

Ammonia Synthesis over Ruthenium Supported on Metastable Perovskite Oxyhydrides BaREO₂H (RE = Y, Sc) Prepared by Mechanochemical Method

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Oxyhydrides have attracted attention as materials with various unique properties derived from lattice hydride ions (H⁻). However, their instability makes synthesis by conventional thermal synthesis methods difficult, so an appropriate synthesis strategy is required. Here, the mechanochemical synthesis of perovskite oxyhydrides BaREO₂H (RE = Y, Sc) for catalyst applications is reported. The formation of BaYO₂H is known to be thermodynamically unstable; however, a mechanochemical process that inevitably proceeds under non-equilibrium conditions enables the synthesis of such a metastable oxyhydride material without any heat treatment. Furthermore, BaScO₂H, which is typically obtained at very high temperatures (1000 °C) and pressure (>4 GPa), is successfully synthesized at room temperature by the mechanochemical method. The ammonia synthesis reaction over these oxyhydrides supporting Ru is significantly enhanced at low temperatures, and the ammonia synthesis rates are significantly higher than conventional oxide-supported Ru catalysts. The mechanochemically synthesized BaREO₂H has many anionic electrons with low work function at the site of H⁻ vacancies, which enables strong electron donation to Ru and the storage of excess hydrogen adatoms from the Ru surface that results in high catalytic performance.

catalytic properties.^[1–4] These properties are mainly due to the unique coordination environment and the specific chemical and physical properties of H⁻, while O²⁻ is responsible for the construction and stabilization of the crystal framework. Oxyhydrides can be synthesized by H⁻ doping of typical oxides such as BaTiO_{3-x}H_x and LaH_{3-2x}O_x by exploiting the similar ionic radius of O²⁻ and H⁻ (135 pm).^[5–7] It is also possible to obtain novel compounds with unique chemical compositions, such as La₂LiHO₃ and A₃MO₄H (A = Rb, Cs; M = Mo, W), which allows for a wide variety of material designs.^[8,9] Although a number of oxyhydrides have been predicted by theoretical calculations, it is difficult to synthesize oxyhydrides by conventional high-temperature solid-state reactions because of the chemical and thermal instability of H⁻. On the other hand, it has been reported that high-pressure synthesis and topochemical reactions are effective for the synthesis of

oxyhydride materials.^[10] The most advantageous point of high-pressure synthesis is the capability to confine hydrogen in the solid phase by ultra-high external pressure (2–8 GPa), which allows hydrogen to react and remain as H⁻ even at high temperatures (800–1200 °C) if the sample is oxygen deficient. In some cases, crystal phases known as pressure-stabilized phases,

1. Introduction

Oxyhydrides, in which oxide ions (O²⁻) and hydride ions (H⁻) form an anion sublattice, are novel inorganic compounds that have attracted attention in the field of materials science due to their unique ionic conductivity, fluorescence properties, and

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which form only above critical pressure, are obtained under high-pressure conditions. Topochemical reactions are typically conducted at low temperatures (<600 °C) by the reaction of host oxide materials with hydride materials such as CaH₂ over a long time (>50 h). This technique limits cation diffusion at low temperatures so that the lattice O²⁻ ions can be replaced by H⁻ without changes in the crystal framework of the oxide.

However, some compounds have been reported to be impossible to synthesize by these methods, such as BaYO₂H. BaYO₂H has been predicted to be within 100 meV per atom from the convex hull based on a machine-learning model that assumes the formation of a tetragonal perovskite structure.^[11] Ba₂YO₃H with a K₂NiF₄-type structure has been produced by high-pressure synthesis (4 GPa)^[12]; however, the high-pressure synthesis of BaYO₂H has not been reported to date. It is also difficult to synthesize BaYO₂H by topochemical reaction due to the difficulty of producing the metastable Ba₂Y₂O₅ precursor as a pure phase without any impurities.^[13] It is important to overcome such metastability of oxyhydrides in developing new materials, which requires constructing a suitable synthesis strategy. Therefore, we have adopted mechanochemical methods in which chemical reactions are induced by mechanical energy under non-equilibrium conditions as an effective method for synthesizing oxyhydrides. The accumulation of strain energy generates a high-energy intermediate state in the material, whereby metastable phases with high Gibbs free energies can be formed.^[14] Mechanochemical methods have been conventionally used to synthesize metastable alloys and hydrides, and there have been some reports on the synthesis of multi-anionic hydrides in recent years.^[15,16] There have also been several reports on the synthesis of oxyhydrides such as BaTiO_{3-x}H_x, Sr₅(PO₄)₃H, and Sr₅(BO₃)₃H, which shows the significant potential of this method for the synthesis of metastable oxyhydrides.^[17-19]

Here, we report the mechanochemical synthesis of a metastable perovskite oxyhydride, BaYO₂H, and BaScO₂H, and their catalytic activity for NH₃ synthesis. Since the powder samples obtained by mechanochemical methods are expected to exhibit excellent catalytic activity and ionic conductivity at their surfaces and grain boundaries,^[20] revealing their functions at the interfaces is an important issue in evaluating the availability of the oxyhydrides obtained by mechanochemical methods. Most recently, the mechanochemical synthesis of perovskite oxyhydrides, including these two oxyhydrides, have been reported before our report.^[21] The paper reported a relationship between the feasibility of mechanochemical reactions and the calculated shear modulus of the starting reagents, while there is no application based on the interfacial or surface properties of these oxyhydrides. In the present work, the catalytic properties toward ammonia synthesis are examined for Ru catalysts supported on the synthesized BaREO₂H (RE = Y, Sc) and compared with those of Ru-loaded oxides with the same cation composition and other reported oxyhydride-based catalysts. In addition, the surface structure of Ru/BaREO₂H is investigated in detail to clarify the role of lattice H⁻ ions. In this catalyst system, hydride-deficient interfaces specifically generated by mechanochemical methods contribute to catalytic performance.

2. Results

2.1. Synthesis and Characterization of BaREO₂H

Figure 1a shows powder XRD patterns for the oxyhydrides after mechanochemical synthesis. The XRD patterns for the samples just after mechanochemical milling of a mixture of the precursors were simple due to the cubic perovskite structure, and no peak splitting or other peaks due to impurity phases were observed. The resultant materials were heated at 500 °C for 72 h under vacuum to improve the crystallinity for Rietveld analysis. The structural data for BaScO₂H obtained from ICSD (No.257866) were used to refine the XRD patterns, and in the case of BaYO₂H, the Sc symbol in this data was replaced by the Y symbol (Tables S1 and S2, Supporting Information). As shown in Figure 1b,c, the main peaks for both samples are well-fitted to BaREO₂H with a cubic perovskite structure (*Pm-3m*). There were no impurities in the BaYO₂H sample, while small impurity peaks were observed only for the BaScO₂H sample. The refined phase fractions for the BaScO₂H sample indicate that the perovskite phase contributes 98.5 wt.%, whereas the Sc₂O₃ phase remains at 1.5 wt.%. The refined lattice parameters for BaREO₂H are summarized in Table 1. The lattice constant for BaScO₂H (*a* = 4.1468(2) Å) is close to the reported value (*a* = 4.15034(3) Å) within an error of less than 0.1%.^[22] The volume of the unit cell for BaYO₂H is ≈1.14 times larger than that for BaScO₂H, which is close to the volume expansion rate (15.0%) observed in GdFeO₃-type orthorhombic perovskite LaREO₃ (RE = Sc, Y).^[23,24] BaREO_{3-δ} with the same crystal structure and cation composition as BaREO₂H was synthesized by the mechanochemical method using only oxide precursors (Figure S1, Supporting Information). The lattice constant for BaScO_{3-δ} (*a* = 4.132(2) Å) is similar to that reported for BaScO_{3-δ} (*a* = 4.13 Å) obtained by firing Ba₃Sc₂(OH)₁₂.^[25] The larger lattice constant for BaREO₂H than for BaREO_{3-δ} can be understood by the introduction of H⁻ into the lattice, i.e., H⁻ with the same ionic size as O²⁻ (135 pm)^[7] occupies the oxygen vacancy sites in oxygen-deficient cubic perovskite BaREO_{3-δ} to form BaREO₂H.

TDS measurements were conducted to determine the amount of H⁻ in the oxyhydrides. Two H₂ desorption peaks (*m/z* = 2) were observed in the TDS profiles for BaYO₂H (Figure 2a) ≈150 °C and above 300 °C. The sharp desorption peak ≈150 °C is attributed to the H₂ desorption from the surface, whereas the broad desorption peaks above 300 °C are the desorption of hydrogen from bulk since the diffusion of bulk H⁻ ion to the surface requires higher temperature. Signals with *m/z* = 18 were also observed below 400 °C, attributed to H₂O physically adsorbed on the sample holder and the sample's surface. However, the intensity of the H₂O signal was only ≈1/100 that of the H₂ signal. BaScO₂H showed desorption profiles similar to those for BaYO₂H (Figure 2b). These results suggest that hydrogen exists in similar environments in the crystals of both compounds.

Table 1. Refined lattice constants for BaREO₂H and BaREO_{3-δ}.

	BaYO ₂ H	BaYO _{3-δ}	BaScO ₂ H	BaScO _{3-δ}
<i>a</i> (Å)	4.3294(5)	4.2979(7)	4.1468(2)	4.132(2)

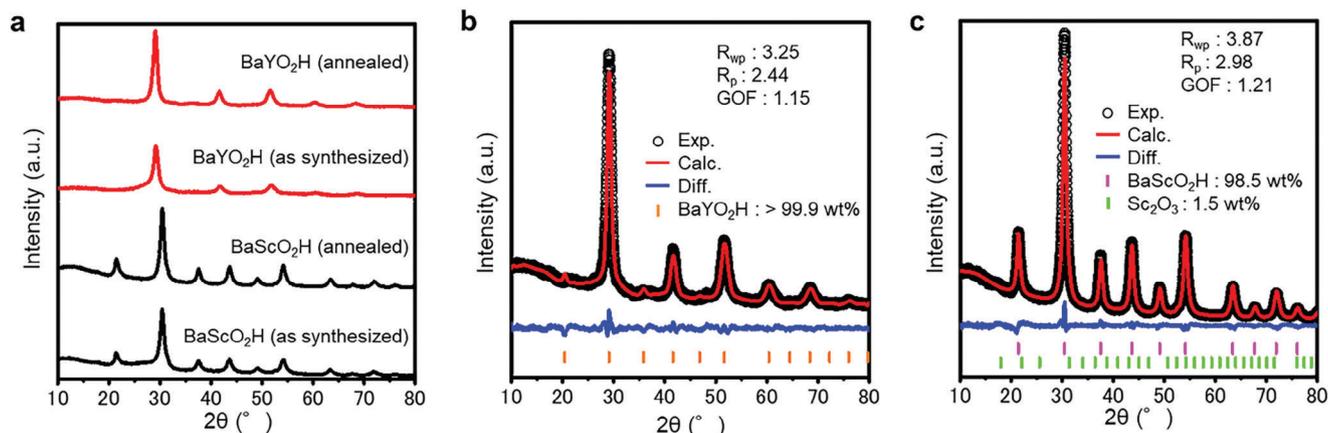


Figure 1. Crystal structure analysis of BaREO_2H . a) XRD patterns for BaREO_2H before and after heat treatment. Experimental XRD patterns and Rietveld refinement for b) BaYO_2H and c) BaScO_2H samples after heat treatment.

The amounts of H_2 released from BaYO_2H and BaScO_2H were 1.12 and 1.06 mmol g^{-1} , respectively. The chemical composition was estimated to be $\text{BaYO}_2\text{H}_{0.58}$ and $\text{BaScO}_2\text{H}_{0.46}$, which suggests that the obtained oxyhydrides contain significant amounts of H^- vacancies. When anion vacancies are formed, optical ab-

sorption of low-energy light should be observed, and the sample was gray in color (Figure S2, Supporting Information). The sample color is caused by the broad and weak absorption band $\approx 1.7\text{--}3.5$ eV (Figure S3, Supporting Information). This band is similar to the simulated optical absorption spectra of H-deficient models

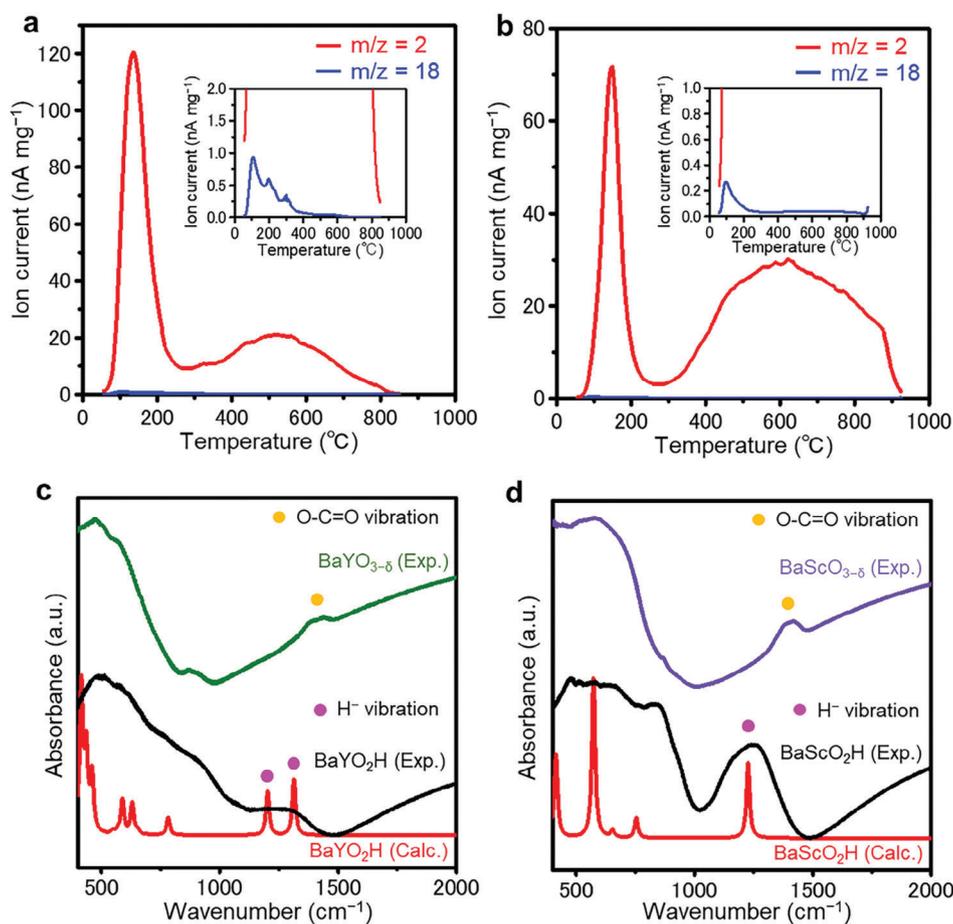


Figure 2. Detection and quantification of hydrogen incorporated in BaREO_2H . TDS spectra of a) BaYO_2H and b) BaScO_2H . c) FT-IR spectra of BaYO_2H and $\text{BaYO}_{3-\delta}$. d) FT-IR spectra of BaScO_2H and $\text{BaScO}_{3-\delta}$. Calculated spectra for BaREO_2H ($\text{RE} = \text{Y}$ or Sc) are shown for comparison.

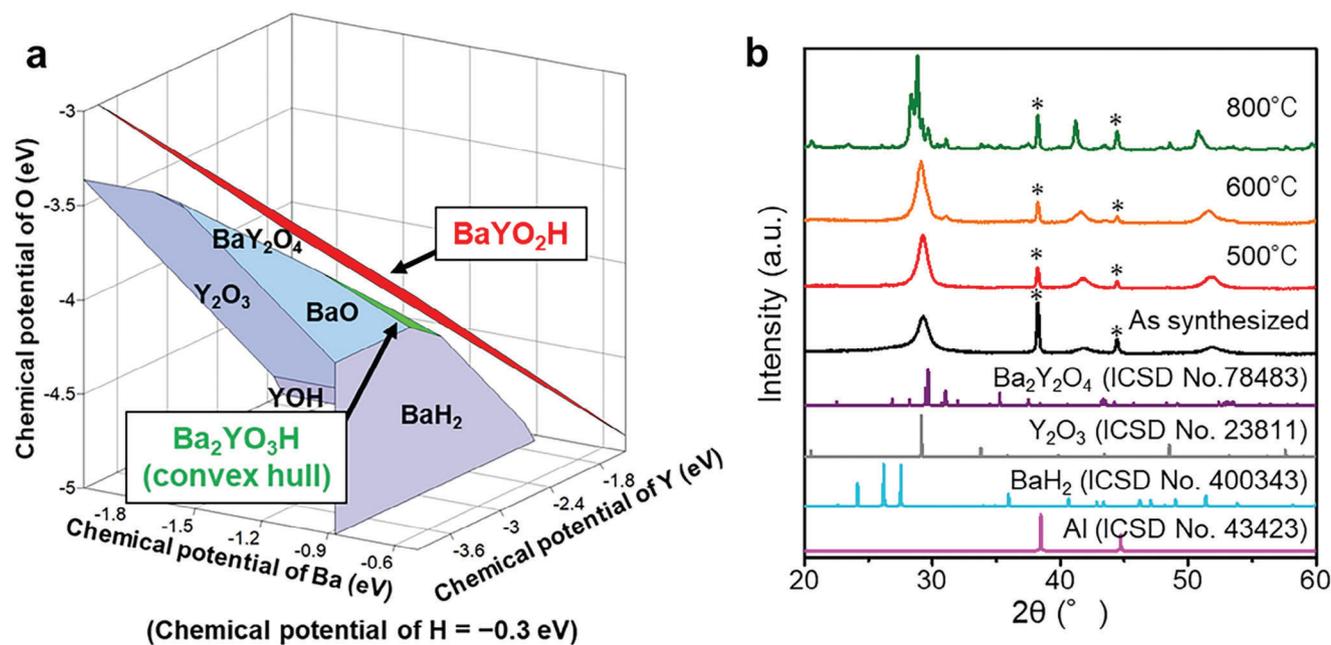


Figure 3. Investigation of the thermodynamic phase stability of BaYO_2H . a) Equilibrium phase diagram of the Ba–Y–O–H system at 0 K when the chemical potential of hydrogen is -0.3 eV. b) XRD patterns for BaYO_2H samples after heat treatment at various temperatures under an H_2 atmosphere. The sharp peaks $\approx 37^\circ$ and 45° marked by * are attributed to the Al sample holder.

calculated by DFT (Figure S4, Supporting Information). Moreover, it was predicted that the electrons are localized at the hydrogen vacancy sites, which gives rise to a mid-gap state in the bandgap (Figure S5, Supporting Information). These results clearly show the presence of electrons trapped at hydrogen vacancies in the synthesized BaREO_2H .

Figure 2c,d show FT-IR spectra for BaREO_2H and $\text{BaREO}_{3-\delta}$ measured in the $400\text{--}2000\text{ cm}^{-1}$ region. Based on a comparison with the computational spectra and phonon density of states (Figures S6 and S7, Supporting Information), the broad peaks observed $\approx 1250\text{ cm}^{-1}$ in the BaREO_2H spectra are attributed to the hydride vibration mode at the anion sites in the perovskite structure (Figure S8, Supporting Information). In contrast, no such vibration was observed in the $\text{BaREO}_{3-\delta}$ spectra, and only a vibration attributed to the carboxylate structure ($\text{O}=\text{C}=\text{O}$) $\approx 1400\text{ cm}^{-1}$ was observed.^[26] Therefore, H^- in the BaREO_2H samples occupies the same anion sites to form metal-hydrogen bonds.

The formation enthalpy (ΔE_f) and the equilibrium phase diagram for the Ba–Y–O–H system at 0 K were predicted from DFT calculations. The ΔE_f for BaYO_2H from BaO , BaH_2 , and Y_2O_3 was estimated to be $+13.0\text{ kJ mol}^{-1}$, which indicates that the formation of BaYO_2H is thermodynamically unstable. Moreover, BaYO_2H did not appear on the convex hull in any regions in the Ba–Y–O–H phase diagram, with the chemical potential of hydrogen as the projection axis (Figure S9, Supporting Information). Figure 3a shows the Ba–Y–O–H phase diagram, where the hyperplane corresponding to the stable region of BaYO_2H is clearly drawn. The hyperplane is discontinuous with the convex hull, which indicates that BaYO_2H is a metastable phase. When BaYO_2H is heated above 600°C , it is decomposed to form the raw materials and BaY_2O_4 , consistent with its thermodynamic instability (Figure 3b). For this reason,

BaYO_2H could not be synthesized by conventional thermal synthesis methods. On the other hand, $\text{Ba}_2\text{YO}_3\text{H}$ can be synthesized by the conventional thermal synthesis method under high-pressure conditions, as predicted from the equilibrium diagram (Figure 3a).^[12]

Sirota proposed that a thermodynamically unfavorable reaction can be allowed under a nanostructural excited state caused by strain energy accumulated by mechanical stress and the insertion of atoms into interstitial spaces.^[14] Quantitative studies on the accumulation of internal energy using shaker mills and planetary mills have already been performed, which have revealed that internal enthalpies accumulate $\approx 0.8\text{--}10\text{ kJ mol}^{-1}$ for Fe, Al, and AlRu alloys.^[27,28] Therefore, the high-energy milling performed in this study enabled the formation of a metastable phase, BaYO_2H , with a positive formation enthalpy. On the other hand, the kinetic effects are expected to be important in the formation of BaScO_2H from BaO , BaH_2 , and Sc_2O_3 because of its negative formation enthalpy (-26.9 kJ mol^{-1}). The mechanochemical method is expected to be effective toward the inhibition of hydrogen desorption at low temperatures because of the high local pressure caused by mechanical stress, similar to that of a high-pressure synthesis process.^[29] Therefore, it would be reasonable for BaScO_2H to form under mechanochemical conditions.

2.2. Catalytic Performance for Ammonia Synthesis

The results have clarified that BaREO_2H with many hydrogen defects easily releases hydrogen even at low temperatures below 200°C , which is similar to the reported highly active hydride-based ammonia synthesis catalysts.^[30–32] Therefore, the

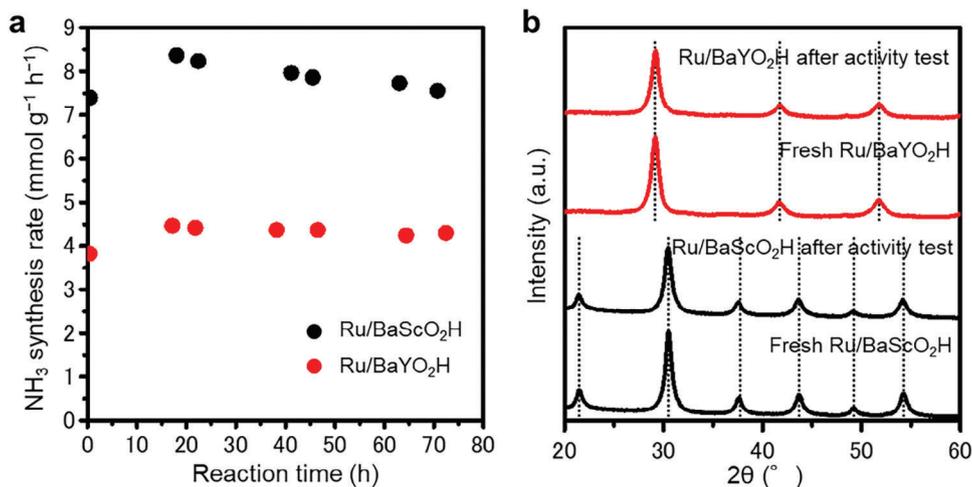


Figure 4. Catalytic stabilities of Ru-loaded BaREO₂H. a) Stability test for NH₃ synthesis over Ru-loaded BaREO₂H at 300 °C and 0.9 MPa. b) XRD patterns for Ru/BaREO₂H before and after ammonia synthesis reaction at 300 °C and 0.9 MPa for 70 h.

synthesized oxyhydrides were applied as catalyst supports of Ru for the ammonia synthesis reaction, and their catalytic properties were evaluated. All catalytic reactions were conducted in a fixed bed flow system as shown in Figure S10 (Supporting Information). The ammonia produced was trapped in an H₂SO₄ solution, and the amount of generated ammonia was quantified using ion chromatography with the calibration curve method (Figures S11, S12, and S13, Supporting Information). The Ru-loaded oxyhydrides worked as catalysts for ammonia synthesis for over 70 h without significant loss of activity (Figure 4a). The crystal structures of BaREO₂H remained unchanged after the reaction (Figure 4b), and of particular note, BaYO₂H exhibited high durability, despite being a metastable phase. XPS measurements were conducted to investigate the chemical stability of these catalysts during ammonia synthesis reactions. Figure S14 (Supporting Information) shows the wide-range XPS spectra of Ru/BaREO₂H before and after the catalytic reaction. All peaks are assignable to the constituent elements of the catalysts. After the catalytic reaction at 300 °C under 0.9 MPa for 24 h, the Ru 3d_{5/2} peaks for Ru/BaREO₂H shifted to a lower binding energy side than the zero-valent Ru peak (280 eV) observed on original Ru/BaREO₂H (Figure 5a,b). This result suggests that the strong Ru-BaREO₂H interaction occurs during ammonia synthesis, resulting in electron transfer from BaREO₂H to Ru. As shown in Figure 5c,d, both Sc 2p_{3/2} and Y 3d_{5/2} peaks shift to lower binding energy after the catalytic reaction, which may be due to the reduction of metal cation sites by replacing lattice O²⁻ with H⁻ ions or by forming hydrogen vacancy sites. Anyway, the catalyst surface was not oxidized during the reaction, and therefore, the Ru/BaREO₂H exhibited stable catalytic activity (Figure 4a).

Figure 6a shows the temperature dependence of the ammonia synthesis rate over various Ru catalysts at 0.9 MPa. The Ru-loaded oxyhydrides exhibited higher activity than the Ru-loaded oxides over the entire temperature range of 200–400 °C. Ru/BaScO₂H showed the highest catalytic performance among the Ru catalysts measured in this study (Table 2). Figure 6b summarizes the ammonia synthesis rates and apparent activation

energies for the various catalysts (Figures S15 and S16, Supporting Information). The activities of the Ru/BaREO₂H catalysts were superior to the conventional oxide-supported Ru catalysts with comparable or higher catalytic activities than those of other oxyhydride-based Ru catalysts such as Ru/BaAl₂O_{4-x}H_y.^[33] The apparent activation energies for Ru/BaREO₂H (49–67 kJ mol⁻¹) are clearly lower than those for conventional Ru catalysts (120 kJ mol⁻¹) and Ru/BaREO_{3-δ} (88–91 kJ mol⁻¹), and close to those for the electrone- and hydride-based catalysts (45–69 kJ mol⁻¹).^[31–33] These electrone and hydride supports have strong promoting effects that lower the energy barrier for ammonia synthesis on Ru; therefore, the results indicate that the BaREO₂H supports also have such promoting effects.

2.3. Analysis of Reaction Kinetics and Surface Electronic Properties

Kinetic analyses were conducted to obtain information on the reaction mechanism for ammonia synthesis. Table 3 summarizes the reaction orders with respect to N₂, H₂, and NH₃ (Figure S17, Supporting Information). The N₂ orders were close to +1 or higher for all the catalysts, which suggests that the rate-determining step is still the dissociation of N₂. In contrast, there was a significant difference in the H₂ orders between the oxide and oxyhydride supports; positive H₂ orders were obtained with Ru/BaREO₂H, whereas negative H₂ orders were obtained with Ru/BaREO_{3-δ}, as for conventional Ru catalysts. Conventional Ru catalysts exhibit negative H₂ orders because adsorption of dissociated H₂ prevents N₂ adsorption on the active sites on Ru at high H₂ pressure.^[34] Therefore, the positive H₂ orders for Ru/BaREO₂H indicate that these catalysts overcome such hydrogen poisoning. The NH₃ orders for Ru/BaREO₂H are largely more negative than Ru/BaREO_{3-δ}, which indicates that NH_x species derived from the reverse reaction are more densely present on Ru/BaREO₂H than on Ru/BaREO_{3-δ}. The accumulated NH_x species may prevent H₂ adsorption, which has an

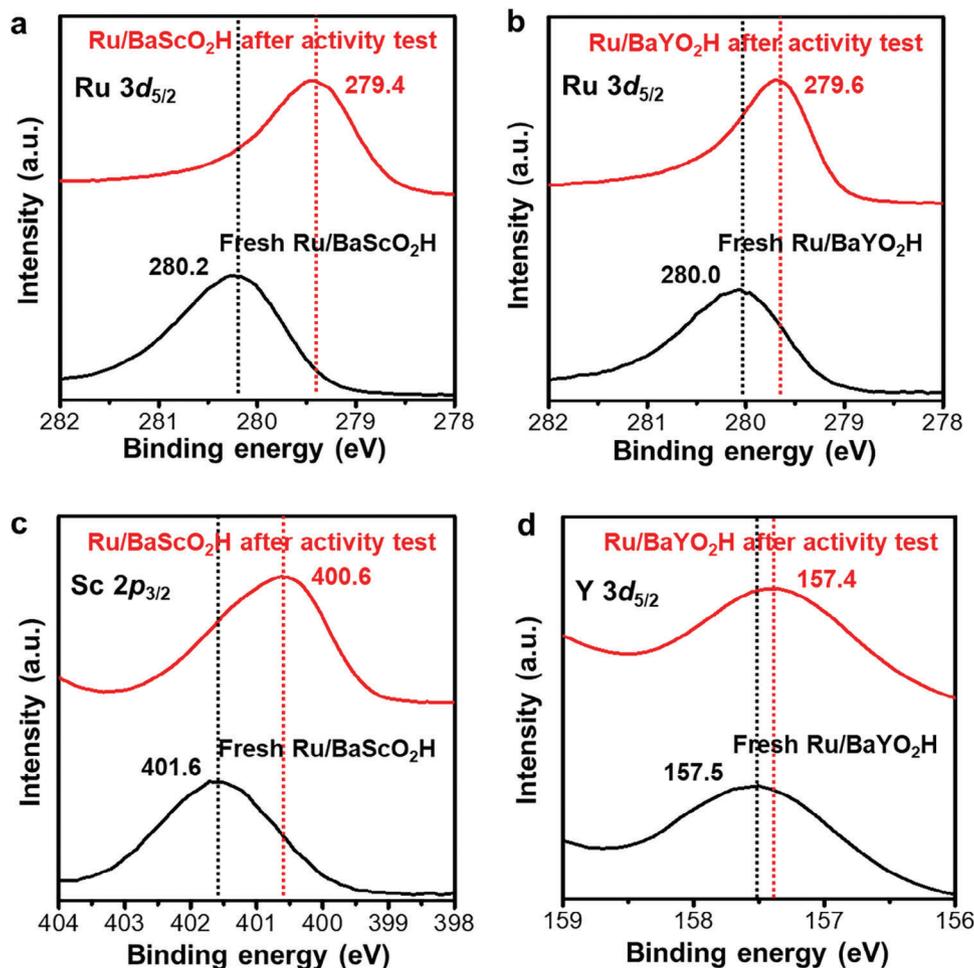


Figure 5. Chemical states of Ru/BaREO₂H surface before and after ammonia synthesis reaction. XPS spectra for Ru 3d_{5/2} of a) Ru/BaScO₂H and b) Ru/BaYO₂H. c) XPS spectra for Sc 2p_{3/2} of Ru/BaScO₂H. d) XPS spectra for Y 3d_{5/2} of Ru/BaYO₂H.

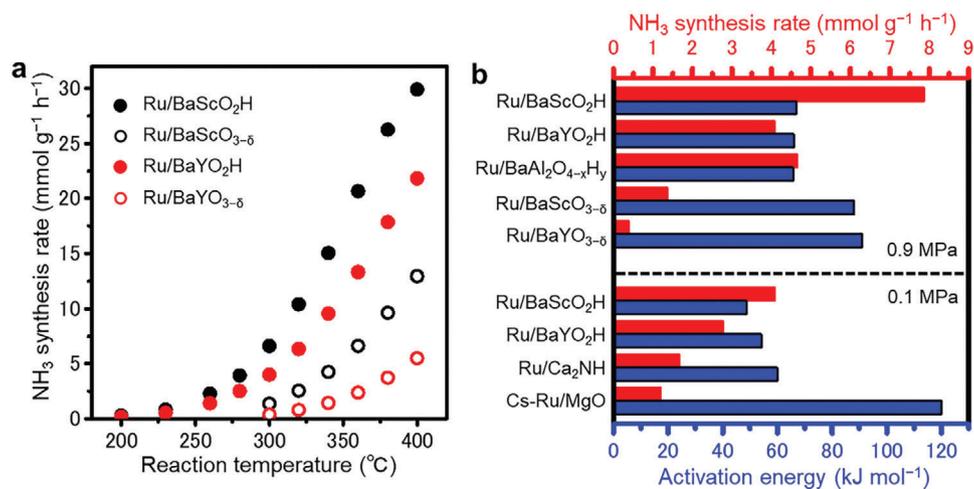


Figure 6. Comparison of catalytic activities. a) Temperature dependence of NH₃ synthesis activity for BaREO₂H and BaREO_{3-δ} with Ru metal at 0.9 MPa. b) NH₃ synthesis rates and apparent activation energies for various Ru catalysts at 300 °C and 0.1 MPa (lower part), and at 0.9 MPa (top part).

Table 2. Catalytic performance of various Ru catalysts measured in this work.

Catalyst	$S_{\text{BET}}^{\text{a)}$ [$\text{m}^2 \text{g}^{-1}$]	Ru loading ^{b)} [wt.%]	Pressure [MPa]	$r_{\text{NH}_3}^{\text{c)}$ [$\text{mmol g}^{-1} \text{h}^{-1}$]	$E_{\text{a}}^{\text{d)}$ [kJ mol^{-1}]
Ru/BaYO ₂ H	2.2	1.8	0.1	2.77	66.0
			0.9	4.35	54.2
Ru/BaScO ₂ H	4.4	1.7	0.1	4.09	66.8
			0.9	7.87	48.9
Ru/BaYO _{3-δ}	–	1.5	0.9	0.39	91.0
Ru/BaScO _{3-δ}	–	1.7	0.9	1.36	88.0

^{a)} Specific surface area of various support materials determined by BET analysis; ^{b)} Determined by XRF; ^{c)} Ammonia synthesis rate measured at 300 °C; ^{d)} Activation energy for ammonia synthesis was estimated from Arrhenius plots in the temperature range of 200–400 °C.

Table 3. Reaction order for various Ru catalysts measured at 0.9 MPa.

Catalyst	Temperature [°C]	N ₂ order (α)	H ₂ order (β)	NH ₃ order (γ)	Refs.
Ru/BaYO ₂ H	300	+1.20	+0.34	–1.20	This work
Ru/BaScO ₂ H	300	+1.05	+0.30	–0.83	This work
Ru/BaYO _{3-δ}	320	+1.08	–0.04	–0.32	This work
Ru/BaScO _{3-δ}	320	+1.47	–0.09	–0.42	This work
Ru/BaAl ₂ O _{4-x} H _y	340	+0.72	+1.02	–1.00	[33]

influence on the positive H₂ order.^[35] However, the H₂ orders for the oxyhydride-supported Ru catalysts cannot be simply explained by the NH₃ orders. For example, Ru/BaYO₂H with a larger negative NH₃ order shows a smaller H₂ order than Ru/BaAl₂O_{4- x} H_y catalysts. Accordingly, other factors would contribute to the positive H₂ orders for the Ru/BaREO₂H catalysts. Positive H₂ orders have been reported for electrone- and hydride-supported Ru catalysts,^[30–32] where reversible exchange between anionic electrons and H[–] occurs at the metal-support interface, which leads to a high tolerance toward H₂ poisoning. BaREO₂H has a large amount of H[–] vacancies so that H adatoms on the Ru surface can react with electrons at the anion vacancies to form H[–]. Subsequently, the regeneration of anion vacancies occurs when H[–] reacts with nitrogen adsorbed on the Ru surface or desorbs as H₂ from the support surface, and this cycle is expected to suppress hydrogen poisoning. Therefore, we tentatively consider

that the above mechanism suppresses hydrogen poisoning on Ru/BaREO₂H, which results in high ammonia synthesis rates, even at temperatures as low as 300 °C.

Furthermore, the superior catalytic activity of Ru/BaREO₂H can be explained by the electron-donating properties of the oxyhydride supports. Nitrogen bond dissociation has been reported to be promoted in electrone- and hydride-supported Ru catalysts by the enhancement of electron donation to the antibonding orbital of N₂ adsorbed on Ru, which is attributed to the charge transfer of loosely bound electrons at the support surface to Ru.^[30,32] Figure 7a shows the work functions (WFs) for the most stable surfaces of BaREO₂H and BaREO_{3- δ} (Table S3 and Figures S18, S19, S20, and S21, Supporting Information). The WFs for BaScO₂H and BaYO₂H for the most stable surface without anion vacancies predicted by DFT calculations are respectively 3.2 eV and 4.2 eV, which are similar to those for BaScO_{3- δ} and BaYO_{3- δ} . However,

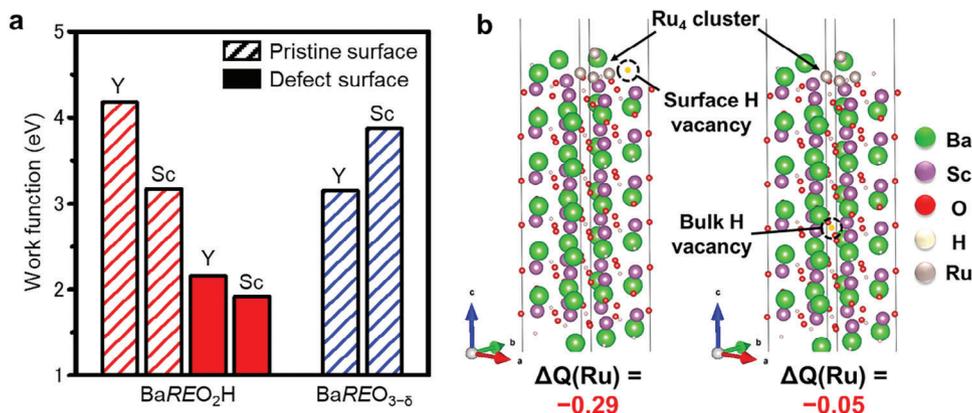


Figure 7. Surface electronic properties. a) WFs of BaREO₂H and BaREO_{3- δ} . b) The most stable geometrical configurations of Ru₄ cluster on BaScO₂H(100) surface with hydrogen vacancy with electrons on the surface (left) and the bulk (right). $\Delta Q(\text{Ru})$ represents the Bader charge on the Ru₄ cluster.

the WFs for BaScO₂H and BaYO₂H were significantly decreased by the formation of H vacancies on the top surface, and the lowest WFs were 1.9 and 2.2 eV, respectively. These values are comparable to that for C12A7:e⁻ (2.4 eV), which has been experimentally confirmed to exhibit high electron donation ability to Ru and N₂ on Ru.^[30,36] As additional information, the surface hydrogen vacancy formation energy ΔE_{VH} , at the most stable surfaces was 0.69–1.31 eV for BaScO₂H and 0.51–1.25 eV for BaYO₂H (Table S3, Supporting Information), which are close to the reported values for Ca₂NH and CaH₂ (0.88–1.11 eV) that are predicted to exhibit low WFs (2.3 eV) by the formation of H vacancies.^[32,37] These calculation results indicate that BaREO₂H exhibits high electron-donating properties due to easily formed H vacancies. TDS results also support the ease of hydrogen vacancy formation. The electron-donating ability of BaREO₂H to Ru was experimentally confirmed by the XPS measurements. As shown in Figure 5a,b, the Ru 3d_{5/2} peak of Ru/BaREO₂H after the catalytic reaction appears at a lower binding energy side than that of metallic Ru (280.0 eV).^[38] This is clear experimental evidence for the electron transfer from the oxyhydride support to Ru. In particular, the Ru 3d_{5/2} peak for Ru/BaScO₂H (279.4 eV) was located at a lower binding energy side than that for Ru/BaYO₂H (279.6 eV), meaning that BaScO₂H has higher electron donating ability than BaYO₂H. As shown in Table S4 (Supporting Information), there is no significant difference in the particle size of Ru between Ru/BaScO₂H and Ru/BaYO₂H, which indicates that the superior catalytic activity of Ru/BaScO₂H is not due to the dispersibility of Ru. Therefore, the efficient electron donation ability of BaScO₂H accounts for the superior catalytic activity of Ru/BaScO₂H than that of Ru/BaYO₂H. Additional DFT calculations were performed on the Ru-loaded model to investigate the electron-donating properties of BaScO₂H to Ru in detail (Figure S22, Supporting Information). Figure 7b shows the charge transfer between Ru cluster and BaScO₂H, which indicates that the electron donation from the surface hydrogen vacancy with electrons is more efficient than that from the bulk hydrogen vacancy. The ΔE_{VH} in the bulk models of BaScO₂H (1.50 eV) is much larger than the surface ΔE_{VH} , which means that the hydrogen vacancies are formed more easily on the surface than in the bulk. Therefore, the high electron-donating ability of BaScO₂H mainly originates from the surface hydrogen vacancies. Moreover, the amount of hydrogen vacancies in BaScO₂H is more than three times higher than that of BaAl₂O_{4-x}H_y (Table S4, Supporting Information). Given the similar Ru particle size between these two catalysts, their activity difference is attributed to the difference in the electron-donating ability between BaScO₂H and BaAl₂O_{4-x}H_y. We consider that these electron donation properties of BaREO₂H contribute to the promotion of N₂ cleavage over Ru, which reduces the activation barrier for ammonia synthesis (49–67 kJ mol⁻¹). From these results, the reaction mechanism of ammonia synthesis over Ru/BaREO₂H is illustrated in Figure 8. The BaREO₂H support has numerous hydrogen vacancy sites (Figure 2), among which the surface hydrogen vacancies mainly contribute to electron donation into Ru nanoparticles to form negatively charged Ru sites (Figure 5a,b, and Figure 7b). N₂ dissociation is facilitated on negatively charged Ru nanoparticles on BaREO₂H. The surface hydrogen vacancy sites can capture the hydrogen atoms on the Ru surface, preventing hydrogen poisoning on the Ru surface (Table 3). The surface lattice

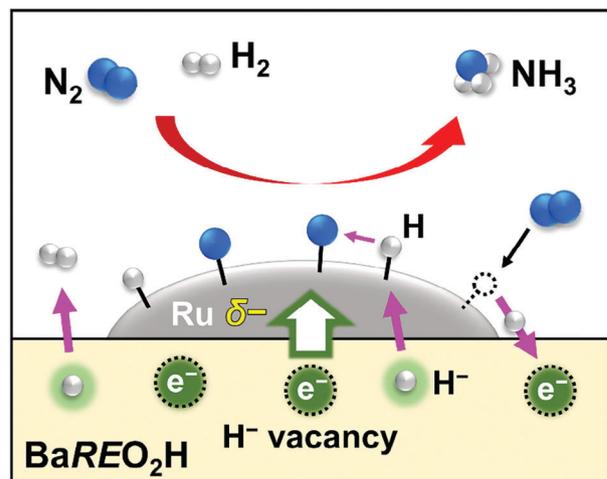


Figure 8. Schematic illustration of ammonia synthesis over Ru/BaREO₂H.

H⁻ ions react with nitrogen species on the Ru surface, and at the same time, hydrogen vacancy sites are regenerated at the Ru-support interface. Thus, the reversible exchange between anionic electrons and H⁻ takes place at the Ru-BaREO₂H support interface. As a result, nonstoichiometric BaREO_{2-x}H_x is preserved during ammonia synthesis as confirmed by TDS experiments (Figure S23, Supporting Information).

3. Conclusion

Mechanochemical synthesis of perovskite-type oxyhydrides BaYO₂H and BaScO₂H was successfully achieved. In particular, BaYO₂H, which is a metastable phase with a thermodynamically unstable crystal framework, could be synthesized only by the mechanochemical method. The synthesized oxyhydrides were used as supports for ammonia synthesis catalysts that exhibited high catalytic performance comparable to those of previously reported efficient support materials at low temperatures. The high catalytic performance is attributed to the inhibition of hydrogen poisoning at the active sites and the high electron-donating ability induced by H⁻ vacancies formed on the oxyhydrides. These results are expected to encourage further syntheses of metastable oxyhydrides and the development of promising catalyst supports for ammonia synthesis.

4. Experimental Section

Synthesis of Support Materials: BaO (99.99%, Sigma–Aldrich), BaH₂, Y₂O₃ (99.99%, Kojundo), and Sc₂O₃ (>99.9%, Kojundo) were used as starting materials for the synthesis of the BaREO₂H (RE = Y, Sc) oxyhydrides. BaH₂ was prepared by heating Ba metal (99.99%, Sigma–Aldrich) under an H₂ (>99.99%) atmosphere at 600 °C for 12 h. The mechanochemical synthesis was conducted with reference to a previously reported method for the synthesis of oxyhydrides.^[18,19] The starting materials (total weight: 2 g, BaO:BaH₂:RE₂O₃ = 1:1:1 molar ratio) were added to a 20 mL grinding bowl made of WC with ten balls (10 mm diameter) under an Ar atmosphere. Mechanochemical synthesis was then conducted using a planetary ball mill (Pulverisette 7 Premium Line, Fritsch) at a speed of 800 rpm for a total of 120 cycles (4 times 30 cycles). One cycle consisted of 2 min of milling and 3 min pauses to reduce the heating of the sample. After 30 cycles, the sample was removed from the grinding bowl and

crushed using an agate mortar. A yttrium-stabilized zirconia grinding bowl and balls were also available and when used, the number of reaction cycles was increased, typically to ≈ 240 –300 cycles at a speed of 850 rpm. To examine the crystal structure, the crystallinity of the milled sample was improved by annealing in an evacuated glass tube at 500 °C for 72 h. The synthesized compounds were highly air-sensitive; therefore, they were stored and handled in an Ar-filled glove box.

BaREO_{3- δ} oxides were also synthesized using the same procedure for the synthesis of BaREO₂H (total weight: 2 g, BaO:RE₂O₃ = 2:1 molar ratio). Mechanochemical synthesis was conducted at a speed of 850 rpm for a total of 90–150 cycles (3–5 times 30 cycles). An annealing process was also conducted using the same conditions as those for BaREO₂H.

Preparation of Catalysts and Catalytic Reaction: Ru₃(CO)₁₂ (99%, Sigma–Aldrich) was used as the Ru precursor for Ru/BaREO₂H and Ru/BaREO_{3- δ} . The amount of Ru was fixed at 2 wt.%, and Ru loading was conducted according to a previously reported method.^[32] The actual amount of Ru loaded on the support was determined by X-ray fluorescence spectroscopy (S8 TIGER, Bruker).

Ammonia synthesis was conducted in a stainless-steel reactor with the catalyst (0.1 g) under a flow of N₂ (purity >99.99995%, 15 mL min⁻¹) and H₂ (purity >99.99999%, 45 mL min⁻¹) with a H₂/N₂ flow ratio of 3 at 200–400 °C and 0.1–0.9 MPa. The ammonia produced was trapped in an H₂SO₄ solution, and the amount of NH₄⁺ ions generated in the solution was determined using ion chromatography (Prominence, Shimadzu) with a conductivity detector. The apparent activation energies were calculated from Arrhenius plots of the ammonia synthesis rates at various temperatures. Ammonia synthesis rates that were less than ca. 15% of the equilibrium conversion were used to evaluate the apparent activation energies.

Kinetic Analysis: The reaction orders of the catalysts were measured using a previously reported method.^[39] The reaction orders with respect to N₂ (α) and H₂ (β) were calculated from the gas partial pressure dependence on the ammonia synthesis rate at a constant flow rate of mixed gas of Ar, H₂, and N₂ (60 mL min⁻¹). The catalyst (0.1 g) was kept at 0.9 MPa and at a temperature where the outlet ammonia concentration was less than 10% of the equilibrium conversion. The ammonia synthesis rate (r) over various catalysts can be expressed by a power law equation using the partial pressures of nitrogen (P_{N_2}), hydrogen (P_{H_2}), and ammonia (P_{NH_3}):

$$r = k P_{N_2}^\alpha P_{H_2}^\beta P_{NH_3}^\gamma \quad (1)$$

where k is a rate constant, and α , β , γ are the reaction orders with respect to N₂, H₂, and NH₃, respectively. The reaction orders were calculated using Equations. (1–5):

$$r = \left(\frac{1}{W}\right) dy_0/d(1/q) \quad (2)$$

$$\log y_0 = \log\left(\frac{C}{q}\right)^{1/m} \quad (3)$$

$$r = \left(\frac{1}{W}\right) \left(\frac{C}{m}\right) y_0^{1-m} \quad (4)$$

$$C = k_2 P_{N_2}^\alpha P_{H_2}^\beta \quad (5)$$

where y_0 , W , q , $(1-m)$ and k_2 represent the mole fraction of outlet ammonia, the weight of the catalyst, the total flow rate, the NH₃ order (γ), and the rate constant respectively.

Characterization: The crystal structures of the oxyhydrides were identified using powder X-ray diffraction (XRD; MiniFlex600, Rigaku) with Cu K α radiation ($\lambda = 0.15418$ nm). The sample was sealed in an X-ray transmitting container to protect it from oxidation and hydration. Rietveld refinements were performed using the TOPAS (Bruker AXS, version 4.2) software. Hydrogen desorption from the support materials was detected using thermal desorption spectroscopy (TDS; TDS-1400TV, ESCO). Powder samples placed on a SiO₂ holder were heated to 1200 °C under vacuum conditions, and desorbed hydrogen ions ($m/z = 2$) and water ions

($m/z = 18$) were counted as an electronic current by a quadrupole mass spectrometer. The numbers of hydrogen molecules and water molecules were calculated based on the area of the desorption peak corrected using a silicon wafer containing implanted hydrogen. The Brunauer–Emmett–Teller (BET) specific surface area of the oxyhydrides was obtained from nitrogen adsorption isotherms measured at liquid-nitrogen temperature using an automatic gas adsorption instrument (BELSORP-mini II, MicrotracBEL). The vibrational spectra were recorded with a Fourier transform infrared spectrometer (FT-IR; Frontier DTGS, PerkinElmer). The samples were sealed in KBr plates to avoid oxygen and water contamination. Measurements were conducted between 4000 and 500 cm⁻¹ with a spectral resolution of 4 cm⁻¹. Optical diffuse reflectance spectra were measured at room temperature with an UV–vis spectrometer (UV–vis; U-4000, Hitachi). X-ray photoelectron spectroscopy (XPS; KRATOS ULTRA2, Shimadzu) was conducted using an apparatus equipped with a charge neutralization system. The binding energy of all spectra was calibrated with reference to the C 1s peak. All samples were delivered from the Ar-filled glovebox to the XPS analysis chamber through the vacuum transfer chamber to avoid oxidation and decomposition of the sample surface upon contact with air. The average particle size of Ru was determined by CO pulse chemisorption at 50 °C with a He flow of 30 mL min⁻¹ and 0.031 mL pulses of 9.51% CO in He using a catalyst analyzer (BELCAT-A, MicrotracBEL); spherical metal particles and a stoichiometry of Ru/CO = 1 were assumed.

DFT Calculations: Density functional theory (DFT) calculations were conducted using the Vienna Ab initio Simulation Package (VASP) code.^[40,41] The electron exchange and correlation were described using a Perdew–Burke–Ernzerhof type generalized gradient approximation.^[42] The 5s², 5p⁶, and 6s² electrons of Ba, 4s², 4p⁶, and 5s² electrons of Y, 3s², 3p⁶, and 4s² electrons of Sc, 2s² and 2p⁴ electrons of O, 1s¹ electron of H, and 4p⁶, 5s², and 4d⁶ electrons of Ru were handled as valence electrons. The core electrons were described using the projector augmented wave (PAW) method.^[43,44] A cutoff energy of 550 eV for BaYO₂H and 500 eV for BaScO₂H were used. $4 \times 4 \times 7$ k -point meshes were used for structural optimization of the bulk, while the Γ -point-only approach was applied for the slab. Electrostatic potentials applied for evaluation of the WF were calculated using $2 \times 3 \times 1$ k -point meshes for the optimized slab models. The convergence criteria for energy and force were respectively 1.0×10^{-5} eV and 1.0×10^{-2} eV \AA^{-1} for other than phonon calculations. For the phonon calculations, $7 \times 7 \times 15$ k -point meshes were used and convergence criteria of 1.0×10^{-6} eV and 1.0×10^{-4} eV \AA^{-1} were used for energy and force, respectively. To determine the stable anion arrangement of BaREO₂H with the lowest energy, 35 structures with different anion arrangements in a $2 \times 2 \times 1$ supercell based on a cubic unit cell were generated using the Supercell program and optimized.^[45] Stable structures of oxygen-deficient perovskite BaREO_{3- δ} were also determined by the same procedure as that for BaREO₂H. The composition of BaREO_{3- δ} was assumed to be BaREO_{2.5} to satisfy the charge neutrality. Phonon calculations were performed based on the finite displacement method, and the displaced structures were generated using the Phonopy module.^[46] IR spectra with fixed line widths of 16.5 cm⁻¹ were calculated using the Phonopy-Spectroscopy package.^[47] Slab models with non-polar and stoichiometric surfaces were generated by the tsubo.pl module with primitive cells of the structure with the most stable anion arrangement as the input.^[48,49] The slabs were constructed in 13 atomic layers, and a 20 \AA vacuum layer was introduced between the slabs to eliminate the interactions between the slabs. Surface energies were calculated for all optimized slab models and the most stable facets were determined as (111) for BaYO₂H, (100) for BaScO₂H, (010) for BaYO_{2.5}, and (111) for BaScO_{2.5}. The formation enthalpies for the BaREO₂H oxyhydrides ΔE_F , at 0 K were defined as $2E(\text{BaREO}_2\text{H}) - \{E(\text{BaO}) + E(\text{BaH}_2) + E(\text{RE}_2\text{O}_3)\}$, where E is the total energy per compositional formula. Structural information for various phases that contained the elements of Ba, Y, O, and H was obtained from the ICSD and Materials Project databases. The formation enthalpies for each element were calculated after optimization of all the structures, and the equilibrium phase diagram for the Ba–Y–O–H system was created using the Chesta program with the calculated enthalpies. The WF was defined as the difference between the Fermi energy for the slab models and the electrostatic potential in the vacuum gap of the slab model. We used a

Bader analysis of the charge density distributions for an atomic charge.^[50] All crystal structures for the bulk and slab models were visualized using the VESTA software package.^[51]

Supporting Information

Supporting Information is available from the Wiley Online Library or from the author.

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Conflict of Interest

The authors declare no conflict of interest.

Data Availability Statement

The data that support the findings of this study are available from the corresponding author upon reasonable request.

Keywords

ammonia synthesis, mechanochemical method, metastable oxyhydride, Ru-based catalyst

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