

Research article

Bulk and surface-scattering loss measurements of CeF₃ crystals at 532 nm via cavity ring down spectroscopy

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ABSTRACT

CeF₃ is a relatively new magneto-optical crystal with a wide transparency window (down to 300 nm) and an outstanding Verdet constant in the UV and visible spectral regions. The high transmittance of this fluoride in the visible was recently demonstrated in cavity ring-down measurements at 532 nm, where bulk losses of no more than 0.004 cm⁻¹ were measured (Xygkis et al., 2023), although the total losses were significantly higher and dominated by surface scattering. Here, we show that reducing surface scattering and improving crystal quality, by suppressing the random formation of hexagonal micro-void defects in the bulk of the crystal which cause bulk scattering, leads to significantly reduced overall losses. Bulk loss coefficients as low as 0.002 cm⁻¹ at 532 nm, half the previously measured value, are achieved in select samples, which is the current state-of-the-art in high-quality CeF₃ single crystals. Further elimination of micro-voids in the bulk is expected to further improve transmittance. Compared to other magneto-optical crystals and glasses, the present CeF₃ crystals achieve the highest values of the *Figure of Merit* (FoM) we have defined for both single-pass and multi-pass (optical cavity) applications.

0. Introduction

Cavity Ring-Down Spectroscopy (CRDS) is widely used for sensitive absorption measurements and is a well-established method for the detection of small optical losses (<1%) in gaseous, liquid, thin-film and transparent bulk samples [1–10], as well as for the measurement of polarimetric [11–18] and ellipsometric angles of samples [19–22]. Recently, our group has used the CRDS technique for the precise and sensitive determination of optical losses in transparent crystals, with an emphasis on evaluating their performance as magneto-optical (M-O) crystals [23], particularly for optical cavity applications.

This technique allows for the evaluation of both uncoated and anti-reflection-(AR)-coated crystals. For non-AR-coated crystals, the alignment is fine-tuned so that the incident light beam is normal to the crystal surfaces, thus ensuring that surface reflections are confined within the cavity and along the beam path, effectively eliminating reflection losses.

Using this method, we have reported measurements on the absorption losses for various M-O crystals and glasses, namely terbium gallium garnet (TGG, Tb₃Ga₅O₁₂), terbium gallium phosphate (TGP, a Tb-based

phosphate glass composed of 20% Tb₂O₃, 15% Ga₂O₃, and 65% P₂O₅), potassium terbium fluoride (KTF, KTb₃F₁₀), fused silica (FS, SiO₂), and cerium fluoride (CeF₃).

To assess the performance of each crystal, a *Figure of Merit* (FoM) was defined, with particular emphasis on multi-pass applications (e.g., optical cavity), which depends on the surface and bulk losses of the crystal (and hence on its length) and its Verdet constant [23]. The conclusion of that study was that CeF₃ exhibited a – very desirable – combination of very low absorption and high Verdet constant [24], but its performance was limited by surface scattering losses. Consequently, for certain applications, particularly those in which short crystal lengths would suffice, other M-O materials (particularly TGP glass) outperformed CeF₃, despite the very low absorption losses of the latter.

In this work, high-quality CeF₃ crystals were grown using an established growth process. Taking extra care with surface preparation and cleaning, we achieved a significant improvement in surface quality: from the previously estimated level of ~0.5%, surface scattering was reduced to ~0.12%, which is on par with the minimum in surface scattering observed across all crystal measurements, even with the highest

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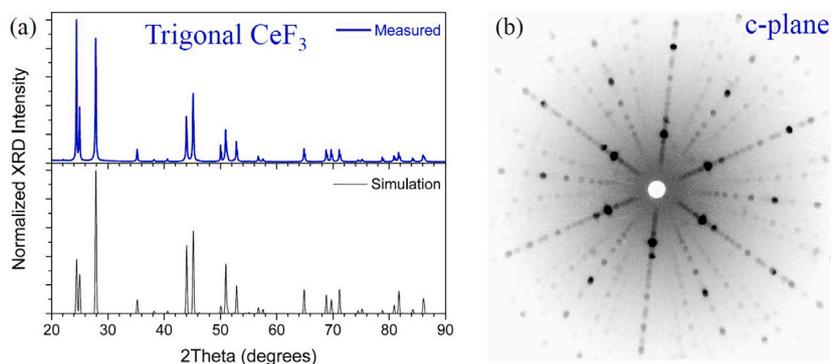


Fig. 1. (a) Powder X-ray diffraction pattern of grown CeF_3 and the trigonal reference ICSD-code #56773. (b) Back-reflection Laue pattern of a c -oriented crystal.

surface quality optics at our disposal, and is probably limited by dust accumulation on the surfaces. Consequently, the total observed optical losses were reduced from 0.7% [23] to 0.16%, still dominated by surface scattering, and followed by bulk losses, which are mainly due to bulk scattering at residual micro-void defects. Thus, we were able to determine that the absorption of CeF_3 is no more than 0.002 cm^{-1} at 532 nm. Further elimination of bulk defect formation during the growth process will lead to even higher transmittance CeF_3 crystals. However, we can already stress that the combination of low surface scattering and low bulk losses make CeF_3 an excellent magneto-optical crystal in the visible. The preparation and characteristics of the CeF_3 crystals are described in detail in Section 1.

To facilitate the comparison among the current and previous CeF_3 crystals, and the other M-O materials, in Section 3 we calculate both the multi-pass-oriented FoM discussed above, as well as the commonly used single-pass M-O FoM [25,26], assuming low to moderate optical power applications where thermal effects can be ignored [27]. In light of these results, we conclude that CeF_3 can be considered the most suitable M-O crystal for both single-pass and multi-pass applications in the visible part of the spectrum (experiments performed at 532 nm), due to its combination of low optical losses and high Verdet constant. We also note that the crystals used in this work, although state-of-the-art, still show scattering (and/or absorption) at defects in the bulk. Therefore, the potential of the CeF_3 material has not been exhausted and further improvements of the CeF_3 properties are expected upon reduction or elimination of the bulk scattering centers.

1. CeF_3 single-crystal discs preparation

A high-quality CeF_3 single crystal was grown by the Bridgman technique as explained in a previous publication [28]. The trigonal phase of grown CeF_3 , with space group $P\text{-}3c1$, was confirmed by X-ray powder diffraction using a Rigaku MiniFlex600 equipped with a Cu-target. The measured pattern is shown in comparison with the simulated one of the database, ICSD-code #56773, in Fig. 1(a).

Since this crystal is uniaxial, it was oriented along the optical axis by back-reflection Laue diffraction (see the 6-fold symmetry in Fig. 1(b)) and cut into thick c -oriented plates of three different thicknesses (with approximate lengths 1, 2, and 5 mm). Subsequently, these were shaped into discs of 8 mm in diameter. After lapping both end surfaces, these were fine processed by chemical–mechanical polishing (CMP) using a 1PM52-1 Logitech precision polishing machine. The surface of polished CeF_3 single crystals was evaluated by coherent scanning interferometry (CSI) using a Hitachi VS1800 Nano 3D optical interferometer. Polishing and surface evaluation were alternatively iterated until the absence of scratches over the whole surface could be confirmed.

Optical-grade polishing of end surfaces is essential to minimize the optical losses caused by surface scattering. As CeF_3 is a non-hygroscopic compound, a standard water-based silica slurry was used for CMP. The quality of CMP polished CeF_3 single crystals evaluated by CSI on the

narrow ($12.8 \times 12.8 \mu\text{m}^2$) and wide ($>8 \text{ mm}^2$, whole surface) ranges is shown in the examples of Fig. 2(a) and (b), respectively. The arithmetic mean roughness, R_a , and the root mean square roughness, R_q , were as small as 2.05 Å and 2.60 Å, respectively, with a peak-to-valley (9.69 Å & -9.86 Å) total roughness, R_t , of 19.55 Å and an average of 0.03 Å. This excellent surface polishing was further confirmed by the complete absence of scratches over the whole surface, despite being a relatively soft fluoride compared to oxides. These results prove that the optical-grade polishing of present CeF_3 is comparable to that of optical-grade fused-silica, and, therefore, their surface losses, S , can be considered as equivalent.

On the other hand, as reflection losses are not evident by naked eye in the case of fused-silica, the 532 nm laser beam scattering observed in the case of CeF_3 in current measurements (see Fig. 5) can be attributed to bulk defects. In general, CeF_3 crystals are well-known to exhibit a milky appearance due to a large density of defects [28], and only high-quality samples, like the present ones, are seemingly scattering-free, as the path of laser beams is barely observable through the bulk of the crystal. Nevertheless, even the latter have been shown to possess a low density of bulk defects, namely flat hexagonal voids in the c -plane [29]. These regularly shaped hexagons are ultra-thin ($\ll \mu\text{m}$), frequently of submicron size and line up, seldom reaching a diameter of several microns, as shown in the optical microscope photographs of Fig. 3. The origin of these micro-voids is attributed to the formation of bubbles in the molten state due to the extraordinarily high vapor pressure of CeF_3 at the melting point (on the order of 10^{-2} atm [30], and evidenced by intense evaporation from the melt), so a growth hot zone with small thermal gradients was targeted to prevent the melt overheating. Large bubbles can move through the low-viscosity melt, leading to intense evaporation. In contrast, smaller ones remain trapped inside the crystal during the solidification process, their shape being determined by the difference in surface tension on different crystal planes. While the appearance of bubbles cannot be avoided at the melting of CeF_3 , the average density of voids is expected to decrease with shallow thermal gradients and reduced overheating. Therefore, it is assumed that the bulk scattering observed in current experiments occurs at these residual voids. This hypothesis is further supported by the fact that observed scattering is inhomogeneous and varies from sample to sample, in good accordance with the random distribution of micro-voids. Since the purpose of the present characterization of CeF_3 using the CRDS technique is to establish an upper limit for the absorption coefficient, a sample with minimal optical losses, *i.e.*, with minimum bulk scattering, was selected.

2. CRDS setup and results

The experimental setup is described in detail in [23]. The optical cavity consists of two high-reflectivity (HR) mirrors, $R_1 = R_2 = R = 0.998$ (Layertec GmbH), and has a length $L_c = 50 \text{ cm}$ (we define the length of a two-mirror cavity as twice the separation between the

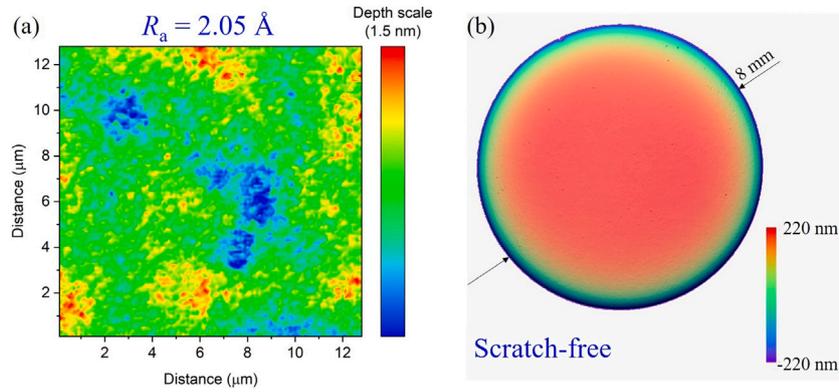


Fig. 2. CSI images of CMP fine-polished CeF₃ - (a) narrow 12.8 × 12.8 μm² range and (b) whole 8 mm in diameter surface.

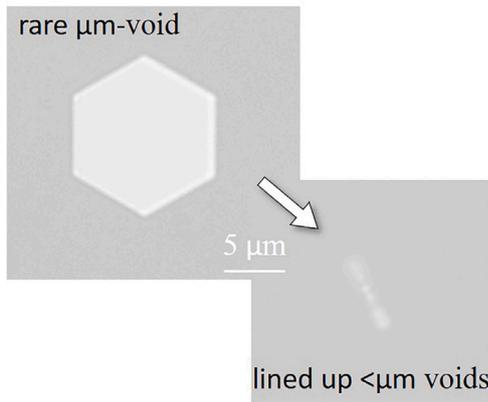


Fig. 3. Optical microscope photographs of scattering centers: a rare large micro-size hexagonal void and common lined up submicron hexagonal voids.

cavity mirrors). The laser source operates at a wavelength $\lambda = 532$ nm (microchip laser, 1.3 ns pulse width, 1 kHz repetition rate, 20 μJ pulse energy). The M-O crystals were placed inside the cavity on a precision optic mount, which allowed micrometric alignment adjustments. The crystals were aligned so that their input/output surfaces were perpendicular to the beam path, ensuring that surface reflections remained confined within the cavity, thus eliminating surface reflection losses (but not surface scattering losses, which cannot be eliminated in this manner).

The single-pass losses of an intracavity crystal sample, L_{s-p} , are determined using standard cavity ring-down theory [1]:

$$L_{s-p} = \frac{\tau_{rt}}{2} \left(\frac{1}{\tau_1} - \frac{1}{\tau_0} \right), \quad (1)$$

where $\tau_{rt} = L_c/c$ is the cavity round-trip time, τ_0 is the ring-down time of the empty cavity, and τ_1 is the ring-down time of the cavity containing the crystal sample. This formula is valid for $L_{s-p} \ll 1$. L_{s-p} has two main contributions: (a) bulk losses (due to absorption and bulk scattering), and (b) surface losses (due to scattering from surface imperfections and/or dust, given that we have eliminated surface reflections, as discussed above). The single-pass losses can also be expressed as:

$$L_{s-p} = 1 - e^{-\kappa d} (1 - S), \quad (2)$$

where d is the crystal length, κ is the bulk loss coefficient (containing both absorption and bulk scattering contributions), and S represents the surface scattering losses. Since pure, single-crystal CeF₃ absorption is expected to be very low in the spectral region under study, κ should be attributed mainly to bulk scattering.

In [23], we first studied optical-grade polished fused silica (FS) crystals, to establish a baseline for surface scattering losses in the case

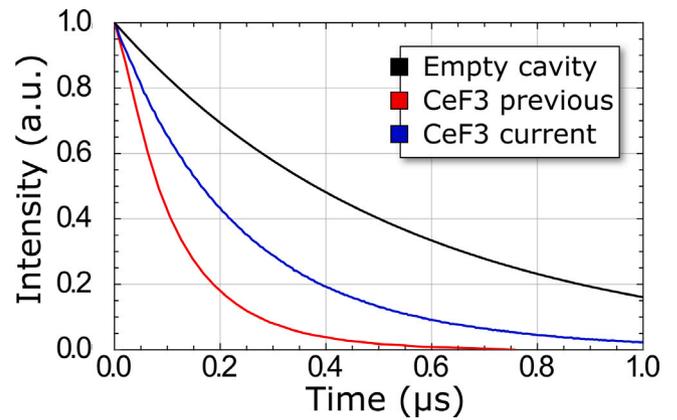


Fig. 4. Ring-down traces for the previous and current CeF₃ crystals at 532 nm. The increased ring-down time of the latter indicates its reduced optical losses (see Section 1).

of minimal bulk absorption. The total FS crystal optical loss was found to be $S = 0.12\%$ per pass, essentially attributed entirely to surface scattering. Indeed, using Eqs. (1) and (2) and $\kappa_{FS} \approx 10^{-5} \text{ cm}^{-1}$ [31], for a $d = 1$ cm fused silica crystal we get $1 - e^{-\kappa d} \approx 10^{-5}$, which is negligible compared to the measured crystal losses. To further verify that measured losses were indeed due to scattering rather than to e.g., misalignment, a thin uncoated BK7 window was placed in the cavity at Brewster's angle. This configuration is much less sensitive to alignment, and measured losses were virtually identical in both cases, confirming that surface scattering was the main source of losses for fused silica and BK7 at 532 nm.

We also measured the losses for two CeF₃ crystals of different lengths (2.2 mm and 6.2 mm) and found no discernible difference in their overall losses per pass, within experimental error. The total per-pass loss was found to be $0.70\% \pm 0.05\%$ for both crystals, and the bulk loss coefficient, $\kappa_{\text{CeF}_3} \leq 0.004 \text{ cm}^{-1}$.

In this work, as described in Section 1, we used a CeF₃ sample with minimal density of bulk defects and entirely scratch-free surface polishing, which showed markedly lower total losses compared to the former, randomly chosen CeF₃ samples. The ring-down traces for the CeF₃ crystals in the two cases are shown in Fig. 4. From the ring-down measurements, the total single-pass loss of the current crystal was found to be $0.16\% \pm 0.05\%$, significantly lower than the previously measured value of $0.70\% \pm 0.05\%$. Having established the high quality of the polished crystal surfaces, we assume its surface scattering losses are comparable to those of fused silica ($S = 0.12\%$, see Section 1), and we calculate the new bulk loss coefficient,

$$\kappa_{\text{CeF}_3} \leq 0.0020 \pm 0.0003 \text{ cm}^{-1} \quad (3)$$

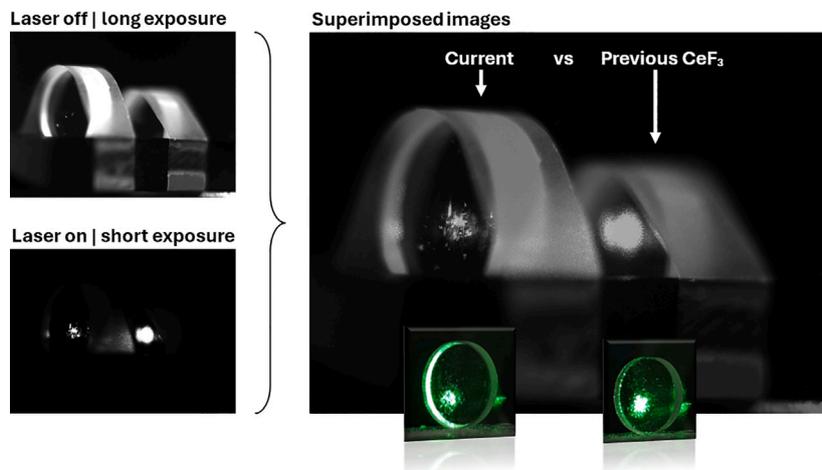


Fig. 5. Scattering of 532 nm light from previous and current CeF₃ crystal samples, under identical experimental conditions. Here, the short exposure image showing the scattering effect is superimposed with a long exposure image taken with the laser off, for better visibility and clarity. The current sample shows notably reduced scattering due to its lower density of bulk defects (see Section 1). Further elimination of residual bulk defects during the growth process will result to even lower optical losses.

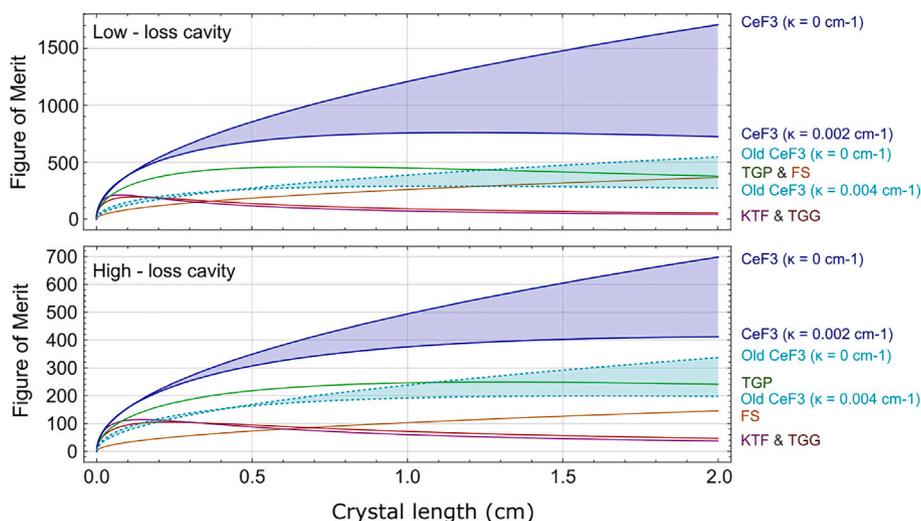


Fig. 6. Figure of Merit for optical cavity applications. **Top:** Low-loss cavity with $T_{IC} = 0.997$ and $R = 0.9995$. **Bottom:** High-loss cavity with $T_{IC} = 0.993$ and $R = 0.9995$. CeF₃ curves are plotted for the lower and upper bounds of the bulk loss coefficient 2σ confidence interval (0 and 0.0020 cm^{-1} , respectively) and for surface scattering losses of $S = 0.120\% - 0.164\%$ per pass (for $\kappa = 0 - 0.0020\text{ cm}^{-1}$ respectively). We note that a minimal value of $\sim 0.12\%$ per pass for surface scattering is common for all crystals under study and is mainly due to small dust particulates settling on the crystal surfaces, and not fundamentally due to the quality of the surface, as the experiments are not performed in a clean room or in vacuum.

3. Discussion

The optical losses and Verdet constants of M-O crystals are critical parameters that determine their suitability for applications such as optical isolation or Cavity Ring-Down Polarimetry (CRDP). In [23] and in this work we focused on CeF₃ crystals, which are of particular interest for applications in the visible part of the spectrum, due to their low absorption losses and high Verdet constant. By using a state-of-the-art growth process and applying high quality surface polishing techniques, we minimized both bulk and surface scattering, and, from the grown crystals, we selected those CeF₃ samples which had the lowest residual bulk defect densities. We measured the total single-pass optical losses of few-mm-long crystals, and we found that, compared to [23], losses were reduced from $0.70\% \pm 0.05\%$, to $0.16\% \pm 0.05\%$ in this work. Thus, a new minimum was established for the value of the bulk loss coefficient of CeF₃: $\kappa_{\text{CeF}_3} = 0.0020 \pm 0.0003\text{ cm}^{-1}$.

To compare sample quality, in Fig. 5 we show pictures of the laser beam scattering on one of the previously used CeF₃ crystals versus

the current one, under identical experimental conditions. Although the improvement is evident and the CeF₃ sample demonstrates very low overall optical losses, it is also clear that visible scattering can still be observed. Given this observation, and considering that absorption of pure CeF₃ is projected to be exceedingly low in the spectral region under study due to the absence of nearby electronic transitions, an even lower loss coefficient than that of Eq. (3) is expected upon reduction or elimination of residual scattering centers.

In Fig. 6, we extend the Figure of Merit (FoM) plot from [23] to include the current CeF₃ crystal results, so that its performance as an intra-cavity M-O element can be compared to the other M-O crystals. We remind here the formula for the FoM, as defined in [23] for multi-pass/intra-cavity applications:

$$\text{FoM} = \frac{(V B d)^{\frac{1}{2}}}{(1 - R T_{IC} e^{-\kappa d} (1 - S))^{\frac{3}{2}}} \quad (\text{multi-pass}) \quad (4)$$

where R is the total reflection coefficient of all cavity mirrors, T_{IC} is the combined transmission coefficient of all intra-cavity optics other

Table 1

Single-pass FoM = V/κ , for the various M–O crystals at 532 nm.

Crystal	V (rad/T m)	κ (m ⁻¹)	FoM (rad/T)
TGG	198	2.89	66.0
TGP	106	0.35	311.8
KTF	107	1.92	55.7
Previous CeF ₃	171	0.40	427.5
Current CeF ₃	171	0.20	855.0

than the crystal, V is the Verdet constant, d the length, and S the scattering losses per pass of the M–O crystal, and B the strength of the magnetic field applied parallel to the light-propagation axis. For more details on the definition of this FoM, the reader is referred to [23]. The FoM is plotted for optical cavity setups with both low and high losses (other than the losses of the M–O crystal). It can be seen that the current CeF₃ crystal outperforms all other M–O crystals by a significant margin, in the spectral region under study, across the whole crystal length range. In particular, CeF₃ surpasses the TGP glass, which in the previous investigation had a comparable FoM, particularly for shorter crystals.

Finally, using the values from [23] for the Verdet constant and absorption coefficient of TGG, TGP, and KTF at 532 nm, we calculate the single-pass FoM commonly quoted for M–O crystals, for single-pass applications [25]:

$$\text{FoM} = \frac{V}{\kappa} \quad (\text{single-pass}) \quad (5)$$

The results are summarized in Table 1. From the calculated values, CeF₃ is confirmed to outperform the other well-known M–O crystals we studied, also for single-pass applications.

Conclusions

We report improved CeF₃ crystals with negligible surface-scattering losses and bulk scattering, and therefore absorption losses of no more than 0.002 cm⁻¹. The reduction in bulk scattering is due to a decrease in micro-voids, which is favored by low thermal gradients and minimum overheating at the molten state. Thanks to these improvements, CeF₃ crystals have the highest figure of merit for magneto-optical crystals in the visible and near UV, both for single-pass and multi-pass (e.g., optical cavity) applications. The present CeF₃ crystals exhibit, to the best of our knowledge, the highest optical quality to date. A further decrease in optical losses implies the elimination of micro-voids, i.e. a suppression of bubble formation. Given the extremely high vapor pressure of CeF₃ at its melting point, growth under high pressure is impractical. Instead, the growth with a flux at a temperature well below the melting point seems a reasonable approach to achieve further improvements in crystalline quality.

CRediT authorship contribution statement

Michail Xygkis: Writing – original draft, Methodology, Investigation, Formal analysis, Data curation. **Encarnación G. Villora:** Writing – review & editing, Resources, Methodology, Investigation, Formal analysis, Data curation, Conceptualization. **George E. Katsoprinakis:** Writing – review & editing, Visualization, Software, Methodology, Formal analysis, Data curation. **Kiyoshi Shimamura:** Writing – review & editing, Resources, Methodology, Investigation, Formal analysis, Data curation. **T. Peter Rakitzis:** Writing – review & editing, Supervision, Project administration, Methodology, Funding acquisition, Conceptualization.

Declaration of competing interest

The authors declare that they have no known competing financial interests or personal relationships that could have appeared to influence the work reported in this paper.

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Data availability

Data will be made available on request.

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