

## Supplementary material

### Tunnel magnetoresistive sensors with non-hysteretic resistance-magnetic field curves using noncollinear interlayer exchange coupling through RuFe spacers

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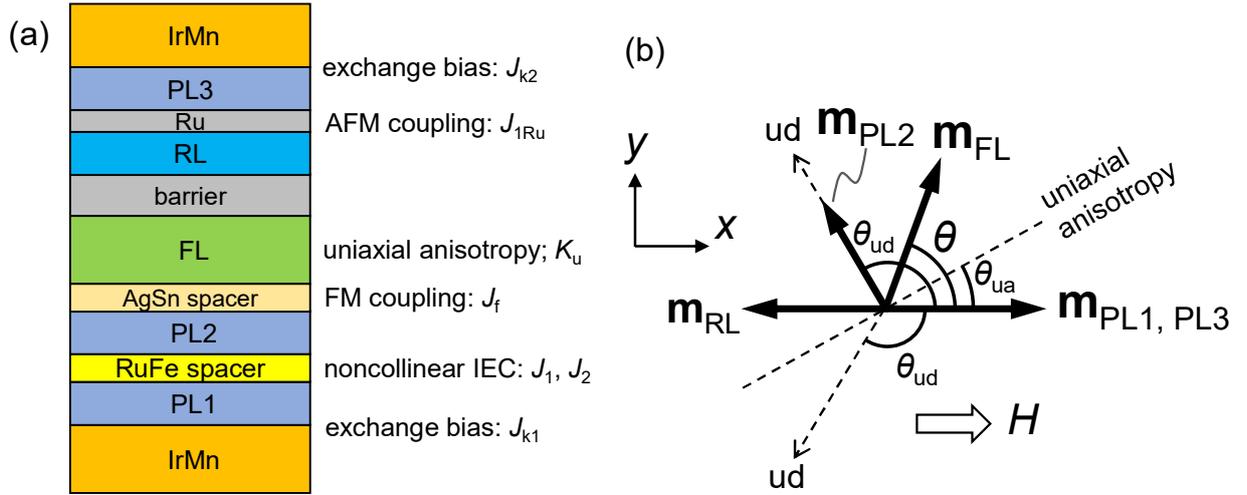
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#### 1. Calculation of $R$ - $H$ curve

The  $R$ - $H$  curves of the spin-valve structure shown in Fig. S1(a) were calculated by minimizing the total magnetic energy in the single magnetic domain regime, the Stoner-Wohlfarth model. Figure 1(b) shows the magnetization configuration under an external magnetic field,  $H$ , in the  $+x$  direction.  $\mathbf{m}_{xx}$  denotes the magnetization of each ferromagnetic (FM) layer.  $\mathbf{m}_{PL1}$  and  $\mathbf{m}_{PL3}$  are pinned in the  $+x$  direction, and  $\mathbf{m}_{RL}$  is pinned in the  $-x$  direction through the antiparallel IEC through the Ru spacer between RL and PL3.  $\mathbf{m}_{PL2}$  is pinned in either  $\pm\theta_{ud}$  titled direction from  $\mathbf{m}_{PL1}$  by the noncollinear IEC through the RuFe spacer. Then, FL receives a unidirectional magnetic anisotropy in the same direction as  $\mathbf{m}_{PL2}$  by the orange-peel FM coupling through the AgSn spacer. In addition, the FL has a uniaxial anisotropy in the  $\pm\theta_{ua}$  titled direction from  $\mathbf{m}_{PL1}$  which is induced by the annealing under a magnetic field. An external magnetic field  $H$  is applied in the  $\pm x$  direction.



**FIG. S1.** (a) Layer structure and the energy terms. (b) Configuration of the magnetizations ( $\mathbf{m}$ ) of the ferromagnetic layers.  $\theta_{ua}$  and  $\theta_{ud}$  are the angles between the easy axes of the uniaxial and unidirectional anisotropies, respectively, and  $\mathbf{m}_{PL1}$ .

We define  $M$  as the saturation magnetization,  $t$  as the layer thickness, and  $\theta$  as the angle between the magnetization and  $H$  for all the FM layers: PL1, PL2, FL, RL, PL3. We considered the following energy terms.

(1) Zeeman energy:

$$E_Z = -H(M_{PL1}t_{PL1} \cos \theta_{PL1} + M_{PL2}t_{PL2} \cos \theta_{PL2} + M_{FL}t_{FL} \cos \theta_{FL} + M_{RL}t_{RL} \cos \theta_{RL} + M_{PL3}t_{PL3} \cos \theta_{PL3}). \quad (S1)$$

(2) Exchange bias to PL1 and PL3:

$$E_{eb} = -J_{k1} \cos(\theta_{PL1}) - J_{k3} \cos(\theta_{PL3}), \quad (S2)$$

where  $J_{k1}$  and  $J_{k3}$  represent the exchange bias energies at the IrMn/PL1 and PL3/IrMn interfaces.

(3) Noncollinear IEC between PL1 and PL2 through the RuFe spacer:

$$E_{ncIEC} = -J_1 \cos(\theta_{PL2} - \theta_{PL1}) - J_2 \cos^2(\theta_{PL2} - \theta_{PL1}), \quad (S3)$$

where,  $J_1$  and  $J_2$  are the bilinear and biquadratic IEC energies, respectively.

(4) Orange-peel FM coupling between PL2 and FL through the AgSn spacer:

$$E_f = -J_f \cos(\theta_{FL} - \theta_{PL2}), \quad (S4)$$

where  $J_f$  is the bilinear IEC energy.

(5) Uniaxial anisotropy of FL:

$$E_{\text{ua}} = K_{\text{u}} t_{\text{FL}} \sin^2(\theta_{\text{FL}} - \theta_{\text{ua}}), \quad (\text{S5})$$

where,  $K_{\text{u}}$  is the anisotropy energy.

(6) Antiferromagnetic IEC between RL and PL3 through the Ru spacer:

$$E_{\text{RuIEC}} = -J_{1\text{Ru}} \cos(\theta_{\text{RL}} - \theta_{\text{PL3}}), \quad (\text{S6})$$

where,  $J_{1\text{Ru}}$  is the bilinear IEC energy.

For simplicity, we assume that the magnetizations of PL1, RL, and PL3 are pinned in the original directions under the applied  $H$ ; therefore,  $\theta_{\text{PL1}} = \theta_{\text{PL2}} = 0$ , and  $\theta_{\text{RL}} = \pi$ . Then, the total magnetic energy equation is simplified to

$$E_{\text{total}} = -H(M_{\text{PL1}} t_{\text{PL1}} - M_{\text{RL}} t_{\text{RL}} + M_{\text{PL3}} t_{\text{PL3}} + M_{\text{PL2}} t_{\text{PL2}} \cos \theta_{\text{PL2}} + M_{\text{FL}} t_{\text{FL}} \cos \theta_{\text{FL}}) + K_{\text{u}} t_{\text{FL}} \sin^2(\theta_{\text{FL}} - \theta_{\text{ua}}) - J_1 \cos \theta_{\text{PL2}} - J_2 \cos^2 \theta_{\text{PL2}} - J_f \cos(\theta_{\text{FL}} - \theta_{\text{PL2}}). \quad (\text{S7})$$

Based on the experimental data, we used the following values:  $M_{\text{FL}} t_{\text{FL}} = 49.5$  T nm,  $M_{\text{PL1}} t_{\text{PL1}} = M_{\text{PL2}} t_{\text{PL2}} = M_{\text{RL}} t_{\text{RL}} = M_{\text{PL3}} t_{\text{PL3}} = 6$  T nm ( $1$  T nm =  $7.95 \times 10^{-5}$  emu/cm<sup>2</sup>),  $J_f = 0.1$  mJ/m<sup>2</sup>, and  $K_{\text{u}} t_{\text{FL}} = 0.03$  mJ/m<sup>2</sup>, corresponding to an anisotropy field ( $H_k$ ) of 1.5 mT from the relationship of  $K_{\text{u}} t_{\text{FL}} = H_k M_{\text{FL}} t_{\text{FL}} / 2$ . For the noncollinear IEC through the RuFe spacer,  $J_1$  was varied, while  $J_2$  was fixed to  $-0.35$  mJ/m<sup>2</sup>. This  $J_2$  value is somewhat larger than the experimentally obtained values of about  $-0.3$  mJ/m<sup>2</sup> for the Ru<sub>100-x</sub>Fe<sub>x</sub> ( $x = 54-70$  at. %) spacers in the CIP-GMR films (Fig. 1). The choice of  $J_2 = -0.35$  mJ/m<sup>2</sup> for the simulations was because  $\mathbf{m}_{\text{RL}}$  is slightly rotated for  $-0.3$  mJ/m<sup>2</sup>, which complicates the interpretation of the results. Since the anisotropy field of the FL is determined only by  $J_f$ , the use of a larger value of  $J_2$  than that by the experiment does not significantly affect the simulation results.

Recalling that  $\theta_{\text{ud}}$  is the angle between the  $\mathbf{m}_{\text{PL1}}$  and  $\mathbf{m}_{\text{PL2}}$ , and the  $\mathbf{m}_{\text{PL1}}$  is pinned in the  $+x$  direction, we obtain  $\theta_{\text{ud}} = (\theta_{\text{PL2}} - \theta_{\text{PL1}})_{H=0} = (\theta_{\text{PL2}})_{H=0}$ . In addition,  $\theta_{\text{ud}}$  follows [1, 2]

$$\begin{aligned} \theta_{\text{ud}} &= 0 && \text{when } J_1/J_2 < -2, \\ \theta_{\text{ud}} &= \pi && \text{when } J_1/J_2 > 2, \end{aligned}$$

$$\theta_{ud} = \cos^{-1}(-J_1/2J_2) \quad \text{when } 2 \geq J_1/J_2 \geq -2. \quad (\text{S8})$$

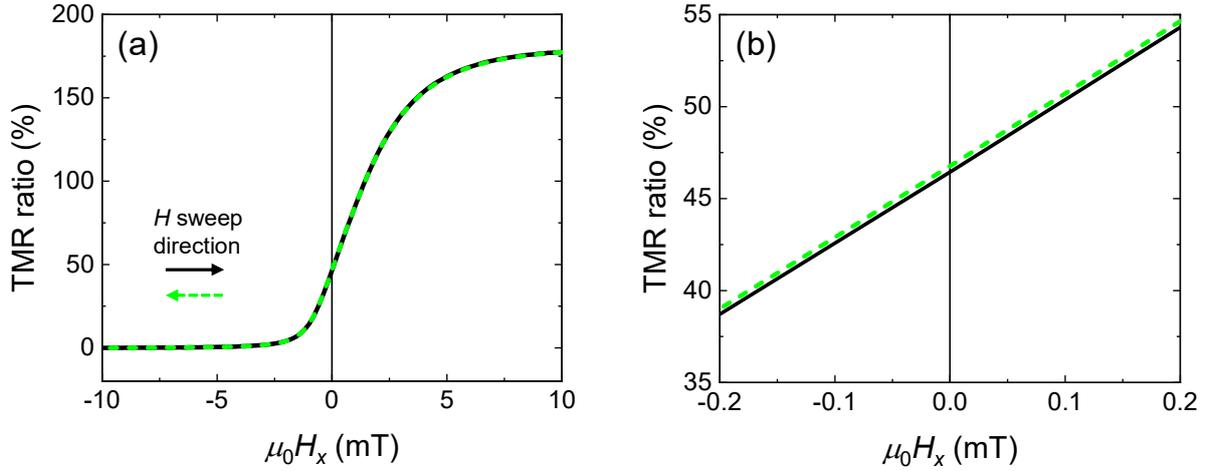
Therefore, for the calculations of the  $R$ - $H$  curve,  $\theta_{ud}$  was varied from 0 to  $\pi$  by changing  $J_1/J_2$  from  $-2$  to  $2$ .

By minimizing  $E_{\text{total}}$  in Eq. (S7), we obtained  $\theta_{\text{FL}}$  at different  $H$ . The  $R$ - $H$  curves were calculated by

$$R = 1 / \left[ \frac{G_{\text{max}} + G_{\text{min}}}{2} + \frac{G_{\text{max}} - G_{\text{min}}}{2} \cos(\theta_{\text{RL}} - \theta_{\text{FL}}) \right], \quad (\text{S9})$$

where,  $G_{\text{max}}$  and  $G_{\text{min}}$  are the maximum and minimum values of the tunnel conductance in the parallel and antiparallel magnetization state between  $\mathbf{m}_{\text{FL}}$  and  $\mathbf{m}_{\text{RL}}$ , respectively, and  $\theta_{\text{RL}} = \pi$ . In this paper, we used  $G_{\text{min}} = 1$  and  $G_{\text{max}} = 2.8$  (i.e., TMR ratio = 180%). The calculated  $R$ - $H$  curves for variations of  $\theta_{ud}$  and  $\theta_{ua}$  were numerically differentiated, and the sensitivity,  $\frac{dR}{dH} \frac{1}{R}$ , was calculated.

## 2. Supplementary data: Hysteresis of the TMR device shown in Fig. 4(b)



**FIG. S2.** (a) Full TMR curve of the device shown in Fig. 4(b) ( $\theta_{ud} \sim \pm 120^\circ$  and  $\theta_{ua} = 60^\circ$ ), showing negligible magnetic hysteresis. (b) The same curve zoomed in small  $H_x$  range.

## References

- [1] E.E. Fullerton and S.D. Bader, Phys. Rev. B **53**, 5112 (1996).
- [2] P.D. Kulkarni, T. Nakatani, T. Sasaki, and Y. Sakuraba, J. Appl. Phys. **129**, 213901 (2021).