction patterns in the i and ii regions in Fig. 5a indicate the presence of the $L2_1$
231 and $B2$ ordered phases by 111 and 002 superlattice reflections in the diffraction patterns
232 obtained along $[111]$ zone axis of matrix phase, respectively, indicating that the ordered
233 structure of CMG(800, 90) varies in the nanoscale containing. We found that the electron beam
234 diffraction pattern in the iii region is different from that of both $L2_1$ and $B2$ phases; an additional
235 superlattice reflection appears diagonally on either side of the 002 spot indicated by the white
236 arrows in the bottom of the right panels of Fig. 5a. To closely see the crystal structure of this
237 unconventional modulated phase, we show the magnified HAADF-STEM images for the $L2_1$,
238 $B2$, and modulated phases in Fig. 5c. In comparison with the $L2_1$ and $B2$ structures, the
239 modulated phase consists of the relatively displaced atoms in the diagonal direction (see red
240 colored dots indicated by the white arrows in the right panel of Fig. 5c), similar to a martensite.
241 Although the TEM observation gives the local information, CMG(800, 30) seems to have a
242 larger amount of the modulated phase than CMG(800, 90) (see the lines of the displaced atoms

243 indicated by the white arrows in Fig. 5b), suggesting that the increase of the sintering pressure
244 at high sintering temperature facilitates the transformation of the modulated phase into the $L2_1$
245 and/or $B2$ phases.

246 We also found clear difference between CMG(800, 30) and CMG(800, 90) in the M - T
247 curves shown in Fig. 6. A large thermal hysteresis appears in CMG(800, 30) within the T range
248 from 500 K to 750 K, while it almost disappears in CMG(800, 90). The observed thermal
249 hysteresis is irrelevant to the magnetic ordering transition because M appears at around 800 K.
250 The onset temperature of M for CMG(800, 90) is lower than CMG(800, 30), and CMG(800,
251 30) shows larger M than CMG(800, 90). A similar thermal hysteresis has been observed in the
252 thin film of CMG [55] and other Heusler alloys with the martensitic transformations caused by
253 the distortion of the crystal structure [56-58]. In our case, the observed martensitic-
254 transformation-like hysteresis can be caused by the diagonal displacement of the atoms in the
255 modulated phase (see Fig. 5c). Although determination of the actual Curie temperature is
256 difficult in our case due to the application of the large magnetic field, the onset temperature of
257 M at 1 T for CMG(800, 90) is closer to the literature Curie temperature for $L2_1$ -type CMG [59]
258 (~ 685 K) than that for CMG(800, 30). By measuring the M - T curves at 1 T at low temperatures
259 (see the inset to Fig. 6), we obtained M_s at $T = 5$ K for CMG(800, 30) as $4.2 \mu_B \text{ f.u.}^{-1}$ and
260 CMG(800, 90) as $4.1 \mu_B \text{ f.u.}^{-1}$. CMG(800, 90) shows M_s consistent with the experimental and
261 theoretical values for $L2_1$ -type CMG [59,60] ($\sim 4.1 \mu_B \text{ f.u.}^{-1}$) and closer to the experimental
262 value for the $B2$ -type CMG film [61] at 4.2 K ($\sim 3 \mu_B \text{ f.u.}^{-1}$) than that for CMG(800, 30). All the
263 results indicate that the magnetic properties of CMG(800, 90) are more similar to those of
264 $L2_1/B2$ -type CMG than those of CMG(800, 30), suggesting the transformation from the
265 modulated phase into the $L2_1$ and/or $B2$ phases. This interpretation is consistent with the TEM
266 observation. Therefore, the sintering pressure at high sintering temperature affects the degree
267 of the crystalline orders in the samples.

268 The above results confirm that the degree of the crystalline order is important for
269 obtaining large S_{ANE} [21,62,63]. We found that CMG(800, 90) exhibits the larger value of S_{ANE}
270 than that in CMG(800, 30), which has more modulated phase than the $L2_1$ and/or $B2$ phases.
271 Because the theoretical origin of large ANE in CMG is the topological electronic band structure
272 in the fully ordered $L2_1$ phase [13,18,62], our results suggest that ANE in the modulated phase
273 seems to be small, and thus the reduction of the modulated phase is crucial for obtaining large
274 S_{ANE} .

275 Now, we focus on the reduction of κ in CMG(800, 30) and CMG(800, 90). The inset to
276 Fig. 3b shows the sintering condition dependence of the nonelectronic thermal conductivity $\Delta\kappa$
277 $= \kappa - \kappa_{el}$, where the electronic thermal conductivity κ_{el} is estimated via the Wiedemann-Franz
278 law with the free-electron Lorenz number of $2.44 \times 10^{-8} \text{ W } \Omega \text{ K}^{-2}$. Since the values of σ in
279 CMG(800, 30) and CMG(800, 90) are comparable to that in the single crystal [19] (see Fig. 3a),
280 κ_{el} does not contribute to the decrease of κ in our samples. On the other hand, we found the
281 sizable decrease in $\Delta\kappa$ compared with the single crystal's value (represented as the dotted lines).
282 Phonon and magnon can contribute to $\Delta\kappa$ in magnetic materials [64]. However, we assumed
283 the magnon contribution is negligibly small in CMG at room temperature because the
284 experimental observation of magnon contribution has been typically at very low temperatures
285 [65,66] and the magnetic damping constant of the polycrystalline CMG [67] is one order of
286 magnitude larger than that of CoFe alloys which show measurable magnon contribution at room
287 temperature [68]. Therefore, the thermal conductivity carried by phonons plays an important
288 role in the decrease of κ .

289 A plausible mechanism of the decrease of $\Delta\kappa$ is the increase of phonon-boundary
290 scattering caused by nano/microstructure [46-48]. To investigate the phonon thermal
291 conductivity κ_{ph} , we carried out a first-principles calculation, whose details are described in
292 Supplementary Information, with taking 3- and 4-phonon, and isotope scatterings into account
293 and obtained cumulative κ_{ph} , which provides a useful insight into the reduction of κ_{ph} by
294 nano/microstructures. Fig. 7a shows cumulative κ_{ph} as a function of the phonon mean free path
295 L for CMG at room temperature. Cumulative κ_{ph} rapidly increases from $L \sim 10 \text{ nm}$ and is
296 saturated to $\sim 23 \text{ W K}^{-1} \text{ m}^{-1}$ above $L > 1 \text{ } \mu\text{m}$. The saturation value is comparable to the value of
297 κ in the single crystal and much larger than that in our samples. Our calculation indicates that
298 phonons with L in the range from 10 nm to 100 nm mainly carry heat in CMG, and scattering
299 centers with the size of such the scale can efficiently reduce κ_{ph} . However, this length scale is
300 much smaller than the typical grain size with the order of 10 μm in both CMG(800, 30) and
301 CMG(800, 90) shown in the SEM images in Fig. 7b (showing the SEM images for all the
302 samples in Fig. S3). We ignored phonon-electron and phonon-magnon scatterings in the
303 calculation. They increase the phonon scattering and play an important role for quantitative
304 discussion on κ , but only make the length scale of the heat-carrying phonons shorter. Therefore,
305 even when phonon-electron and phonon-magnon scatterings are taken into account, the grains
306 of the order of 10 μm in size cannot be responsible for the decrease in $\Delta\kappa$ due to the phonon-
307 boundary scatterings. On the other hand, recall that the CMG samples contain the crystal phase
308 separation in the nanometer scale, as observed in Figs. 5a-c. The coincidence between L of the

309 heat-carrying phonons and the size of the crystal phase separation indicates that the crystal-
310 domain boundary induces phonon scatterings, resulting in the decrease of $\Delta\kappa$. Our results
311 suggest that phonon engineering using not only grain boundaries but also crystal-domain
312 boundaries can increase the performance of thermoelectric materials.

313 **4. Conclusion**

314 In summary, we investigated ANE at room temperature in polycrystalline CMG slabs
315 prepared by the SPS method in various sintering conditions. The maximum values of S_{ANE} and
316 α_{xy} of our polycrystalline CMG slabs prepared at a high sintering temperature and pressure are
317 comparable to those in the single-crystalline CMG slab and are largest at room temperature
318 among polycrystalline magnetic materials. Furthermore, the optimized CMG slab achieved the
319 record-high $z_{ANE}T$ value of 8×10^{-4} at room temperature, which is larger than that for the single-
320 crystalline CMG samples, owing to the decrease of κ . The transport measurements and
321 nano/microstructure analysis indicate that the degree of the crystalline order is important for
322 obtaining large S_{ANE} . Based on the calculation of the phonon transport spectrum and nanoscale
323 structure analysis, we suggest the importance of the crystal-domain boundary for increasing
324 phonon scatterings to decrease $\Delta\kappa$ and κ , which is a different strategy of the conventional
325 phonon engineering using grain boundaries to increase phonon scatterings. Our results
326 demonstrate that the integration of approaches used for development of the conventional
327 thermoelectric materials [69], e.g., phonon engineering, nano-structuring, and fabricating bulk
328 composite, will be also important to improve the performance of the magneto-thermoelectric
329 devices.

330 **Acknowledgement**

331 The authors thank M. Isomura and K. Suzuki for technical supports, and S. J. Park for
332 fruitful discussion. This work was supported by JST CREST “Creation of Innovative Core
333 Technologies for Nano-enabled Thermal Management” (JPMJCR17I1), JST ERATO
334 “Magnetic Thermal Management Materials” (JPMJER2201), JSPS KAKENHI Grant-in-Aid
335 for Early-Career Scientists (21K14519), JSPS KAKENHI Grant-in-Aid for Scientific Research
336 (S) (22H04965), NEC Corporation, and NIMS Joint Research Hub Program. The computations
337 in the present work were performed using the Numerical Materials Simulator at NIMS.

338 **Declaration of Competing Interests**

339 The authors declare that they have no known competing financial interests or personal
340 relationships that could have appeared to influence the work reported in this paper.

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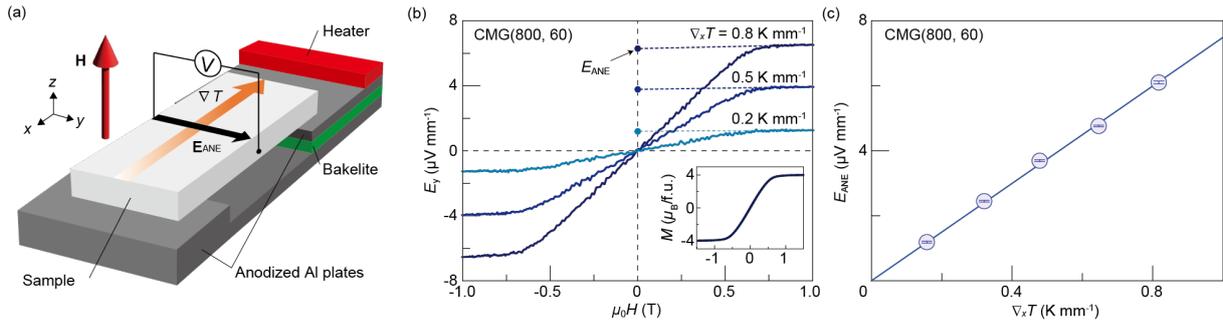
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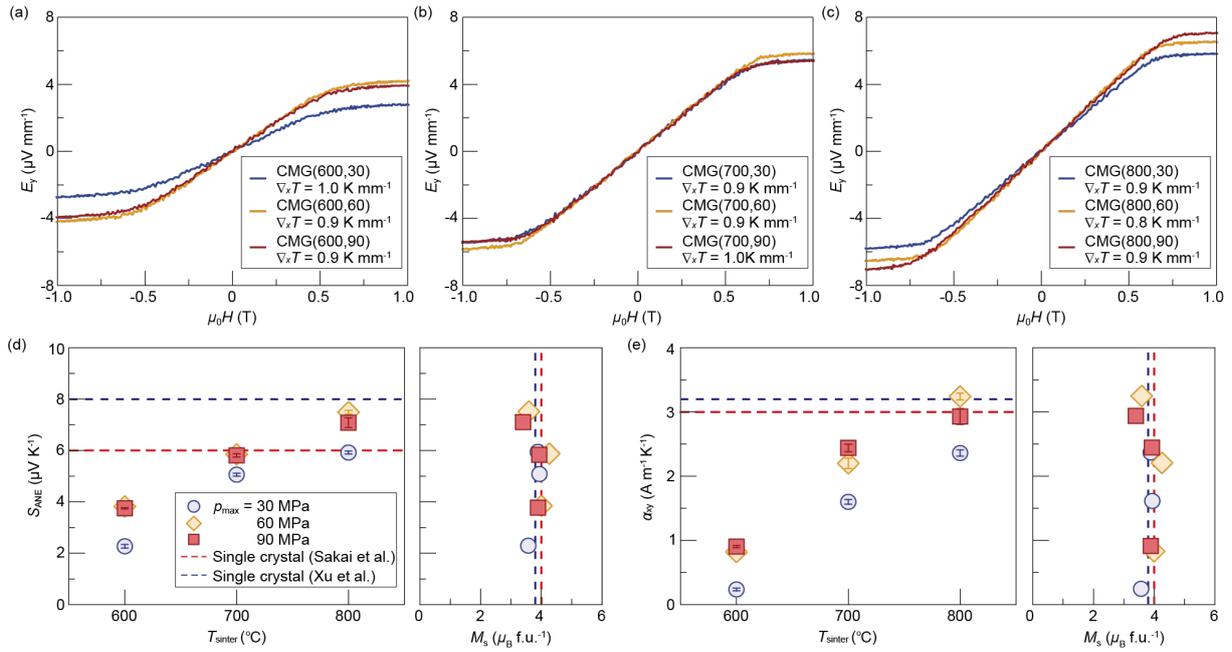
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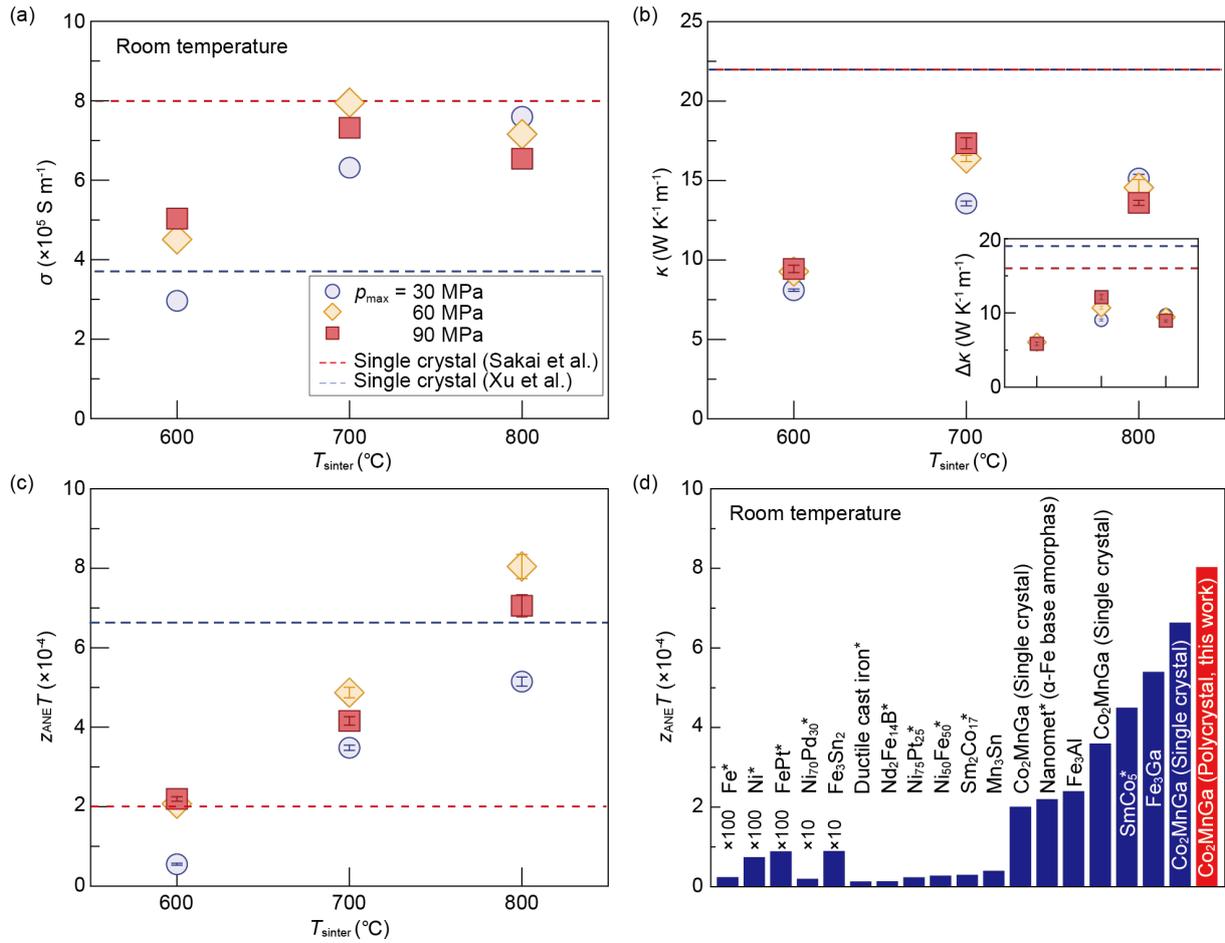
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Fig. 1 (a) Schematic illustration of the measurement setup. (b) H dependence of E_y in the CMG slab sintered at $T_{\text{sinter}} = 800^\circ\text{C}$ and $p_{\text{max}} = 60$ MPa, i.e., CMG(800, 60), for various values of $\nabla_x T$. The inset to (b) shows the M - H curve of CMG(800, 60). The colored dashed lines in (b) show the linear extrapolation with the data in the high H region, where M is saturated (see the M - H curve), for estimating E_{ANE} represented as the colored dots at $\mu_0 H = 0$. (c) $\nabla_x T$ dependence of E_{ANE} . The solid line in (c) shows the result of a linear fitting, of which the slope corresponds to S_{ANE} . The error bars represent the 68% confidence level (\pm s.d.).



539

540 **Fig. 2** (a-c) H dependence of E_y in the CMG slab sintered at $T_{\text{sinter}} = 600^\circ\text{C}$ (a), at $T_{\text{sinter}} = 700^\circ\text{C}$
 541 (b), and at $T_{\text{sinter}} = 800^\circ\text{C}$ (c). (d) T_{sinter} , p_{max} , and M_s dependences of S_{ANE} . (e) T_{sinter} , p_{max} , and
 542 M_s dependences of α_{xy} . The red and blue dashed lines in (d) and (e) correspond to the S_{ANE} , α_{xy} ,
 543 and M_s values obtained in the single-crystalline samples in Refs. 13 and 19, respectively. The
 544 error bars represent the 68% confidence level (\pm s.d.).



545

546 **Fig. 3** (a-c) T_{sinter} and p_{max} dependences of σ (a), κ (b), and $z_{\text{ANE}}T$ (c) at room temperature ($T =$

547 300 K). The inset to (b) shows the T_{sinter} and p_{max} dependences of $\Delta\kappa$. The red and blue dashed

548 lines in (a-c) correspond to the σ , κ , $\Delta\kappa$, and $z_{\text{ANE}}T$ values obtained in the single-crystalline

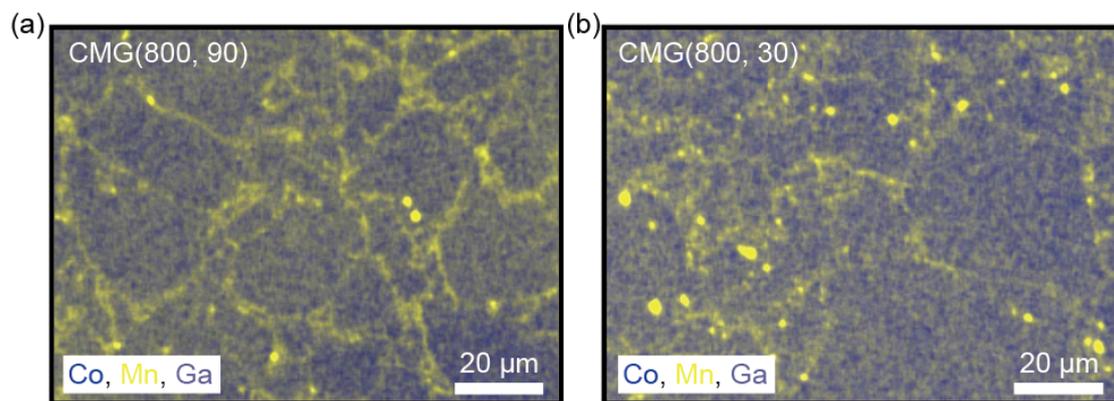
549 samples in Refs. 13 and 19, respectively. The error bars represent the 68% confidence level

550 (\pm s.d.). (d) Comparison of $z_{\text{ANE}}T$ between our polycrystalline CMG slab (red bar) and the

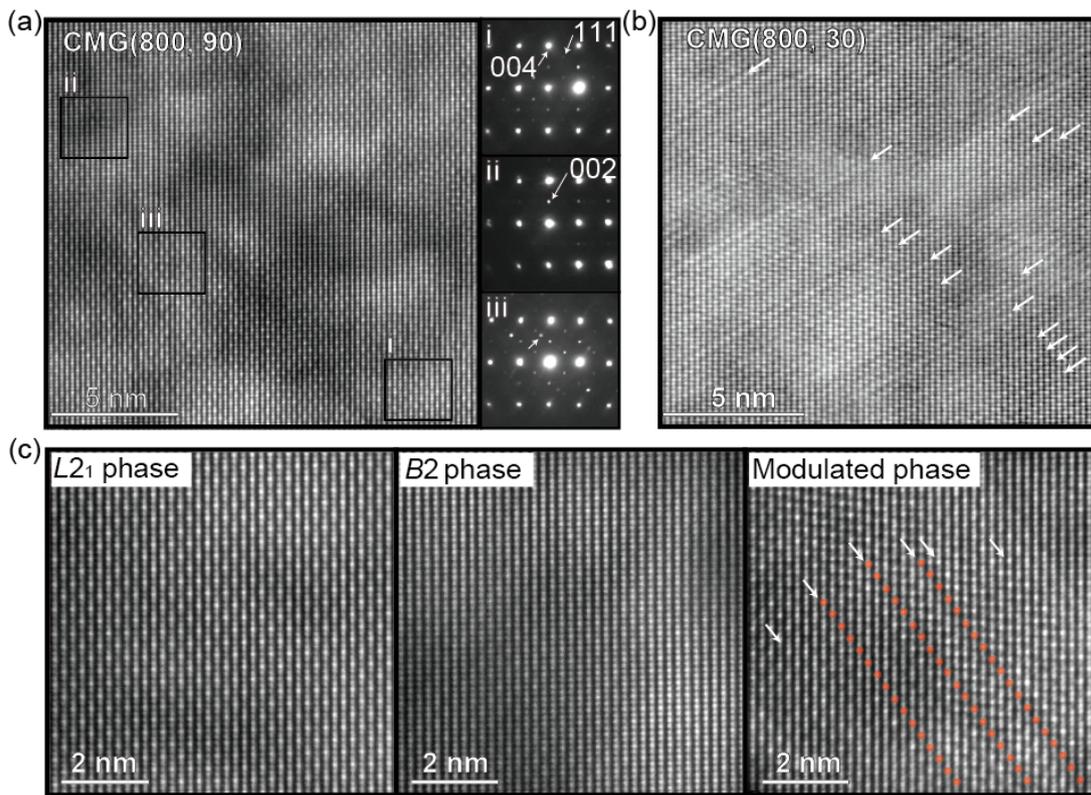
551 various bulk magnets (blue bars) around room temperature. $z_{\text{ANE}}T$ for the materials with an

552 asterisk are estimated using the experimental results of the anomalous Etingshausen effect and

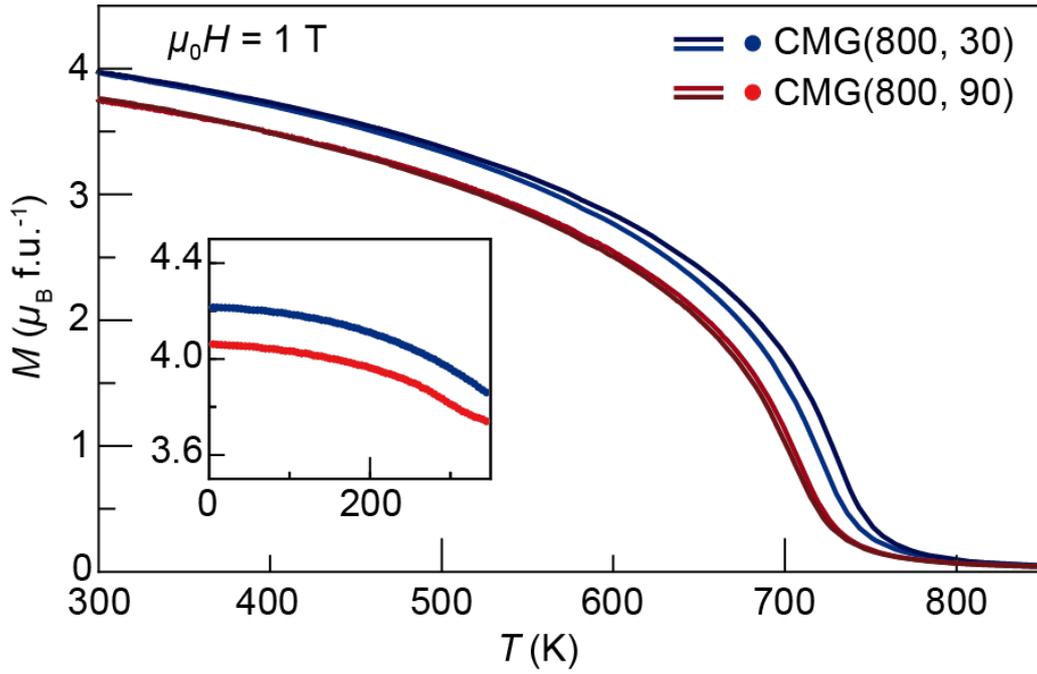
553 the Onsager reciprocal relation.



554 **Fig. 4** (a, b) SEM-EDS maps for CMG(800, 90) (a) and CMG(800, 30) (b).



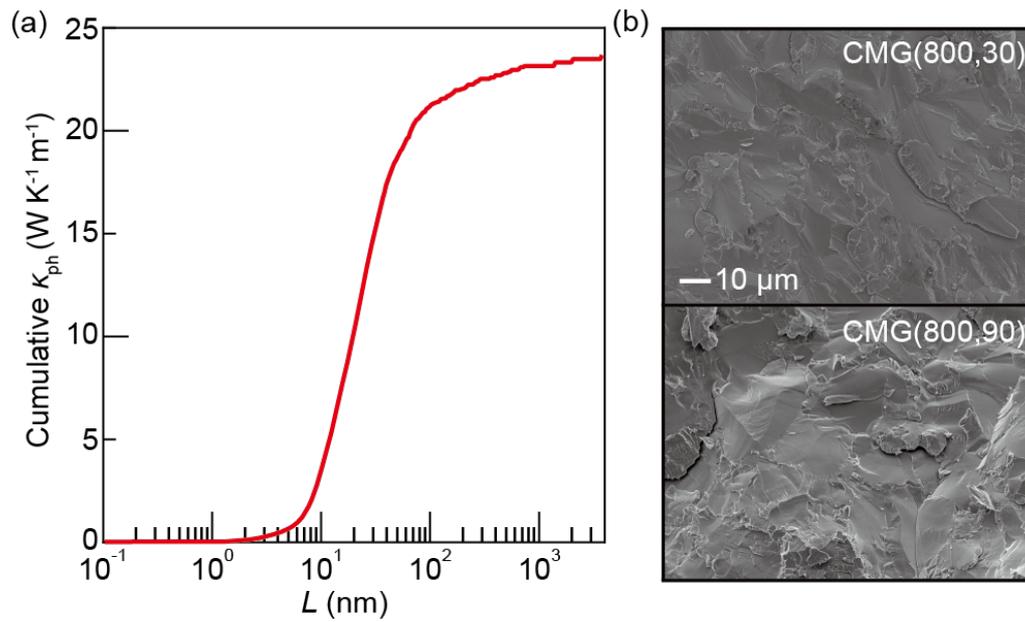
555 **Fig. 5** (a) High-resolution HAADF-STEM image obtained from CMG(800, 90) and electron-
 556 beam diffraction patterns obtained from the labelled regions. (b) High-resolution HAADF-
 557 STEM image from CMG(800, 30). (c) High-magnification HAADF-STEM images showing
 558 the $L2_1$, $B2$, and modulated phases.



559

560 **Fig. 6** T dependence of M for CMG(800, 30) and CMG(800, 90) at $\mu_0 H = 1$ T. The inset shows
 561 the averaged values of M in the T range from 5 K to 350 K.

562



563 **Fig. 7** (a) Calculation of cumulative κ_{ph} for CMG as a function of L at $T = 300$ K. (b) SEM
 564 images of the fracture surface of CMG(800, 30) and CMG(800, 90).