



## Abstract

11

12 We have investigated the moiré Bloch bands of photoexcited electrons in image potential states  
13 (IPS) on graphene covered Ir(111) surfaces using high-energy-resolution angle-resolved two-photon  
14 photoemission spectroscopy. An energy gap of approximately 20 meV at the  $\bar{K}$  point of the moiré  
15 Brillouin zone is resolved. The band structure is well reproduced by density functional theory  
16 (DFT) combined with the embedded Green’s function technique. A simplified periodic potential  
17 model, whose spatial distribution shows close agreement with the DFT results, also describes the  
18 system well. These findings demonstrate that the electronic band structure of photoexcited states  
19 can be engineered solely via moiré potential modulation. This opens a new avenue for excited-  
20 state band engineering and the design of ultrafast optoelectronic functionalities in moiré-engineered  
21 materials.

22 When a two-dimensional (2D) material is grown on a crystalline surface, or when multiple  
23 2D materials are stacked with a mismatch in their lattice periodicities or orientations, spa-  
24 tial interference patterns known as moiré structures emerge[1]. Although moiré structures  
25 were once appreciated mainly for their geometric aesthetics and usefulness in structural  
26 analysis[2], their functional significance has come into focus more recently. In particular,  
27 novel electronic transport phenomena arising from the moiré superlattice, such as the emer-  
28 gence of superconductivity and Mott insulating states in twisted bilayer graphene at so-called  
29 “magic angles” [3, 4] and fractal electronic spectra known as Hofstadter’s butterfly [5], are  
30 regarded as one of the most impactful advances in condensed matter physics in the past  
31 decades.

32 The relevance of moiré superlattice have been recognized also in optical processes. For ex-  
33 ample, spatially localized excitons in moiré superlattices formed by stacked transition metal  
34 dichalcogenides[6] has opened new possibilities for controlling photoexcitation and light–  
35 matter interactions. However, in contrast to electronic transport, the implications of moiré  
36 effects in optical phenomena remain poorly understood. To gain a deeper understanding  
37 of such optical properties, it is important to focus on moiré Bloch bands[7], which played  
38 a crucial role in explaining exotic electronic behavior. These miniband structures, formed  
39 via hybridization of electronic states under the long-range periodic potential of the moiré  
40 pattern, may also be key to understanding moiré-modified light–matter interactions.

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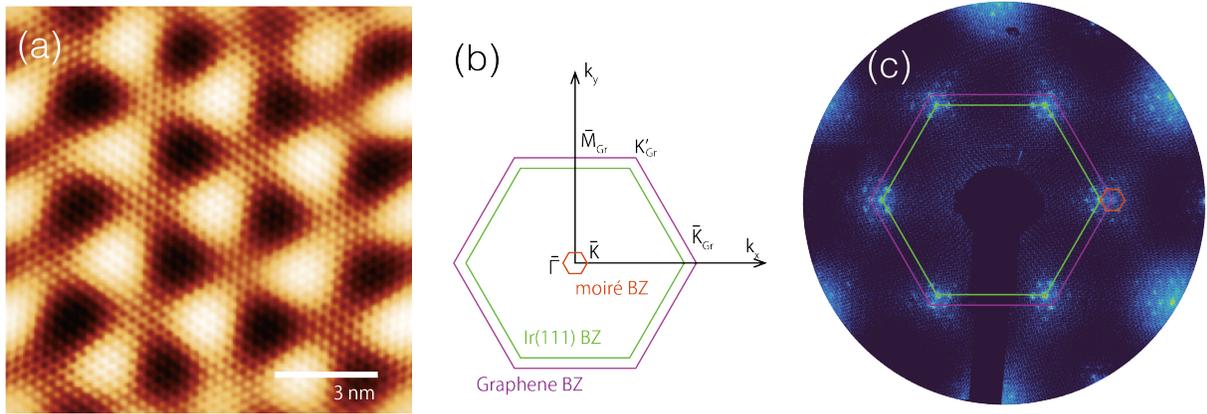


FIG. 1. (a) Scanning tunneling microscope (STM) image of graphene covered Ir(111) (Gr/Ir(111)) surface, showing the formation of long-period moiré superlattice due to the lattice mismatch between graphene and Ir(111) surface. The bias voltage and the tunneling current were set to -80 mV and 1.2 nA, respectively. (b) Brillouin Zones (BZs) of the Ir(111) surface and graphene lattices, drawn to scale. The moiré BZ, indicated by the red hexagon, shows a significantly reduced size, enabling the emergence of miniband. (c) LEED picture of Gr/Ir(111), showing sharp diffraction spots from Ir, carbon and the surrounding moiré satellites, indicating high structural quality and uniformity of the sample surface.

42 In this Letter[8], we report the experimental observation of moiré Bloch bands of photoex-  
 43 cited electrons in image potential states (IPS) on the graphene-covered Ir(111) (Gr/Ir(111))  
 44 surfaces (Fig. 1), by using high-resolution angle-resolved two-photon photoemission (HR-  
 45 AR2PPE) spectroscopy [9, 10]. As shown in Fig. 1(a), Gr/Ir(111) provides a well-defined  
 46 moiré superlattices with a periodicity of approximately 25 Å, which is much larger than  
 47 the lattice constant of graphene (2.46 Å) and Ir(111) (2.72 Å) [11, 12]. It is widely ac-  
 48 cepted that the (10×10) supercell of graphene on the (9×9) cell of Ir(111) well describes  
 49 the Gr/Ir(111) superlattices, with the lattice vectors of graphene and Ir(111) being aligned  
 50 in orientation [11, 12]. Thus, the Brillouin zones (BZ) of these two surfaces and resulting  
 51 moiré BZ are drawn as shown in Fig. 1(b). IPS are quantized electronic states formed by the  
 52 Coulomb attraction between an electron and its induced image charge at a metallic surface.  
 53 Owing to their well-defined nature and surface sensitivity, IPS serve as an ideal platform  
 54 for investigating photoexcited carrier dynamics, including energy relaxation and quantum

55 interference phenomena on solid surfaces[13, 14]. We expected that their surface sensitivity  
56 makes IPS particularly suitable for probing moiré potential effects, such as the formation of  
57 moiré bands in photoexcited states. Previous works investigated IPS on graphene-covered  
58 metal surfaces[15–20], revealing the energy positions, lifetimes, and the effective masses.  
59 On certain metal surfaces such as the Ru(0001), graphene forms a relatively large rippled  
60 structure, which leads to a band splitting of the IPS state[15]. However, the effect of the  
61 moiré superlattice on the electronic structure of IPS has not been fully explored, and, to  
62 our knowledge, the opening of a gap in the moiré Bloch bands of the unoccupied states has  
63 not been reported. This motivates our present study on Gr/Ir(111) IPS, where we directly  
64 probe the moiré-induced electronic reconstruction in the unoccupied states

65 The experimental setup consisted of a laser system and an ultra-high vacuum (UHV)  
66 electron spectroscopy system. A Ti:sapphire laser oscillator generated infrared (IR) pulses  
67 with 2.0 ps duration at 80 MHz. Part of the IR output was converted to ultraviolet (UV)  
68 light using nonlinear crystals. P-polarized IR and UV pulses were aligned collinearly and  
69 focused onto the sample. Two-photon photoemission (2PPE) measurements were conducted  
70 in an ultra-high vacuum system with a base pressure below  $7 \times 10^{-11}$  mbar. The sample  
71 temperature was held at 11 K during the measurements. Energy and momentum resolutions  
72 were 9.5 meV and better than  $0.01 \text{ \AA}^{-1}$ , respectively. Graphene was grown by a two-step  
73 thermal decomposition of ethene [11, 21] on the clean Ir(111), confirmed by a sharp moiré  
74 induced spots in low energy electron diffraction (LEED) as shown in Fig. 1(c). First-  
75 principles calculations were performed using density functional theory (DFT) combined  
76 with the embedded Green’s function and full-potential linearized augmented plane-wave  
77 methods[22–25] for modeling graphene on the semi-infinite Ir(111) substrate. The DFT  
78 potential  $\bar{V}_{\text{eff}}(z)$  was smoothly matched to a classical image potential[26] to describe IPS.  
79 Experimental and computational details are provided in the Supplemental Material[8], which  
80 includes the following literatures [10, 11, 21–37].

81 Figure 2 shows the HR-AR2PPE spectra for the first IPS of Gr/Ir(111). The pump and  
82 probe photon were 4.401 and 1.467 eV, respectively. At normal emission, the peak was  
83 located at 5.308 eV with a width of 56 meV, indicating the binding energy of IPS with  
84 respect to the vacuum level is -0.849 eV (The workfunction determined from the vacuum  
85 level cutoff was 4.69 eV.). Unlike the 2PPE data of IPS on noble metal such as Cu(001) and  
86 Ag(001), the maximum intensity does not occur at the bottom of the band. This strong

87 intensity originates from the surface resonances of the Ir(111) in the occupied region [37].  
 88 This surface resonance is known as a Rashba-type spin-split hole-like band. Although the  
 89 intensity is weak, photoelectrons coherently excited from the surface resonance state are  
 90 indeed observed[8]. These values and features are consistent with the previous report [17].

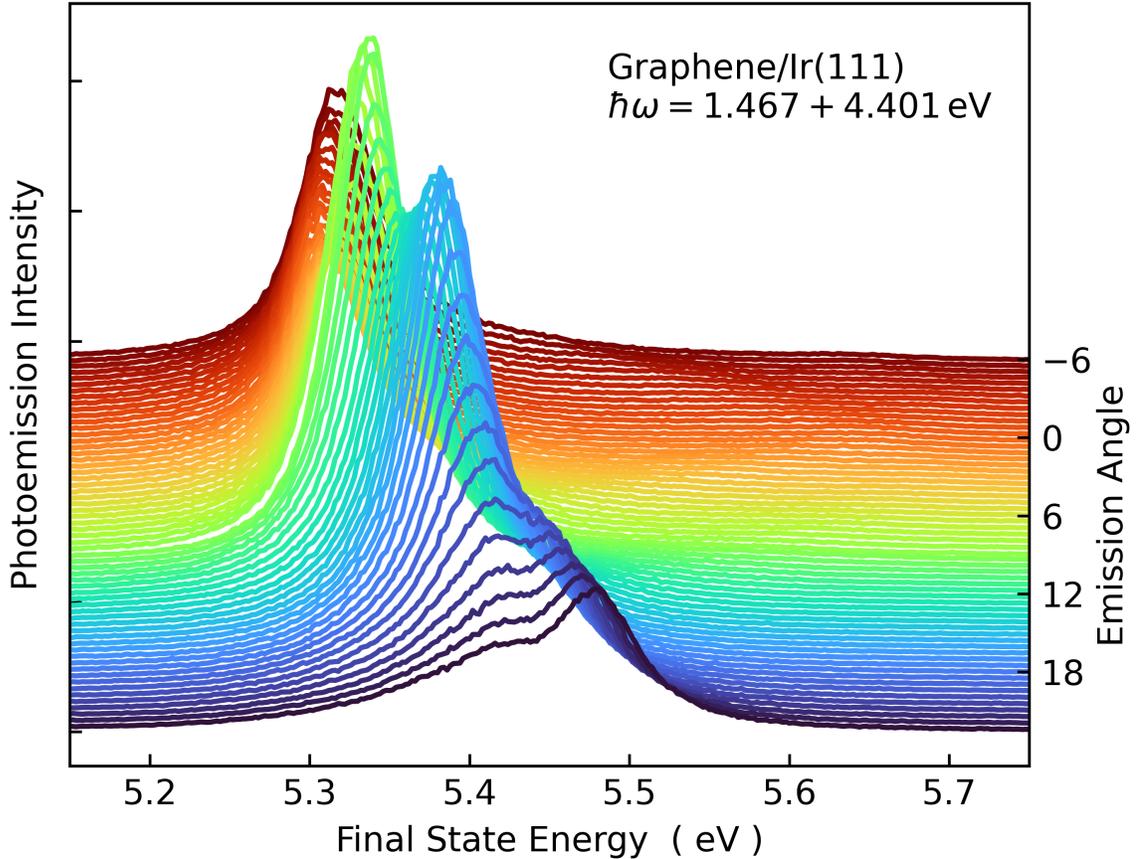


FIG. 2. Angle resolved two-photon photoemission spectra of graphene covered Ir(111). At low angles, a single peak appears at around 5.3 eV final-state energy. The final state energy refers to the excited state energy measured from the Fermi level. As the emission angle increases, a shoulder emerges and evolves into a pronounced double-peak structure, clearly visible at  $23^\circ$ , indicating an energy gap of  $\sim 20$  meV at the  $\bar{K}$  point of the moiré BZ. This angular-dependent splitting provides direct experimental evidence of the formation of moiré Bloch bands in the unoccupied electronic structure.

91 Importantly, while a single peak is observed at low emission angles, the spectra exhibit a

92 pronounced double-peak structure at higher emission angles. As the emission angle increases,  
 93 a shoulder starts to develop around 17°. At 23°, the spectrum clearly exhibits a double-peak  
 94 structure, with an energy separation of 62 meV between the peaks. This splitting clearly  
 95 demonstrates the presence of an energy gap in the unoccupied electronic states, providing  
 96 direct experimental evidence of the moiré-induced band modification. By spectral fitting  
 97 using two Lorentzian curves, we have evaluated the energy gap at the  $\bar{K}$  point of the moiré  
 98 BZ to be 20 meV[8].

99 Figure 3 shows the log-intensity map of the electronic structure of moiré Bloch band  
 100 arising from IPS of Gr/Ir(111). This data is obtained from the HR-AR2PPE spectra taken  
 101 by using another photon energy pair: 1.600 + 4.800 eV. The measured IPS spectra along  
 102 the  $k_x$  direction (along  $\bar{\Gamma}$ - $\bar{K}$ , see Fig. 1(b)) show the energy splitting induced by the moiré  
 103 potential. We confirmed that the location of the energy gap in the momentum axis and its  
 104 magnitude are essentially independent of the excitation photon energy. Furthermore, one  
 105 can see the folded band appears well. These features also clearly imply a robust feature of  
 106 the moiré superlattice.

107 The emergence of the moiré band with an energy gap is supported by DFT calculations. In  
 108 supplemental materials[8], the calculated band dispersion was imposed on the experimental  
 109 results (see. Fig. S3). Since the band splitting due to spin-orbit coupling was less than a few  
 110 meV, we plotted the energy dispersion averaged over two spin components. The calculated  
 111 energy levels have been shifted upward by 80 meV to align the experimental results. Note  
 112 that the actual binding energy discrepancy between the experimental and theoretical energy  
 113 values is larger when considered relative to the vacuum level. The calculated work function  
 114 was 4.847 eV, resulting in a binding energy discrepancy of -89 meV. The calculated energy  
 115 gap at the  $\bar{K}$  point of the moiré BZ was 22 meV. Although the energy values does not precisely  
 116 reproduce the experimental results, the overall band structure shows good agreement with  
 117 the measurements.

119 Since the electron in IPS essentially behaves as the free electron, the moiré Bloch band  
 120 arising from IPS is expected to be well described by a simplified nearly free-electron (NFE)  
 121 model under a periodic moiré potential. By fitting the DFT-calculated dispersion, we obtain  
 122 an effective mass equal to the free-electron mass, along with a complex Fourier coefficient  
 123 of the moiré potential  $V$ :  $V = \alpha + i\beta$ , where  $\alpha = 7.5$  meV and  $\beta = 1.1$  meV. This confirms  
 124 that the essential features of the moiré band, including the energy gap at the  $\bar{K}$  point, can

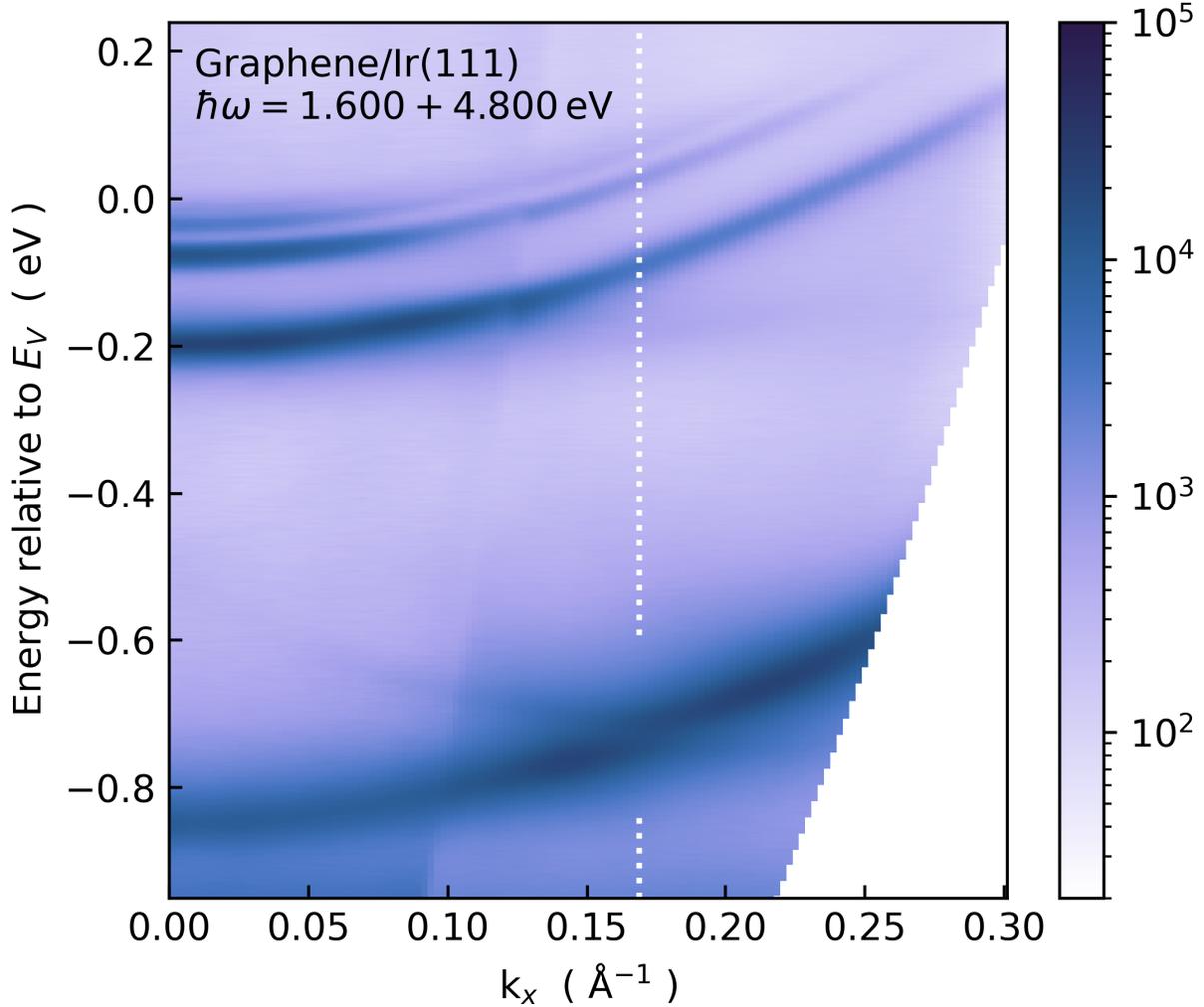


FIG. 3. A log-intensity map of electronic structure of moiré Bloch band arising from IPS of Gr/Ir(111). The  $k_x$  direction is along the  $\bar{\Gamma}$ - $\bar{K}$  direction in BZ, as shown in Fig. 1(b). The pump and probe photon energies were 4.800 eV and 1.600 eV, respectively. The vertical dotted line denotes the BZ boundary in the  $\bar{\Gamma}$ - $\bar{K}$  direction for the moiré BZ. The folded features match well with the theoretical prediction, despite weak intensity. The clear splitting observed near the  $\bar{K}$  point evidences the opening of a moiré-induced energy gap.

125 be quantitatively described by NFE model. Details of the model and the resultant fitting  
 126 curves are provided in the Supplemental Material[8], which shows that the NFE model nearly  
 127 perfectly reproduces both the experimental and DFT results.

128 Now let us examine the effective potential landscape induced by the moiré superlattice  
 129 in the electronic system. Figure 4(a) presents a contour map of the potential distribution

130 obtained from the NFE model, while Fig. 4(b) shows that derived from DFT calculations.  
 131 The height of the potential distribution in the plot (b) was determined by referencing the  
 132 charge density distribution along the surface normal. The first moment of the charge density  
 133 distribution was found to be 6 Å (Fig. 4(c)), and this value was used as the reference height.  
 134 While the potential distribution derived from the DFT calculations includes contributions  
 135 from atomic cores, the overall landscape of the potential is well reproduced by NFE model.  
 136 The situation  $\alpha \gg \beta$  implies that the system is essentially characterized by the sixfold  
 137 rotational symmetry, and the difference between the hcp and fcc sites in Gr/Ir(111) can be  
 138 neglected as shown in Fig. 4. This comparison further reinforces the interpretation that the  
 139 observed energy gap originates from the moiré potential.

141 As shown in Fig. 3, the energy gap opens in the energy dispersion relation of the first  
 142 IPS alone, while no gap is observed in the higher order ( $n \geq 2$ ) IPS. This is consistent with  
 143 the theoretical prediction that the spatial variation of the moiré potential for the higher  
 144 order IPS is too weak to open the gap. It is well known that the first moment of the  
 145 wave function, and thus that of the charge distribution, moves farther from the surface as  $n$   
 146 increases [13, 31]. This means that the electron in the higher order IPS feels a weaker moiré  
 147 potential, resulting in no gap opening. Indeed, the first moment of the charge distribution for  
 148 the second IPS is located at around  $z \sim 14$  Å in our DFT calculations as shown in Fig. 4(c).  
 149 Note that in Fig. 4(c),  $z_b$ [8] denotes the position above the plane of the embedding surface  
 150 on the vacuum side. In our calculation, we assume that at this position the potential curve  
 151 is given by the classical image potential and is independent of  $x$  and  $y$ . This corresponds to  
 152  $\alpha = \beta = 0$  in the NFE model, resulting in no energy gap. This result suggests that energy  
 153 gap can be controlled by tuning the modulation of the moiré potential.

154 We note that the IPS are free-electron-like states and therefore isotropic in  $k$  (i.e., the  
 155 constant energy surface should be circular). However, the moiré potential is not isotropic  
 156 and has a specific symmetry (see, e.g., the occupied spectrum in ref.[38]). In the present  
 157 work, we have measured the spectra only along the  $\bar{\Gamma}$ - $\bar{K}$  direction, but measurements along  
 158 other directions are planned for future studies to further explore the effects of the moiré  
 159 symmetry on the IPS. Our DFT calculations indicate that the band gap at the  $\bar{M}$  point is  
 160 about 15 meV, slightly smaller than that at the  $\bar{K}$  point. The NFE model also reproduces  
 161 this band gap at the  $\bar{M}$  point, although experimental confirmation is still required.

162 Before concluding, we would like to discuss the impact of the graphene structure on

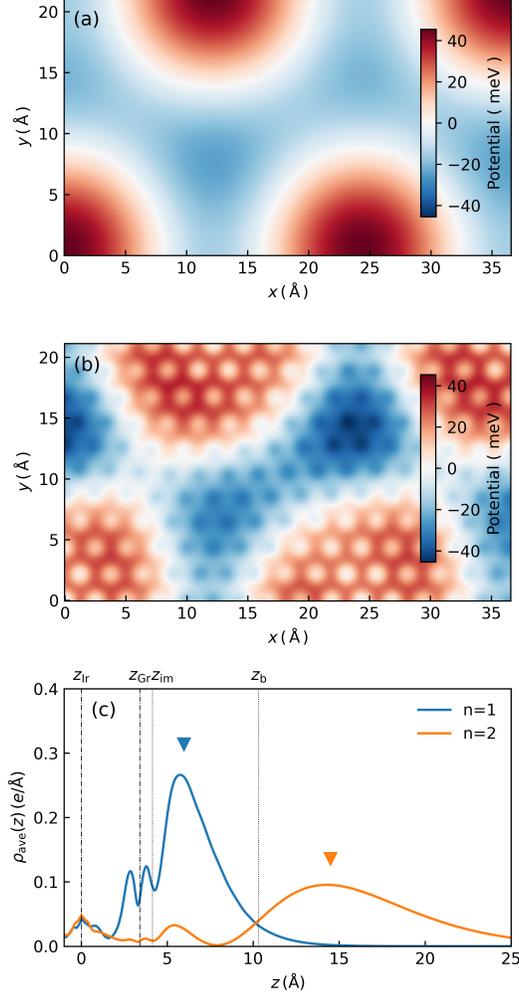


FIG. 4. (a) Contour map of the potential distribution calculated from the nearly free electron model described in the Supplemental Material. (b) Corresponding electrostatic potential distribution at a height of  $z = 6 \text{ \AA}$  above the Ir substrate, obtained from DFT calculations. The qualitative agreement between (a) and (b) supports the validity of the simplified model. (c) Planar-averaged charge density ( $\rho$ ) distribution of IPS ( $n = 1, 2$ ) at the  $\bar{K}$  point of the moiré BZ, which is used to determine the effective height for evaluating the lateral potential distribution. The vertical dash dot line at  $z = 3.40 \text{ \AA}$  indicates the average height of the carbon atoms of graphene. The vertical dot lines at  $z = 4.13 \text{ \AA}$  and at  $z = 10.3 \text{ \AA}$  indicate the height of the image plane ( $z_{im}$ ), and the plane of the embedding surface ( $z_b$ ), respectively. For  $z > z_b$ , we model the potential as the classical image potential. The triangles indicate the height corresponding to the first moment of the charge density distribution for IPS (blue:  $n = 1$ , orange:  $n = 2$ ).

163 Ir(111) surface. It is well accepted that the graphene forms a rippled structure on the  
164 Ir(111) surface [11, 12], and our calculations take this into account. The ripple amplitude  
165 is smaller than that of graphene on the Ru(0001)[15]. As a result, we cannot identify the  
166 energy splitting, even though the energy resolution of our experimental setup was better  
167 than in previous works [16–20]. Nevertheless, the presence of this small ripple structure is  
168 still significant. The periodicity of the rippled structure is identical to that of the moiré  
169 superlattice. Which of the two, then, is fundamentally responsible for the origin of the gap  
170 formation? In this context, we recently have demonstrated that the surface corrugation  
171 caused by the surface reconstruction induces the energy gap of IPS[32]. To answer this  
172 question, we have performed DFT calculations for flat graphene on the Ir(111) surface.  
173 Despite the absence of the rippled structure, an energy gap is still observed in the calculated  
174 band dispersion of IPS, and the magnitude of the gap was essentially identical to that  
175 of the rippled graphene system. This result indicates that the gap formation originates  
176 solely from the geometric moiré structure. Although macroscopic wrinkles may exist due to  
177 thermal expansion mismatch between graphene and Ir[39], these features are non-periodic  
178 and are unlikely to affect the moiré-induced gap observed in our measurements. This is  
179 consistent with the sharp LEED spots across the sample. Beyond confirming the structural  
180 origin of the gap, this result implies that moiré potentials can be used to deliberately tailor  
181 the unoccupied electronic structure of excited states. This establishes a new conceptual  
182 framework for excited-state band engineering using structural moiré design alone, without  
183 relying on external fields or chemical modifications.

184 In conclusion, we have experimentally demonstrated the formation of moiré Bloch bands  
185 with an energy gap in the unoccupied image-potential states of Gr/Ir(111), supported by  
186 DFT calculations and a simple NFE model. The observed energy gap originates solely  
187 from the geometric moiré potential. These findings provide direct evidence that excited-  
188 state electronic bands can be modulated by structural moiré design, establishing a new  
189 approach to excited-state band engineering. This concept opens a pathway toward ultrafast  
190 optoelectronic control in moiré-engineered materials, without requiring chemical doping or  
191 external fields.

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