

# Microstructure and flexural strength of hafnium diboride via flash and conventional spark plasma sintering

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## Abstract

Microstructure evolution in bulk hafnium diboride ceramics prepared by spark plasma sintering in flash regime was compared with conventional spark plasma sintering. The conventional and flash spark plasma sintering resulted in ceramics with a high relative density exceeding 96 % of their theoretical density. A remarkably fine grain size distribution was noticed for the specimen prepared in the flash regime. This atypical microstructure evolution provides a possible insight into the mechanism of flash sintering for conductive bulks. The room temperature flexural strength of the hafnium diboride processed by flash SPS was 650 MPa which is 140 MPa higher than the sample produced by conventional SPS.

**Keywords:** hafnium diboride; flash sintering; flexural strength; high temperature materials.

## 1. Introduction

Due to the high melting point and low diffusivity, the consolidation of  $\text{HfB}_2$  requires the application of pressure [1–3], or the combination of pressure and a pulsed electrical current [4–6] with temperatures on the order of 2000 °C. Studies of the pressureless sintering of bulk

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diborides suggested that a vapor controlled mechanisms is dominant above 2000 °C, which leads to significant particle coarsening without any significant gain in density. Thus pressureless sintering of HfB<sub>2</sub> leads to the coarse grains of 15–22 μm [7].

Furthermore, the presence of surface oxides, such as B<sub>2</sub>O<sub>3</sub> and HfO<sub>2</sub>, inhibits densification [1,3,7,8]. Thus a promising approach for overcoming these obstacles is to use field assisted sintering techniques which allows: i) high-heating rates to minimize grain coarsening during heating and ii) electrochemical reduction/sublimation of the surface oxides.

From this point of view, a recent modification of the widely used spark-plasma sintering (SPS) method, flash SPS (FSPS), offers an opportunity to utilize heating rates higher than 1000 °C/min. Several ceramics, including SiC, B<sub>4</sub>C, and ZrB<sub>2</sub> with diameters up to 60 mm have been consolidated by the FSPS with a discharge time below one minute [9–12]. In this respect, the consolidation of metal-like conductive diborides offers a genuine opportunity for obtaining bulk ceramics, which are hard to consolidate by other methods [11].

For zirconium diboride [9], in particular, it was observed that consolidation during FSPS takes place within ~35 s, and such a short time might not be sufficient to complete the chemical reactions between the free carbon and oxygen-rich layer. The use of the extremely high heating rates of FSPS exceeding 10<sup>4</sup>/min might allow near instantaneous full densification of these materials. Apart from this, the very limited time exposure at high temperature might preserve the fine microstructure of the starting powders [11]. Because using the versatility of the FSPS process, large (i.e., ≥ Ø60 mm) bulk diboride ceramics can be consolidated using commercial powders. At present, the relationship between the processing times and properties is still not clear.

The objectives of this study are to obtain dense hafnium diboride ceramics using commercially available powders by FSPS and to gain insight into the consolidation details. In this study, dense HfB<sub>2</sub> monoliths were prepared by the FSPS method at 2000 °C and a 30-

1 second dwell using the as-received raw powder. The effect of the pre-consolidation  
2 conditions, and consolidation method (i.e., flash vs conventional SPS (CSPS)), on the  
3 microstructure development was investigated. Furthermore, the flexural strength of thus  
4 prepared bulks at ambient temperature and at 1600 °C was tested and analyzed.  
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## 10 11 **2. Experimental**

12 Commercially available HfB<sub>2</sub> (Grade O, Lot # T302510) with an average powder particle  
13 size between 1 and 3 μm (Japan New Metals Co. Ltd., Osaka, Japan) was used as the starting  
14 material. In this study, the initial HfB<sub>2</sub> powder was found to contain 1.1 to 1.6 wt% of  
15 oxygen. Other possible impurities, such as C (0.35 wt%) and N (up to 0.4 wt%) were within  
16 the specification provided by the manufacturer (O 0.8 wt.%, C 0.3 wt% and N 0.3 wt%). The  
17 total nitrogen, oxygen and carbon contents of the powders were measured again as these  
18 might have been affected by the storage conditions. The analyses were done using an ON-900  
19 and CS-800 (Eltra GmbH, Haan, Germany).  
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33 The as-received powders were subjected to homogenization in alcohol, followed by drying at  
34 about 100 °C. The resultant powders were screened through 60 and 400 mesh screens. The  
35 homogenized powder mixture was loaded into a graphite die with an inner diameter of 30  
36 mm and subjected to the SPS. The outer surface of the die was wrapped in 5-mm-thick  
37 graphite felt to homogenize the temperature distribution and reduce heat loss by radiation.  
38 The mold system containing the powder mixture was placed in an SPS furnace ('Dr. Sinter',  
39 SPS 1050, Sumitomo, Japan) [12,13]. A two-step consolidation process was used to produce  
40 the FSPS and CSPS specimens [9,13]. First, specimens with a diameter of 30 mm and heights  
41 of 5–6 mm were prepared by the preliminary SPS consolidation at 1600 °C. The samples  
42 were heated under vacuum to 1600 °C at 100 °C/min under the axial pressure of 60 MPa.  
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1 After a 20 min dwell at this intermediate step, samples for the FSPS were cooled to room  
2 temperature at the rate of 100 °C/min.  
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4 After cooling, the specimens were removed from the graphite die and subjected to a mold-  
5 free [9,10] FSPS consolidation. This step consisted of wrapping the pre-consolidated HfB<sub>2</sub>  
6 specimens with additional graphite foils and placed in a setup described in ref [13]. The  
7 Sumitomo unit was operated in the current control mode, thus a current limit of 3000 A was  
8 selected based on previous FSPS runs to reach the stationary temperature of 2000 °C.  
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10 The temperature during the FSPS experiments was determined by a side pyrometer focused  
11 on the side of the graphite felt using an emissivity of 0.90. Because the graphite felt is a  
12 thermal insulator, a tolerance for the accuracy of the temperature measurement was  
13 considered as ±50 °C. It was estimated that the sample temperature was at least 100 °C hotter  
14 than the probed one (*see section 3.1 on temperatures calibration*).  
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16 In the FSPS experiments, a constant uniaxial pressure of 20 MPa was applied. The apparatus  
17 was operated in the constant current control mode, thus preliminary studies allowed us to  
18 tune the voltage of the FSPS runs to approximately 6 V (**Fig. 1 (e)**). The power was switched  
19 off after the selected discharge time, and specimens were allowed to cool to room  
20 temperature under unchanged pressure conditions. The FSPS experiments were performed in  
21 argon gas at the flow rate of 2 L/min.  
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23 For reference, the samples were also sintered using a CSPS configuration. For these studies,  
24 SPS was continued after a preliminary consolidation step at 1600 °C. Thus, after the 20-min  
25 dwell at 1600 °C in a vacuum, the SPS chamber was backfilled with argon, and the pre-  
26 consolidated HfB<sub>2</sub> specimens were heated up to 2000 °C at the rate of 200 °C/min and then  
27 held for 5 min. The pressure of 60 MPa was maintained during the consolidation and cooling  
28 stages, as the application of lower pressures did not result in dense materials. Each specimen  
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1 was gradually cooled to 600 °C at the rate of 100 °C/min, then naturally to room temperature  
2 in the furnace. Argon gas at the flow rate of 2 L/min was used.  
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4 The sintered specimens were ground using diamond disks with a particle size of up to 0.5  
5 μm. The density of the samples was then measured by the Archimedes method using ethanol  
6 as the medium in accordance with ASTM B 963–08.  
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11 The three-point flexural strength was determined according Japanese Standard JIS R160  
12 using rectangular bars (2×2×20 mm) cut from the specimens with a diameter of 30 mm using  
13 an electric discharge machining. Their lateral surfaces were ground and polished using  
14 diamond pastes. The flexural strength tests were conducted at room temperature and at  
15 1600 °C in argon using a Shimadzu AG-X plus system (Shimadzu, Japan) [14]. The span of  
16 16 mm and loading speed of 0.5 mm/min were used. Ten bars were tested for each specimen  
17 at room temperature, and four specimens at 1600 °C. In addition, a single specimen was  
18 tested at 600 °C and 1200 °C in order to understand the temperature dependence of the  
19 flexural strength of the FSPSed specimen.  
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33 Microstructural observations and analyses were carried out on the fracture surfaces using a  
34 scanning electron microscope (SEM, SU 8000 cold-emission FE-SEM Hitachi). Observations  
35 were made on the fractured surfaces after the flexural tests.  
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### 43 **3. Results and discussion**

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45 In general, the *flash processes* are considered to have an electric discharge time of minute  
46 long [11], but application of pressure during the FSPS and its rapid nature often [12] does not  
47 allow producing a large ( $\varnothing > 20$  mm) crack-free specimen. The main reason for this cracking  
48 during cooling is that the pressing punches are cooler than the specimen's surface, thus after  
49 power is switched off, a temperature difference between the punches and specimen causes the  
50 cracks. Thus an additional dwell time was essential for producing crack-free specimens.  
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1 Mind, that the shrinkage curve in **Fig. 1 (e)** for the specimen #66F (here and afterwards the  
2 numbers denote the internal numerical system related to the SEM & strength measurements)  
3 serves as a direct indicator that the initial 60-sec long discharge results in an essentially fully  
4 dense specimen, but in order to minimize cracking during cooling, an additional 30 sec dwell  
5 was used.  
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### 11 *3.1 Temperature gradient during FSPS studies*

12 Debate over the temperature probing during the FSPS in particular, and for SPS, in general, is  
13 one of the current key problems for researchers. Few solutions have been proposed, such as  
14 probing the temperature from the top rather than from the side [9–11], but it is agreed that  
15 regardless of the temperature measurement method (i.e., by pyrometer or thermocouple) there  
16 is room for localized overheating during the spark plasma sintering. In the present study, the  
17 question for accuracy of the temperature measurement was addressed by preliminary FSPS  
18 runs using approximately 1-mm thick specimens.  $\text{HfB}_2$  has an eutectic reaction with carbon  
19 at approximately 2340 °C [15] or below 2400 °C [16]. These temperatures can be used as a  
20 marker for calibration, which is a common procedure when calibrating pyrometers. Thus,  
21 there is a possibility for the formation of a ceramic with the quasi-eutectic  $\text{HfB}_2\text{--C}$  structure  
22 in the case of the local overheating on the ‘graphite felt–specimen’ interface. Our previous  
23 studies of  $\text{B}_4\text{C--NbB}_2$  [17] showed that eutectic formation during SPS is accompanied with a  
24 rapid shrinkage. Thus, in order to understand the minimum allowed gradient during the FSPS  
25 experiments using the Sumitomo unit, we attempted to identify the temperature for the  
26 maximum shrinkage rate if the eutectic reaction between  $\text{HfB}_2$  and carbon is triggered. The  
27 results of these trial experiments are illustrated in **Fig. 2**.  
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55 For the specimen #100 presented in **Fig. (2 (a))**, the temperature at which a rapid shrinkage  
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1 increase in shrinkage was noticed. The general fracture and analysis of the polished surface  
2 suggested that (a) elongation of the HfB<sub>2</sub> grains was quite visible, and (b) the graphite phase  
3 percolates in the area between diboride grains. These are most likely to be a consequence of  
4 eutectic formation. In this case, the temperature difference between the previously reported  
5 temperature and probed in situ during the FSPS using a side pyrometer set-up was  
6 approximately 120 °C, which may be considered as a first approximation inaccuracy inherent  
7 to the temperature probing.  
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10 In addition, **Figure 2** (b) shows that the structure of the trial specimen using a 2000 °C FSPS  
11 run is free from elongated grains, but resulted in a crack-free specimen, thus it was suggested  
12 that the temperature of 2000 °C should be used for the HfB<sub>2</sub> consolidation. Because of the  
13 dimensions of the specimens obtained in the preliminary runs, the mechanical performance  
14 cannot be evaluated. Some large sized grains observed in **Fig. 2 (b)** can be viewed as a local  
15 overheating caused by contact with the upper punch of the SPS unit. In both presented cases,  
16 the current flow during the FSPS consolidation process was from left to right. The majority  
17 of grains in the middle of the specimen #88 cross-section was between 10 and 20 microns.  
18 Here, one should take into account that the temperature distribution while comparing 1-mm  
19 thick and 5-mm thick specimen is expected to be different and may be a good challenge for  
20 temperature simulation studies, and thus may lead to different grain sizes. Nevertheless, in  
21 order to deal with ‘overheated’ area in the present study, rather thick specimens were  
22 prepared for the FSPS runs, and eventually during preparation of the specimens for the  
23 flexural tests, this thin surface was polished off. Thus fracture surfaces subjected to the  
24 analysis represent the middle section of the FSPSed specimen.  
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### 56 *3.2 Effect of SPS processing mode on the microstructure*

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1 The fractional density of the hafnium diboride bulks prepared by FSPS and CSPS is (#66F)  
2 97.9% and (#61) 96.9%, respectively. The only crystalline phases were identified as HfB<sub>2</sub>  
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4 (PDF #38-1398).  
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7 Despite the similarity in the fractional density, a clear difference in the grain-size distribution  
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9 was observed between specimens consolidated using the different methods. The SEM  
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11 fractographs of the fractured surfaces shown in **Figs. 3** and **4** [2,3,6,18,19] illustrate the  
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13 difference in the final microstructure.  
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16 The FSPSed hafnium diboride possessed a clear bimodal grain size distribution, which is  
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18 macroscopically similar to that expected for the dual architecture composites [20], thus  
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20 making it in some sense dual architecture ‘monolith’. This type of structure can be considered  
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22 the initial stage of the grain-growth for some ceramics [21], as large grains occupied roughly  
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24 1/5 of the fracture surface. A previous study [22] predicted that the normal grain growth will  
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26 take place if the grain boundaries are isotropic, and the grain growth rate is linear with the  
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28 driving force. Hence, the data for the FSPS suggest that a non-linear correlation between the  
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30 grain growth and the capillary driving force (i.e., curvature between grains) may occur during  
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32 a dwell at high temperature, i.e., a stage where densification prevails over grain growth is  
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34 expected at the high-heating rate stage of the ‘flash’ consolidation process. It is assumed that  
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36 the final stage of consolidation usually associated with pore closure is not being affected by  
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38 the FSPS. Thus after the density exceeding 90 % is achieved, a conventional increase in the  
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40 grain size, (to a lesser extent) and in density will take place. Because the grain growth  
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42 process is quite sensitive to exposure to high temperatures, a bimodal grain size distribution  
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44 can be associated with a short made during FSPS (**Fig. 1 (e)**). Without a doubt, an additional  
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46 30 seconds of dwell during the FSPS may be sufficient time for the observed grain growth  
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48 (compare with **Fig. 2 (b)**, but mind different heating rates), but further experiments on this  
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50 subject are required. At first approximation, **Fig 2 (b)** indicates the possibility of local grain  
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1 growth at the upper SPS electrode–graphite felt–specimen interface. This may be attributed to  
2 the local *surface* overheating, and regarding specimen #66F, the initial thickness of the green  
3 specimen was much higher, and any anomalies observed can be considered to be caused by  
4 the local *bulk* overheating and thus associated with the current flow through the specimen.  
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9 Alternatively, for TiB<sub>2</sub> [8], the existence of a zone with finer/coarser grains was previously  
10 attributed to a strong reducing environment around the specimen created by the graphite  
11 crucible during hot-pressing. Because the graphite crucible was used only for the pre-  
12 consolidation stage in the case of the FSPS, the structure obtained during the flash stage  
13 cannot be fully attributed to the findings in Ref. [8].  
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17 Thus in order to understand the *bulk* effects in HfB<sub>2</sub> during the FSPS process, one should take  
18 into account that (a) a completely random distribution of ‘chains’ consisting of coarser  
19 grains, and (b) after the flexural test, we see the surface that is perpendicular to the current  
20 flow and to the pressure direction. Thus a process of a ‘flash’-type consolidation suggested in  
21 [23] is also possible. Namely, spark-like impulses that follow the string of conductive  
22 particles [24] are expected to be the main source for heating/densification for conductive  
23 powder materials. In this situation, a percolating network of large particles might also serve  
24 as an additional driving force for densification. It is thought that formation of the bimodal-  
25 type structure is mainly due to a short dwell at flash temperature, noting that pores were  
26 rarely observed after the FSPS.  
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45 Furthermore, as **Fig. 1 (c)** shows, after the preliminary consolidation, some grains had surface  
46 markings that resemble that after a surface diffusion or evaporation-based mechanism [21]. A  
47 preconsolidation step at 1600 °C did not result in a significant grain growth and densification  
48 (density bellow 60 % TD, 1–5 μm). In fact, the relative density of the as-received HfB<sub>2</sub> hot  
49 pressed at 2200 °C was only 85.8 % and the densification of HfB<sub>2</sub> by hot pressing started  
50 above 1650 °C [3]. This suggests that non-densifying mechanisms, such as vapor-  
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1 condensation, were active. This also agrees with findings of  $B_2O_3$  volatilization [3,7] in  
2 this temperature range. Because during the SPS (similar to hot pressing), the graphite mold  
3 may also serve as an additional source of C, CO or  $CO_2$  [8, 12], a vapor induced crystal  
4 growth observed in preconsolidated specimen, may result in an oxygen decrease, as  
5 preliminary results suggest that the oxygen level for bars after the flexural tests was  
6 0.34 wt.%, which is quite helpful in achieving high bulk density diborides [7]. Specifically, in  
7 order to be subjected to FSPS, the reconsolidated bulks are required to have a fairly good  
8 level of mechanical properties as the flexural strength of  $305 \pm 25$  MPa was measured for the  
9 reconsolidated specimen.  
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11 In the case of the CSPS runs, during a comparable 1-min dwell run at 2000 °C, the CSPS  
12 resulted in a density below 92 %, thus a much longer dwell time was required to achieve a  
13 density comparable to that for the FSPS. As result, after 5-min exposure at 2000 °C, the grain  
14 size of  $HfB_2$  was 10–18  $\mu m$  (**Fig. 4**). The majority of the pores was located within the grains,  
15 suggesting the domination of grain growth over densification. We also observed the presence  
16 of a secondary phase (undetectable by XRD) which is thought to have a nature similar to that  
17 previously observed for TaC [25], i.e., a non-stoichiometric carbide phase.  
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19 For the, lower limit of the grain size, i.e., 10  $\mu m$ , is close to the large grains for the FSPSed  
20 specimen. This also serves as an indirect indicator of the local *bulk* overheating [12] and  
21 grain growth during the FSPS process. Importantly, an analysis of the densification behavior  
22 of  $HfB_2$  in [3] suggests that in order to reach a high density, a dwell of 60 min is required at  
23 1900 °C, which suggests that a complex combination of mass transport processes is expected.  
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### 25 *3.3 Analysis of FSPS sintering kinetics using non-isothermal sintering approach*

26 The typical profile presented in **Fig. 1 (e)** was quite common within the specimens obtained  
27 in the present study, and one can easily divide it into three areas. For simplicity, these are  
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1 clearly indicated in **Fig. 5**, where the output of the Sumitomo unit represents the temperature  
2 dependence of shrinkage. Here one can see that the flash sintering during the FSPS is  
3 essentially finished by 2000 °C. At this temperature, a change in shrinkage is not observed.  
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5 At this point, the powder specimen has achieved full density (similar to #88 **Fig. 2 (b)**), but  
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7 an additional dwell was added to equilibrate the temperature distribution within the relatively  
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9 thick specimen to avoid cracking.  
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12 One can see that, in the high-temperature dwell zone, a slight change in shrinkage was  
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14 observed, which can be viewed as an activation of the initial stage for the grain growth.  
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16 Anyhow, the plot of the natural logarithm of the shrinkage rate as a function of the inverse  
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18 value of the absolute temperature (**Fig. 6**) provides additional information on this subject.  
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20 First, the flash sintering step is completed at around 1800 °C, where the shrinkage change  
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22 becomes insensitive to the temperature observed for the FSPSed specimen of HfB<sub>2</sub>.  
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24 Furthermore, based on an almost linear dependence of the shrinkage in **Fig. 7**, it can be  
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26 assumed that for the temperature range between 900 °C to 1800 °C, the FSPS process may be  
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28 controlled by a single mechanism (**Fig. 8**). It is noted that other FSPSed specimens of HfB<sub>2</sub>  
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30 produced with a similar heating profile without dwell (i.e. #88) also shared a linear  
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32 dependence of shrinkage up to ~1800 °C.  
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35 After the densification is completed, it is assumed that the plateau and the zone with an  
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37 inverse shrinkage dependence up to 2012 °C is due to the competition between the grain-  
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39 growth and densification presumably by vapor-controlled mechanisms. This is followed by a  
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41 rapid increase in shrinkage which is being associated with the uncontrolled temperature  
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43 increase, when the power for the SPS unit was intentionally turned off.  
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46 The activation energy for the densification based on the slope for this zone was estimated in  
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48 **Figs. 7 and 8**. The apparent activation energy ( $nQ$ ) based on the unaltered #66F data was  
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50 33±4 kJ/mol. Within a close approximation, the activation energy of the densification process  
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1 can be evaluated using  $n$  equal to 1, 1/2 and 1/3 for the viscous flow, volume or grain-  
2 boundary diffusion, respectively [26]. Although the model in [26] was developed for the  
3 conventional sintering, in the case of SPS and constant pressing conditions, the shrinkage  
4 data can be analyzed using the conventional (pressureless) sintering equations [27].  
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9 This yields an activation energy of 66 kJ/mol for the grain boundary diffusion and 99 kJ/mol  
10 for the volume diffusion. Nevertheless, because there is an uncertainty that is associated with  
11 the temperature measurements performed during the flash sintering experiments in general,  
12 and in the case of the FSPS, in particular, we attempted to evaluate the activation energies for  
13 the densification taking into account the possible overheating of 100 °C and 300 °C. These  
14 results are presented in **Fig. 8** and **Table 1** [28–33]. The  $nQ$  of 37 to 45 obtained from **Fig. 8**  
15 in the case of the local overheating provides an activation energy of 74 to 90 kJ/mol for the  
16 grain-boundary diffusion and 111 to 135 kJ/mol for volume diffusion.  
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19 A possible effect of pressure on the densification process during the FSPS can be addressed  
20 in further studies. Due to the findings in refs.[27] and [34], it was found that an increase in  
21 pressure will affect the consolidation process during the pressure assisted flash sintering. It  
22 was summarized in [34] that an applied uniaxial stress during sinter-forging also affects the  
23 threshold temperature for the flash sintering. As the stress is increased, the temperature for  
24 the onset of flash sintering is reduced. In another study [27], it was reported that application  
25 of pressure-assisted and conventional sintering analysis for the spark plasma sintering of  
26 zirconia will yield identical activation energies when the process is being controlled by a  
27 single mechanism of grain-boundary diffusion.  
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32 Based on the data presented in **Table 1**, one should highlight that in the case of the high-  
33 pressure hot pressing of  $\text{HfB}_2$ , the activation energy of 96 kJ/mol was reported [29]. Other  
34 data for  $\text{ZrB}_2$  and  $\text{TiB}_2$  collected by different methods yielded an activation energy higher  
35 than 400 kJ/mol. Thus in ref. [32], for  $\text{TiB}_2$ , it was argued that such a high activation energy  
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1 may be associated with diffusion of the metal into the metal diboride lattice (like in [19] for  
2 TaB<sub>2</sub>), since the activation energies for the diffusion of B into TiB or TiB<sub>2</sub> are reported to be  
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4 ~190 kJ/mol [33]. Here one should point that heating rate may influence a number of  
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6 mechanisms simultaneously contributing to densification, but the rule of thumb for SPS is  
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8 that high heating rate allow one to avoid surface diffusion induced coarsening [35].  
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11 Compared with the values estimated from **Fig. 8** with that previously reported for transition  
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13 metal diborides, one can assume both stages to be controlled by the bulk diffusion of boron in  
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15 the diboride, which becomes especially clear taking into account possible overheating at the  
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17 interface between the specimen and the graphite felt.  
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21 In general, the situation observed during consolidation at elevated temperatures can be  
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23 illustrated in **Fig. 9**. The area where the majority of the flash experiments on non-oxide  
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25 ceramics is located on the left side of **(a)**. It is expected that the activation energy of the  
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27 coarsening process has the lowest activation energy, while the activation energy for the grain  
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29 growth via bulk diffusion is the highest one. This is true for the majority of metals and  
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31 ceramics, but in the latter case, it is possible that anions of the metal and non-metal will have  
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33 a different activation energy and the preexponential factor [36], similar to the finding listed in  
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### 36 **Table 1.**

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38 This implies that even in the case of the dominant consolidation mechanism, the  
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40 identification process of the main diffusion mechanism and diffusing species can be  
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42 complicated. Two or more mechanisms usually contribute to consolidation at the same time,  
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44 which significantly complicates analysis, because it is well known that porous ceramics  
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46 require higher temperatures than the bulk one. Thus the development of the bimodal structure  
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48 observed for the FSPSed HfB<sub>2</sub> becomes possible if one reaches temperatures in the window  
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50 of opportunity identified in **Fig. 9**. In this range even a small (e.g., 1 °C or 100 °C) thermal  
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52 gradient can cause a local increase in the grain growth rate (**Fig. 9 (b)**), given that a sufficient  
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1 driving force is available in the consolidated specimen. Furthermore, the inability to 'freeze'  
2 the consolidation immediately at a specified point adds more uncertainty to the subject of the  
3 grain growth process.  
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6 Thus it can be emphasized that analysis of the shrinkage kinetics for the presented hafnium  
7 diboride is a preliminary attempt to understand the consolidation mechanism for the flash  
8 spark plasma sintering. We should point out that a radial expansion during FSPS was  
9 minimized to 100  $\mu\text{m}$ , while the displacement measured by SPS was in the axial direction (up  
10 to 2 mm after cooling, when green specimens were  $\sim 6\text{mm}$  thick). This may contribute to an  
11 error during evaluation of the activation energy using specimens axial shrinkage rate. Other  
12 aspects of this process associated with grain growth, or the effect of pressure, electrical field,  
13 and the *effect of the heating rate* on the FSPS process are expected to be analyzed in a  
14 separate study. In the absence of available experimental data for other diborides via FSPS or  
15 CSPS, these aspects remain unanswered.  
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### 31 *3.4 Flexural strength performance of bulk hafnium diboride prepared using FSPS and CSPS*

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33 At room temperature, the flexural strength of the FSPSed specimen was higher than that  
34 produced by CSPS, i.e.  $650\pm 45$  MPa and  $512\pm 35$  MPa, respectively. At room temperature,  
35 the bimodal structure of  $\text{HfB}_2$  resulted in a higher flexure strength and had a difference in the  
36 loading–stress curves (see **Fig. 2 (g)** and **Fig 10**), which hints that the finer and coarser grains  
37 fracture in multiply stages similar to the matrix-fiber composites [37]. Such a loading curve  
38 was observed for 4 out of 10 specimens and their flexural strength was above 640 MPa. In  
39 the case when a typical linear fracture was observed, the strength was within  $623\pm 31$  MPa. A  
40 slightly lower value in the case of the CSPS specimen can be explained by the Hall-Petch-  
41 like relation (see **Fig. 3 (e)** [2,3,6,18,19]).  
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A closer examination of the macroscopic fracture surface of the bars (**Fig. 10**) showed that a different distribution of the large-sized grains (highlighted by red color) could explain the strange behavior of the FSPSed specimens during flexure. Specimens with a linear loading–stress curve had a different distribution of the large-sized grains. Specimens with a linear behavior of the loading–stress curves fractured in blocks (highlighted in **Fig. 10 (b)**). During fracture in these specimens (**Fig. 10 (b)**) the grains with a size of 10–18  $\mu\text{m}$  were not isolated from each other as for the specimen presented in (**Fig. 2 (a)**) or (**Fig 10 (a)**). Thus it is assumed that the work of fracture increases if the large-sized  $\text{HfB}_2$  grains participate in the fracture of the material, i.e., the fine-grained  $\text{HfB}_2$  ‘matrix’ does not fracture before the large-sized  $\text{HfB}_2$  grains contribute to the macroscopic fracture. In both cases, the large-sized grains act as a reinforcement phase and fracture trans-granularly. The high values of the strength for these ceramics are likely caused by the grain refinement (see **Fig. 3 (c)**). Because of the lack of information on the fracture of ceramics with this unusual grain size distribution, and because the flexure bars were prepared from a single specimen, it is possible that the different grain size distribution may represent different stages of the grain growth / densification during FSPS.

Furthermore, it is clear that work to fracture for the FSPSed  $\text{HfB}_2$  was slightly higher at room temperature (0.62 vs 0.35  $\text{J/m}^2$ , for the FSPS and CSPS, respectively). This implies that hafnium diboride after the FSPS fractures “like a” composite [37], where the large  $\text{HfB}_2$  grains serve as a reinforcing phase of the matrix consisting of fine-grained  $\text{HfB}_2$  (hence the change in slope can be seen during the flexural test). Alternatively, a high work to fracture is due to thermal stresses induced by the high heating/cooling rates during the FSPS processing. However, in the absence of further experiments with ceramic bulks with bimodal grain size distributions, this question remains unanswered.

1 After the flexural tests at 1600 °C, the fracture of the FSPSed and CSPS was much smoother  
2 than that at room temperature. The appearance of rounded grains (i.e., number of grains with  
3 sharp corners decreased substantially) was very noticeable due to the activation of plastic  
4 deformation and surface diffusion. In terms of the flexural strength, at 1600 °C, the FSPS and  
5 CSPS specimens showed a remarkable difference. With an increase in the temperature, the  
6 FSPSed specimens showed a rapid decrease in strength; to 282±19 MPa at 1600 °C, while in  
7 the case of the CSPSed specimens, a slight decrease in the flexural strength was observed, i.e.  
8 493±24 MPa.  
9

10 The FSPS specimen showed a gradual decrease in strength (**Fig. 11**) [2,25,38–41] and  
11 behaved in a quasi-plastic manner even at 1200 °C, in contrast, the CSPS specimens showed  
12 a slight plasticity at 1600 °C. Hence, the flexure strength difference between specimens at  
13 1600 °C is more likely to be a combination of plastic deformation and grain size. Kalish et al.  
14 [2] observed an increase in the flexural strength of HfB<sub>2</sub> from 25 °C to 1000 °C, i.e. 344 MPa  
15 to 460 MPa, followed by a rapid decrease at 1400 °C, where a strength below 200 MPa was  
16 observed. It was argued that a decrease in strength can be attributed to heterogeneous slip  
17 processes and elastic residual stresses.  
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19 In this study, even at 1600 °C, some HfB<sub>2</sub> grains for the CSPS specimen fractured in a trans-  
20 granular manner. Similar to the observation in [2,40], a number of grains fracturing in a  
21 transgranular manner may control the strength. Therefore, because intergranular fracture  
22 dominates in the FSPS case at elevated temperatures (presumably because the grain size is  
23 much different than that in the CSPS case), this may also be an indirect indication of the  
24 strength decrease.  
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26 This is in good agreement with the general observation that the large grain ceramics are  
27 naturally more resistant to creep than the finer grained ceramics at elevated temperatures. In  
28 the present study, an FSPS specimen with a unique microstructure showed some plasticity at  
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1 600 °C, and a further increase in temperature thus lead to a gradual strength decrease (see  
2 **Fig. 2 (g)**). Other factors that might affect the strength at elevated temperatures are (i) short  
3 processing time (compare 1 min vs 5 min for the FSPS and CSPS at 2000 °C, or as high as 60  
4 min. at 1900 °C for hot pressing [3]), and (ii) the relaxation of the internal thermal stresses  
5 [42,43] induced by rapid processing of the hafnium diboride during the FSPS. Due to local  
6 stress gradient, which is a direct result of the temperature gradient during FSPS, some of the  
7 preliminary specimens had macroscopic cracks. This is a crucial factor when scaling up, e.g.,  
8 from 1 to 5 mm thickness, but an additional short dwell at elevated temperature seems to be a  
9 vital step to equilibrate the temperature within a specimen and thus increase the chances of  
10 obtaining a crack-free specimen [12]. This allows further optimization of the FSPS process, if  
11 the generation of an abnormal structure reported in the present study is not required.  
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#### 29 **4. Conclusions**

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31 In summary, as received, coarse HfB<sub>2</sub> powder, was subjected to pre-densification by SPS and  
32 then consolidated to a high density using CSPS and FSPS without sintering aids. Rapid  
33 consolidation (total discharge time below 60 s) using FSPS resulted in a bimodal grain size  
34 distribution, where large-sized 10-μm grains were evenly distributed in the specimen  
35 consisting of 1 to 5 μm grains. A comparable density was achieved by CSPS only after a 5-  
36 minute dwell at 2000 °C, but associated with significant grain growth. Such a difference in  
37 grain size suggests complex densification mechanisms of the flash-type processes, which  
38 may be favorable to the development of unique structures. The flexural strength results  
39 confirm that despite ultra-rapid processing, ceramics with a strength of 650 MPa were  
40 attained.  
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## Figure captions

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2 **Fig. 1.** Structure evolution during FSPS of  $\text{HfB}_2$  monoliths: (a) original powder, (b)–(d)  
3 show a fracture surface of typical ‘green’ specimen after three-point flexure at room  
4 temperature. (e) shows output of Sumitomo unit during FSPS run at  $2000 \pm 50$  °C. Mind that  
5 after roughly 50 seconds, the specimen reached a plateau in temperature, where it is thought  
6 that the consolidation dwell time starts. The SPS is manually switched off after experiencing  
7 a slight increase in temperature (and thus shrinkage), which may be an indirect indicator that  
8 the full density of the specimen was reached. Prior to that we experienced only a slight  
9 increase in the macroscopic shrinkage after reaching the temperature of  $\sim 1920$  °C. Note that  
10 after reaching the peak voltage of 6 V, the voltage slowly decreased, which is an indirect  
11 indication of the specimen densification.  
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26 **Figure 2** Structure of the bulk hafnium diboride specimens after FSPS with maximum  
27 temperature of (a) (#100) 2220 °C and (b) (#88) 2000 °C (no dwell in both cases), and  
28 moderate heating rate of 800 °C/min was used via manual control of the SPS power ( $\sim 30\%$  of  
29 total power) in order to improve the accuracy of the temperature measurements. Inset in (a)  
30 shows the polished surface of  $\text{HfB}_2$  specimen (left side in the (a)). Note that for the specimen  
31 presented in (b), some local grain growth can be seen on the left side (SPS’s upper punch),  
32 while the grain size on the right side (SPS’s lower punch) is uniform. Both images were taken  
33 in the BSE mode. In the case of the (b), the black areas are contamination from the graphite  
34 felt caused during the SEM observations as both sides of the fracture were examined.  
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48 **Fig. 3.** Details of fracture by FSPS of  $\text{HfB}_2$  monoliths: (a)–(c) show fracture surfaces of  $\text{HfB}_2$   
49 after the FSPS following flexural test at room temperature, while (d)–(f) are after the flexural  
50 strength test at 1600 °C. Note the chaotic distribution of the large grains in (a) and (d) does  
51 not change. (g) shows typical loading diagrams observed flexural strength test for bars in  
52 (c),(f). High-temperature data at 600 °C and 1200 °C were collected using a single test and  
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1 are presented in order to show the tendency in the flexural strength behavior at elevated  
2 temperatures.  
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4 **Fig. 4.** SEM images of HfB<sub>2</sub> ceramic obtained by CSPS (2000 °C/ 5 min) after flexural test at  
5 (a,c) room temperature and (b,d) 1600 °C. Mind that for (a) and (b), the majority of pores are  
6 located within the grains, and have both spherical and elongated shapes; (b) shows that some  
7 of the grains were fractured in a trans-granular manner. (e) compares the data of HfB<sub>2</sub>  
8 obtained in this study with previously obtained results for HfB<sub>2</sub> [2,3,6,18] and TaB<sub>2</sub> [19]. In  
9 the case of the bimodal structure for the FSPS the data points correspond to the large and fine  
10 grains.  
11

12 **Fig. 5.** Temperature dependence of shrinkage for the powder specimen during FSPS  
13 experiments using a Sumitomo unit (#66 F). One can see three distinctive zones: (1)  
14 pyrometer adjustment, (2) flash sintering and (3) a zone for a short dwell. The displacement  
15 rate is provided as the red dashed line.  
16

17 **Fig. 6.** Shrinkage rate for the powder specimen during the FSPS experiments using a  
18 Sumitomo unit (#66F) as a function of the inverse temperature. The temperature was  
19 experimentally determined (see section 3.1). One can see that roughly the same three zones  
20 can be noticed. The Figure (b) inset shows the elevated temperature dependence of the  
21 shrinkage in detail. Mind the presence of the area where the temperature decreased after  
22 reaching 2000 °C. At this point, the temperature was manually controlled using the current  
23 value, and after a short dwell during which the temperature rapidly increased, the SPS unit  
24 was turned off.  
25

26 **Fig. 7.** Shrinkage rate for the powder specimen during the FSPS experiments using a  
27 Sumitomo unit (#66F) as a function of the inverse temperature. One can see that roughly the  
28 same three zones can be observed. Importantly, a linear behavior of the densification rate  
29 between 860 °C and 1760 °C allows estimation of the activation energy.  
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**Fig. 8.** Evaluation of the activation energy for the hafnium diboride consolidated by flash spark plasma sintering. Additional data points show the effect of the possible error associated with the temperature measurement. The evaluated values of the apparent activation energies were evaluated by linear fitting.

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**Fig. 9.** Schematic diagrams showing contribution of main processes at consolidation on different stages of the process. Temperature zone for the flash processes (FSPS) is indicated. Note that because grain growth in a porous body requires a higher temperatures, development of bimodal structures is expected if the bulk overheating and hot-spot generation are active. (b) shows that in the case of the grain growth accelerated at higher temperatures requires a lower driving force, and has a higher growth rate. These two factors allow one to obtain ceramics with a bimodal grain size (possible window of opportunity). Heating rate underline finding of [35] for alumina, where surface diffusion was avoided while using heating rate of 600 °C/min.

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**Fig. 10.** Details of fracture of FSPSed of HfB<sub>2</sub> monoliths at ambient temperature: (a) and (b) show macroscopic images of flexure bars after the tests, while (c) present loading curves observed during fracture. Large-sized grains with identical grain size were highlighted in (a) and (b) in order to show their distribution.

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**Fig. 11.** Effect of temperature on the flexural strength of transition metal diborides [2,25,38–40] and diboride–diboride composite [41]. Argon was used during the high-temperature flexural test for all the reported data. The dashed line for the ZrB<sub>2</sub> ceramics indicates the general tendencies observed in previous studies [38,39]. The closed symbols indicate that the strength was measured using a four-point setup and the open symbols show the results of the three-point flexural strength tests.

Tables

**Table 1** Experimentally determined activation energy, and estimated sintering mechanism for transition metal diborides of the IV group.

Diboride	Consolidation method	Applied pressure, MPa	Activation energy, kJ/mol	Possible mass transport mechanism
HfB <sub>2</sub>	FSPS	20	99	Volume diffusion*
			66	Grain-boundary diffusion*
HfB <sub>2</sub>	FSPS error of +100 °C is assumed	20	74	Volume diffusion*
			111	Grain-boundary diffusion*
HfB <sub>2</sub>	FSPS error of +300 °C is assumed	20	90	Volume diffusion*
			132	Grain-boundary diffusion*
HfB <sub>2</sub> [28]	High-pressure hot-pressing	790	96	Volume diffusion of boron, or stress-directed grain boundary diffusion of hafnium
ZrB <sub>2</sub> [29]	Hot-pressing	50	695±62	Volume diffusion
ZrB <sub>2</sub> [30]	Pressulress sintering	-	416±174 and 678±114	-
TiB <sub>2</sub> [31]	Pressureless sintering	-	774±46	Volume diffusion
TiB <sub>2</sub> [32]	Microwave sintering	-	850±60 and 638±20	-
Boron diffusion in TiB <sub>2</sub> [33]		-	190	Volume diffusion

\* It is assumed that this is volume of grain boundary diffusion of B in HfB<sub>2</sub>, based on findings in [28] and [33]. Metal atoms usually have an activation energy of bulk diffusion in diboride lattice ~ 1000 kJ/mol, see for instance [19].

Figure 1  
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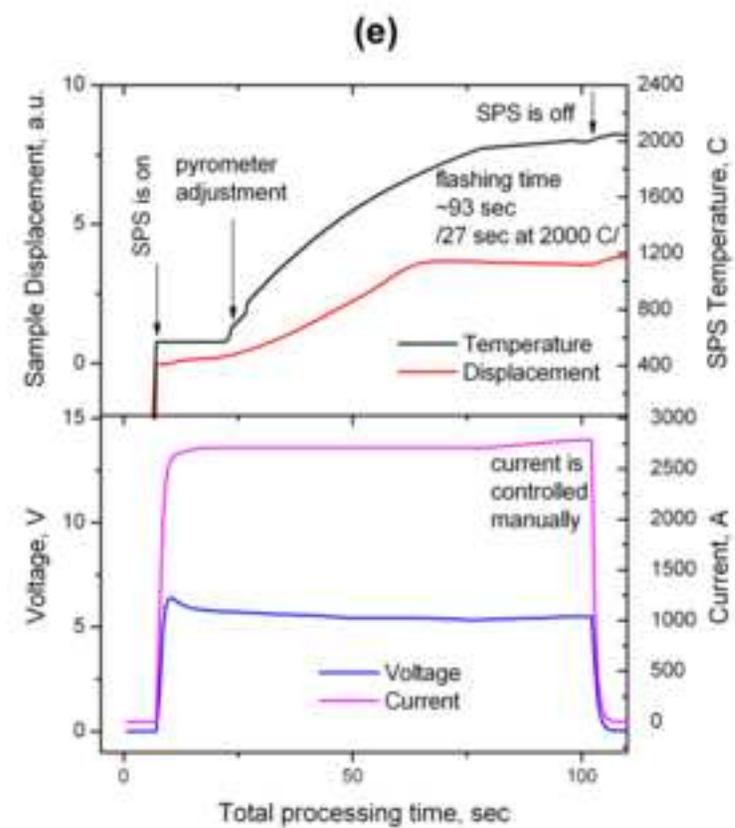
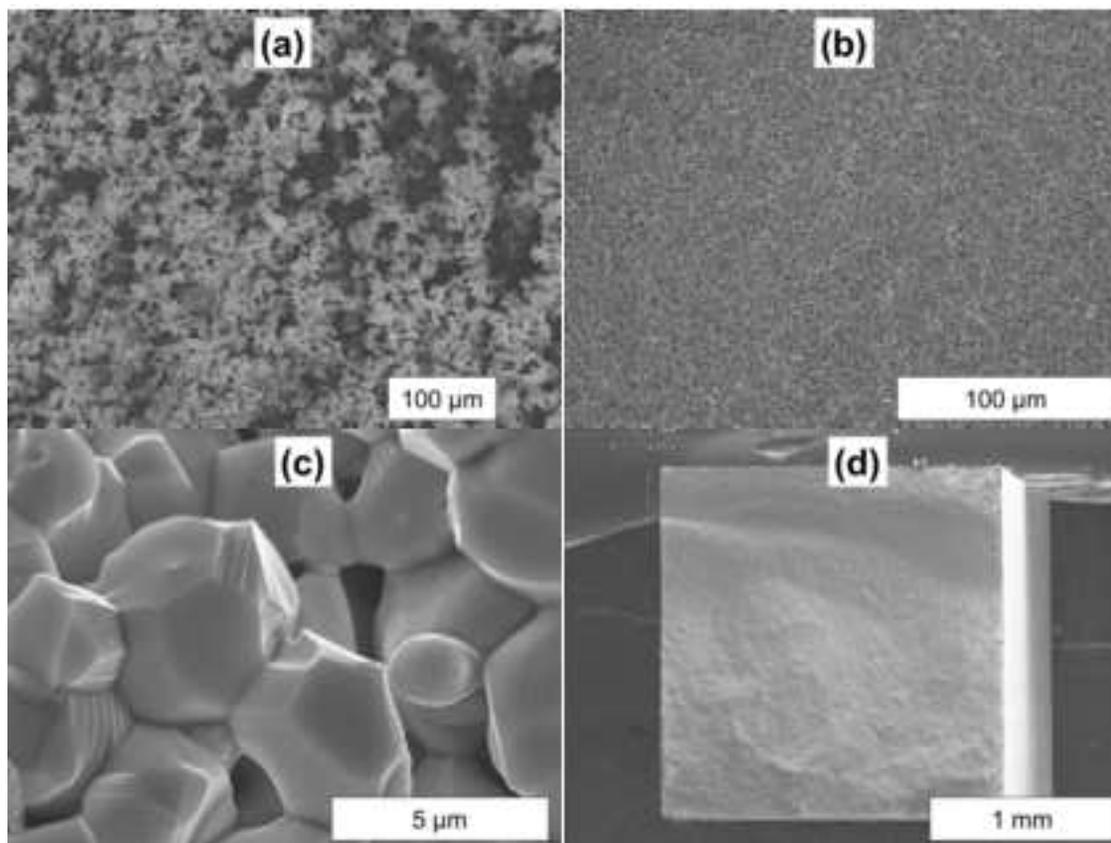
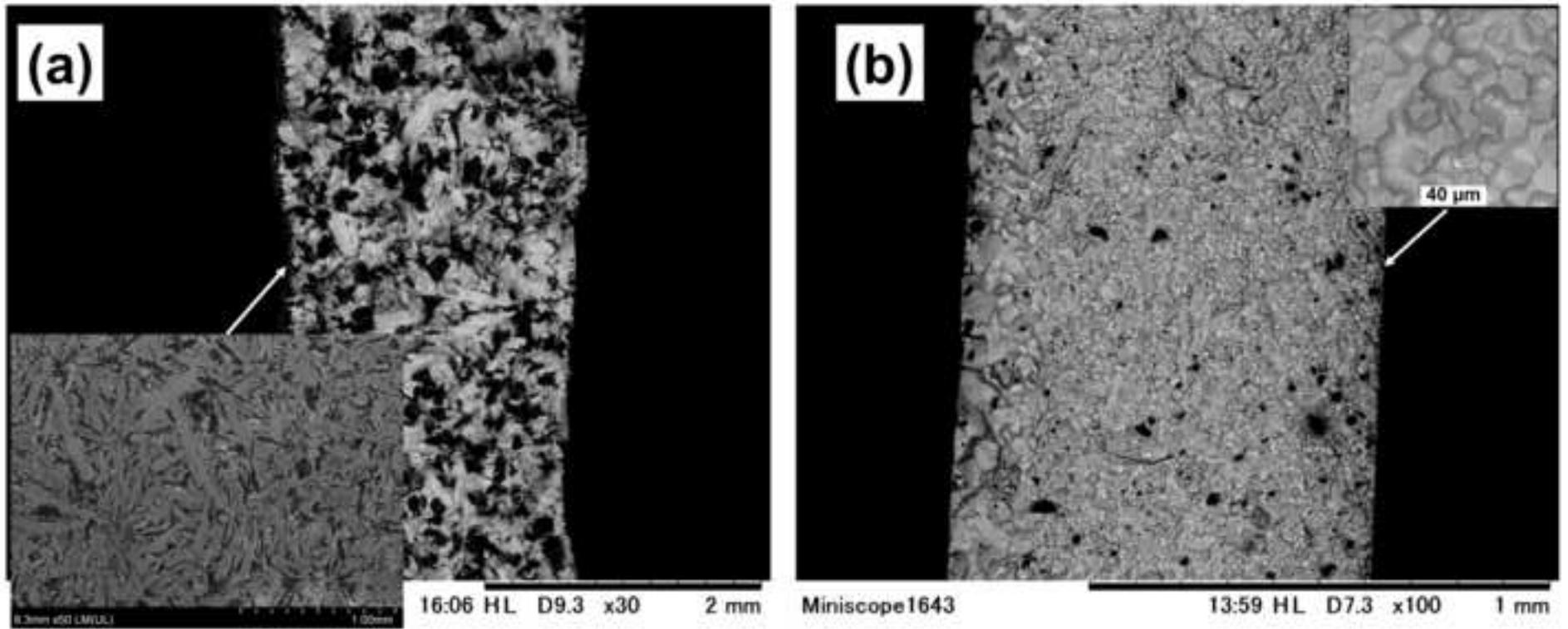


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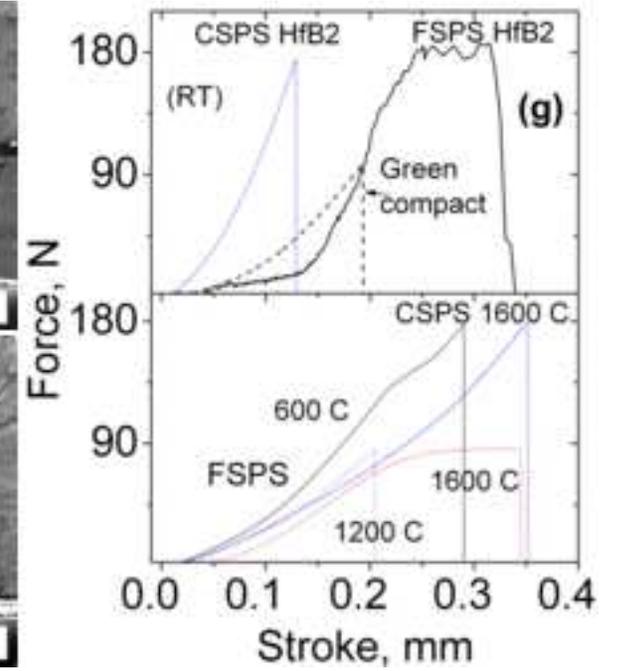
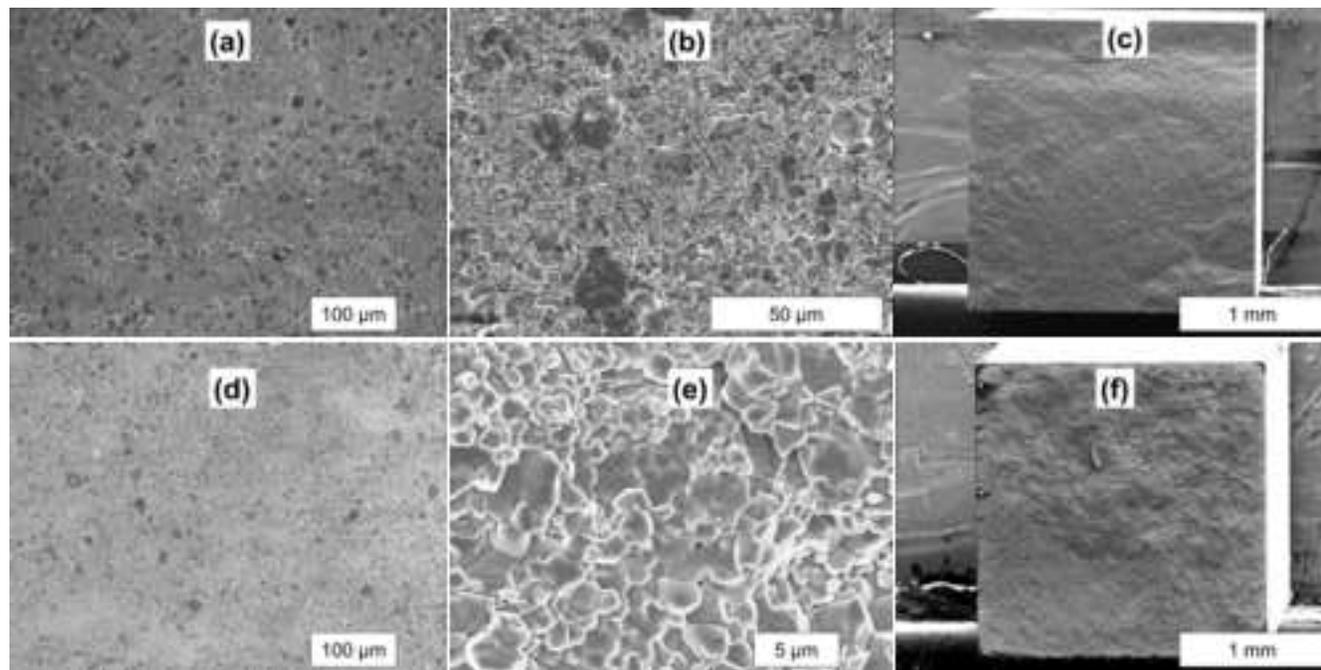


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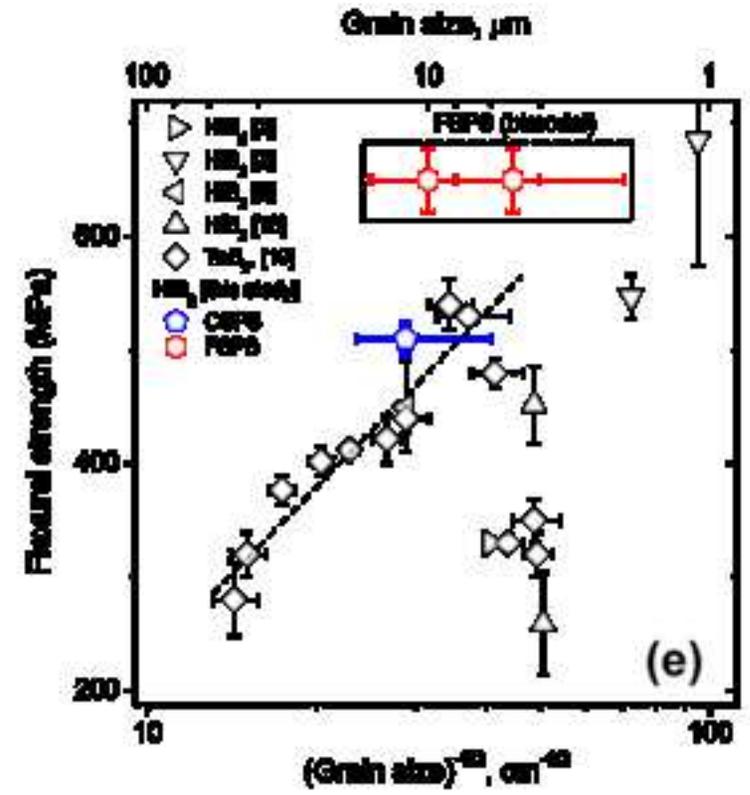
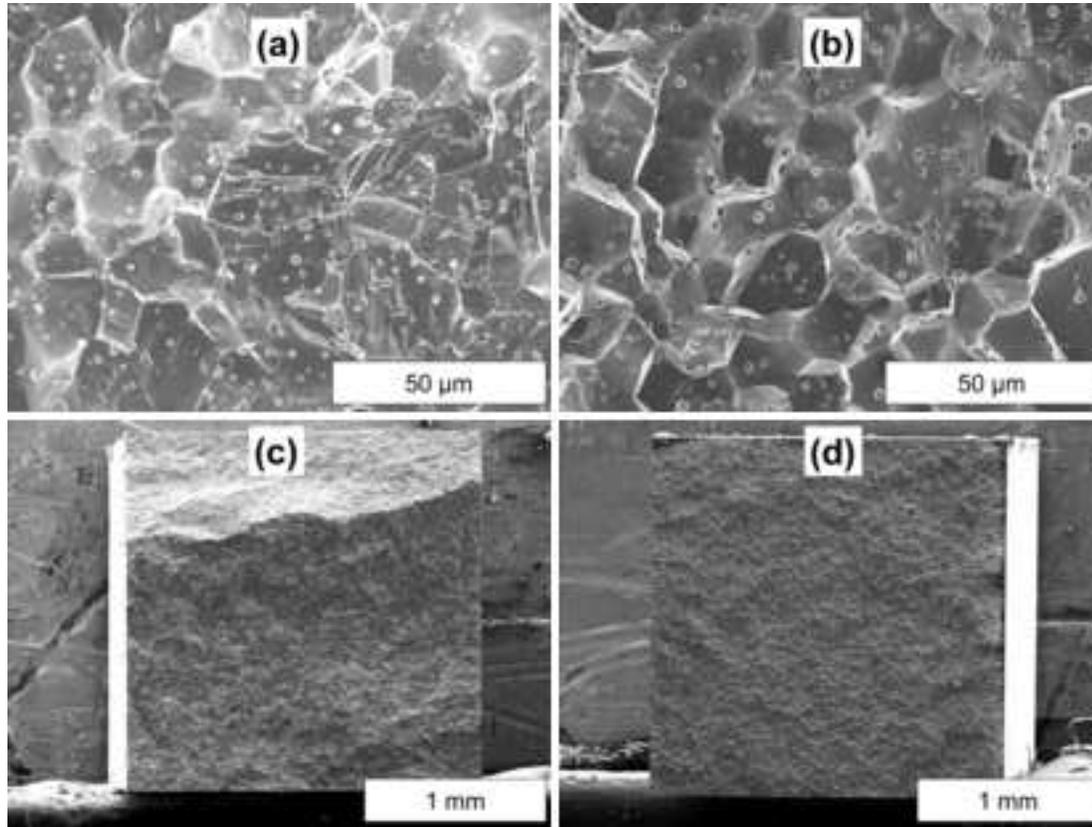


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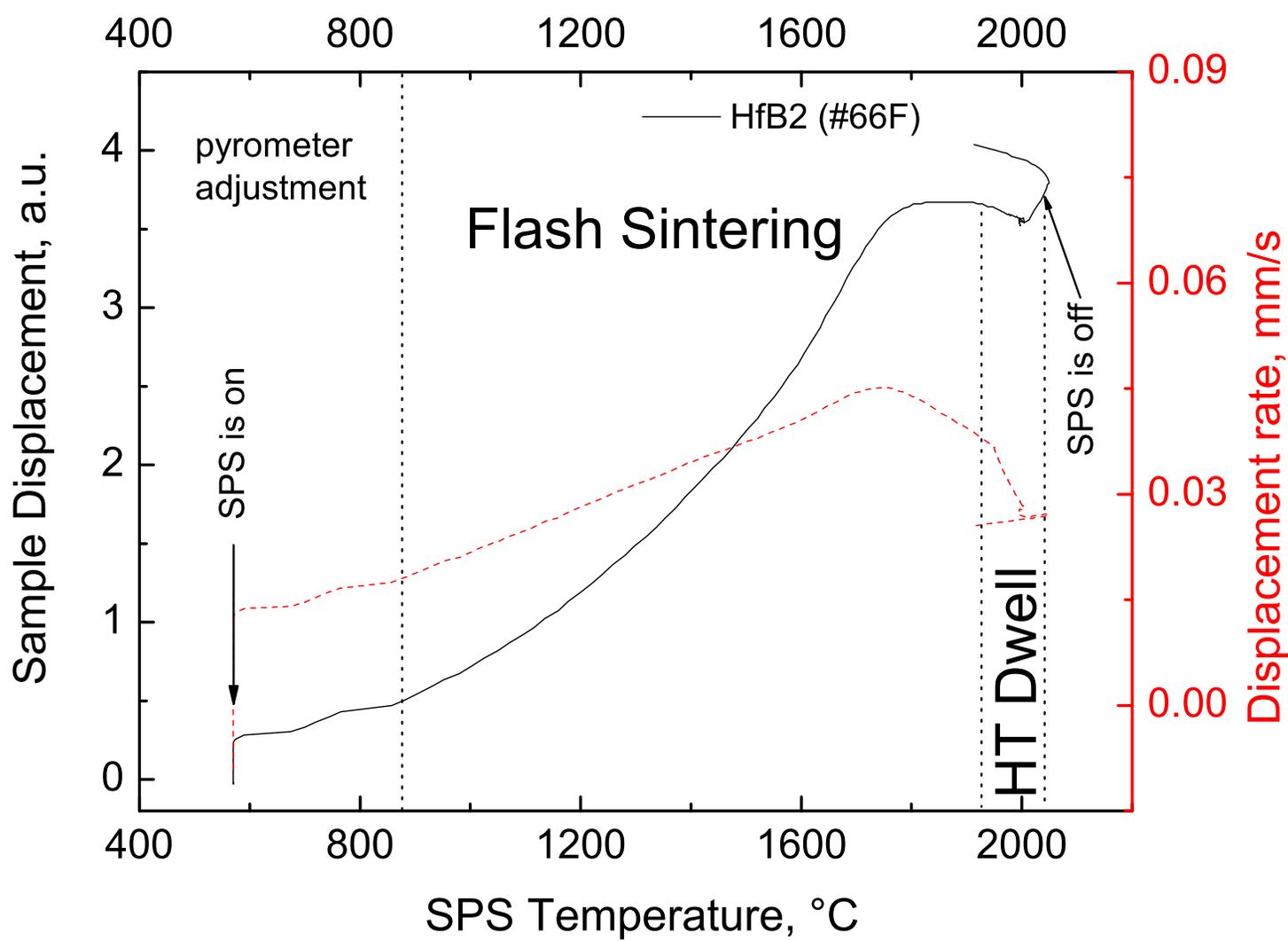


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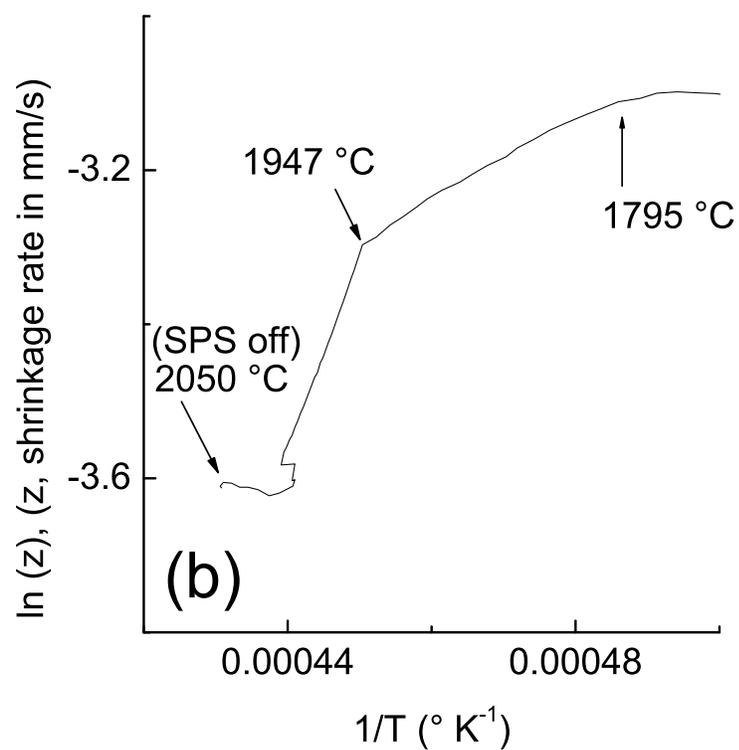
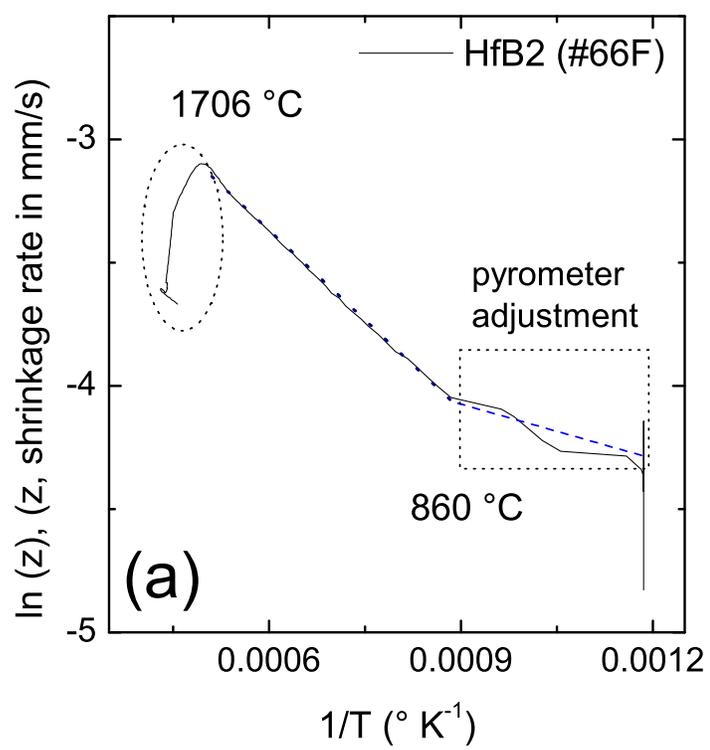


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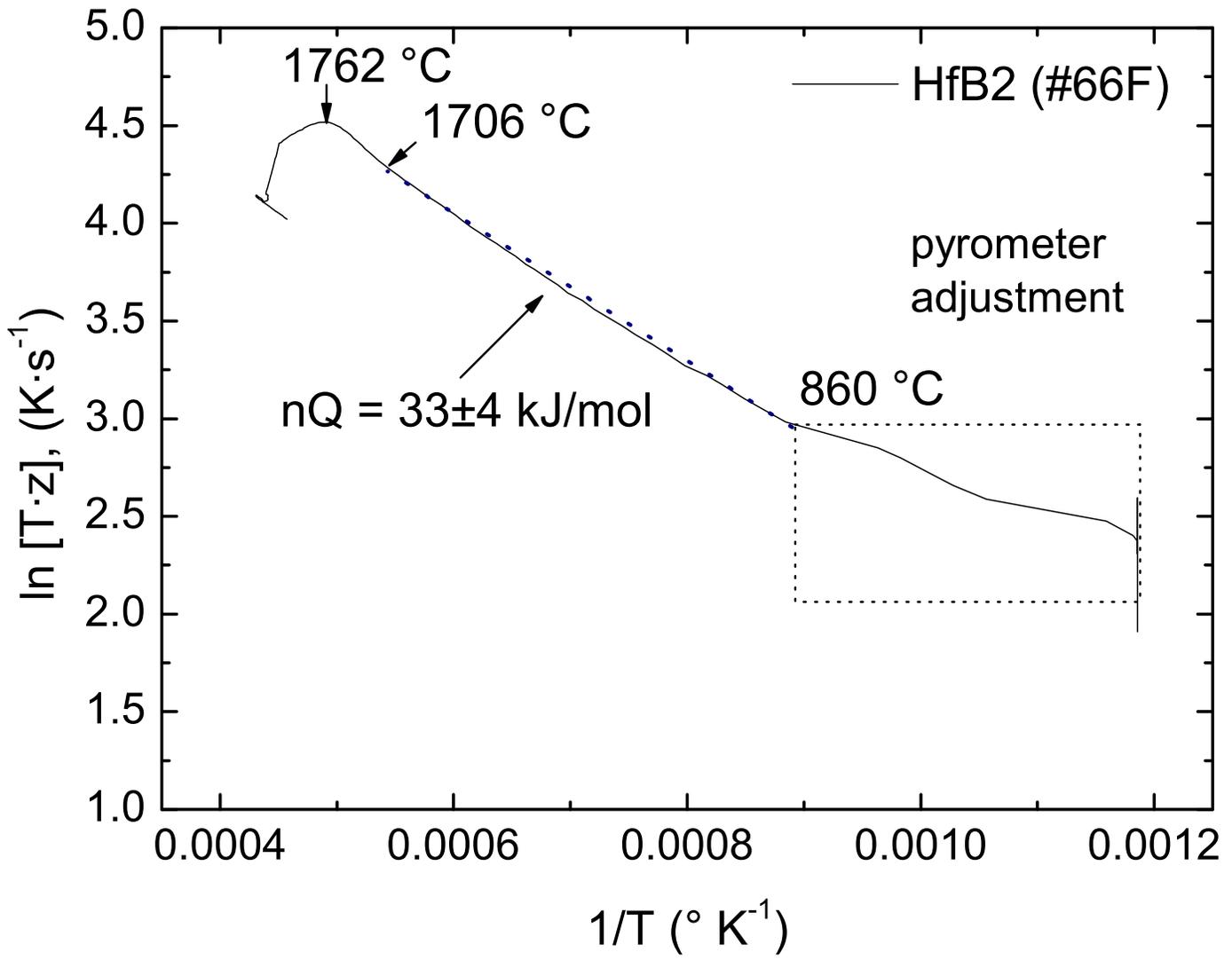


Figure 8

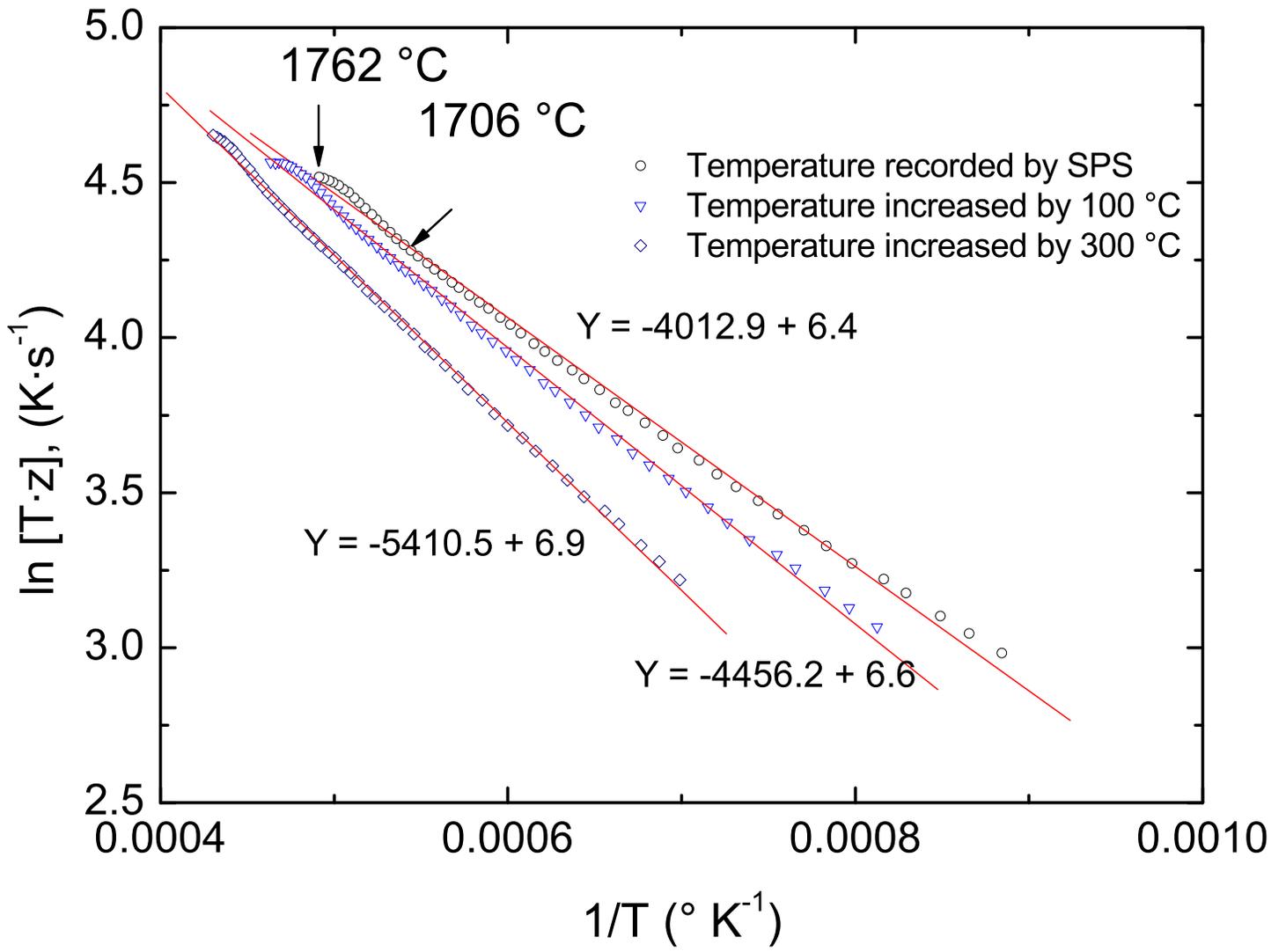


Figure 9

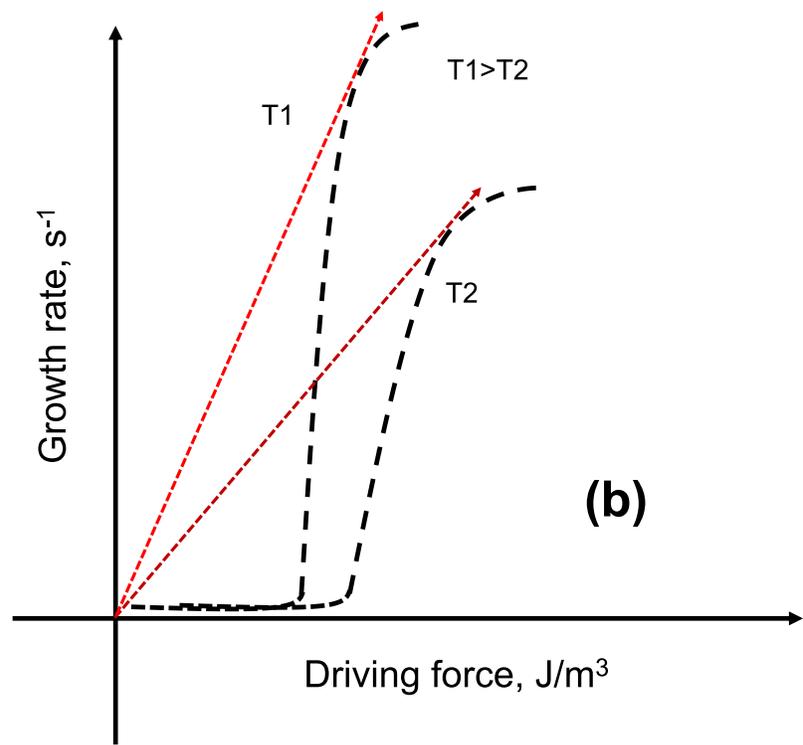
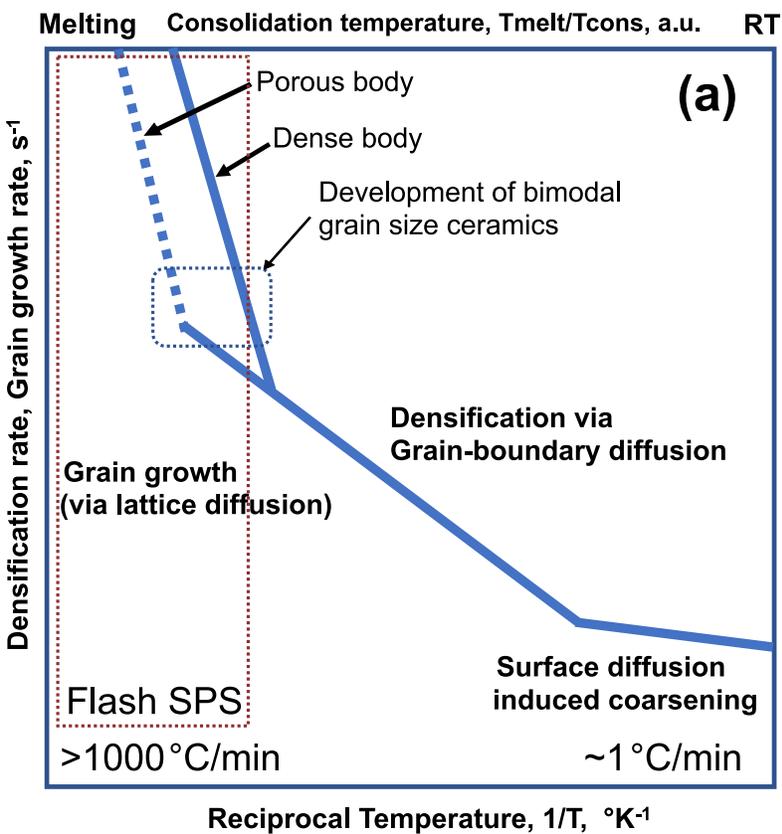


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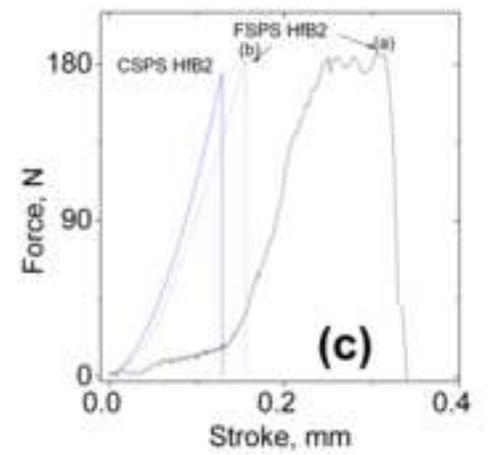
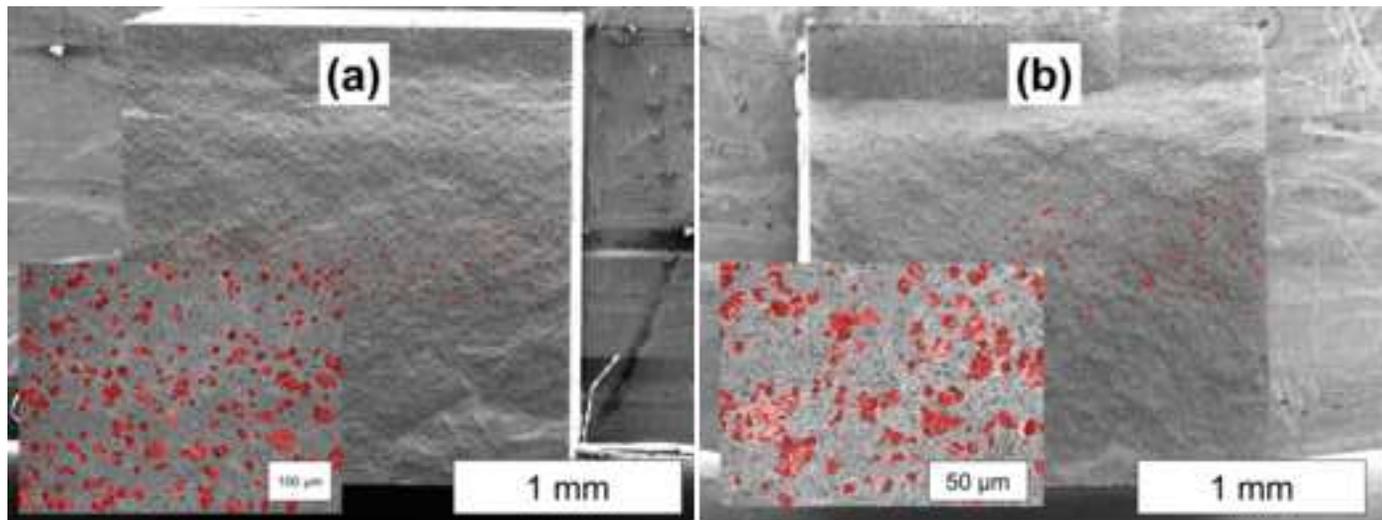


Figure 11

