

Quantum oscillations in a dipolar excitonic insulator

Received: 12 January 2025

Accepted: 29 July 2025

Published online: 25 August 2025



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Quantum oscillations in magnetization or resistivity are a defining feature of metals in a magnetic field. The phenomenon is generally not expected in insulators without a Fermi surface. Its observation in Kondo and other correlated insulators provided counterexamples and remains poorly understood. Here we report the observation of resistivity oscillations in a gate-controlled excitonic insulator realized in Coulomb-coupled electron–hole double layers. When the electron or hole cyclotron energy is tuned to exceed the exciton binding energy, recurring transitions arise between the excitonic insulator and layer-decoupled quantum Hall states. Compressibility measurements show an oscillatory exciton binding energy as a function of the magnetic field and electron–hole pair density. Coulomb drag measurements further reveal the signature of finite-angular-momentum excitonic correlations. These findings are qualitatively captured by mean-field calculations. Our study establishes a highly tunable platform based on electron–hole double layers for studying quantum oscillations in correlated insulators.

The observation of quantum oscillations in magnetization or resistivity in insulators^{1–10} has intrigued the condensed-matter physics community because it is long believed that the phenomenon could occur only in metals with a well-defined Fermi surface. Many theoretical proposals have been put forth to explain the observation, including magnetic-field-induced gap oscillations in both single-particle and correlated insulators^{11–22}, competing many-body ground states as a function of the magnetic field^{8,19,21,22} and an exotic fractionalization scenario with neutral fermions and gauge fields^{23,24}. So far, the mechanism responsible for oscillations in different material systems remains under debate, especially for strongly correlated systems. Limits on the ability to control the properties of many of the bulk correlated materials have hindered the development of a cohesive understanding. The emergence of highly tunable correlated insulating states in van der Waals' heterostructures provides an opportunity to study this problem from a fresh perspective.

In this work, we report the observation of quantum oscillations in the resistivity, exciton binding energy and exciton current in a dipolar excitonic insulator (EI)^{25–32}. This is achieved through a suite of magnetotransport, capacitance and drag counterflow measurements performed on Coulomb-coupled MoSe₂/WSe₂ electron–hole double layers. The quantum oscillations originate from recurring transitions between competing EI and layer-decoupled quantum Hall (QH) states as a function of the magnetic field and electron–hole pair density^{19,21,22}. Compared with earlier reports on quantum oscillations in EI candidate InAs/GaSb quantum wells^{6–8,33,34}, the ability to electrically tune and address the electron and hole layers separately has allowed us to establish the emergence of quantum oscillations in an EI.

Electron–hole double layer

Figure 1a shows a schematic of the cross-section of a dual-gated electron–hole double-layer device. The double layer consists of a natural

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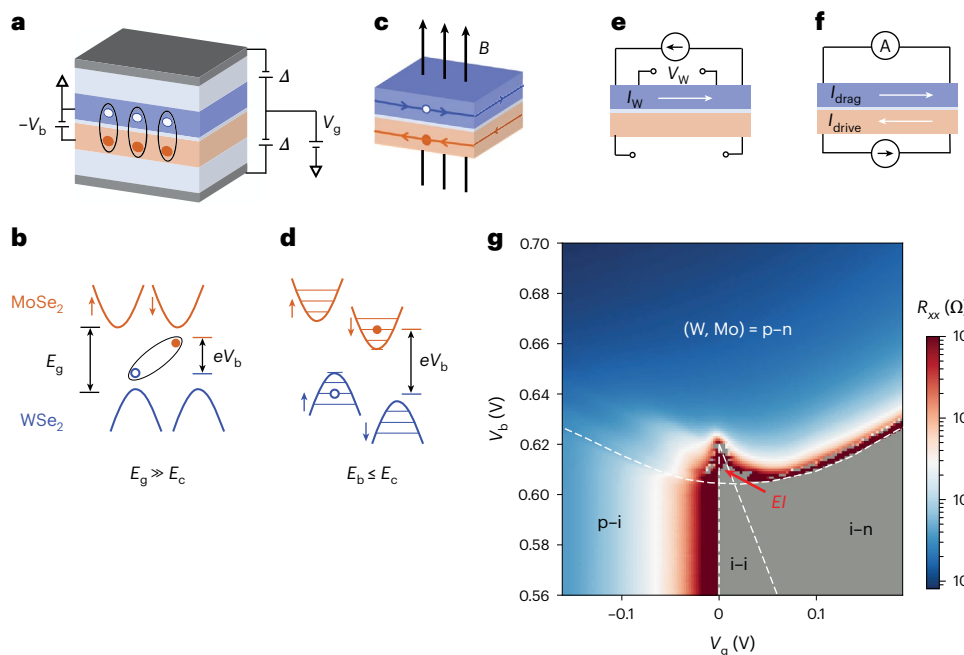


Fig. 1 | Coulomb-coupled MoSe₂/WSe₂ double layer. **a**, Device schematic. Interlayer bias voltage V_b (with the W layer grounded), V_g and Δ control the exciton chemical potential, net charge density and out-of-plane electric field in the double layer, respectively. Interlayer excitons (oval) are stabilized at $B = 0$ T and low electron–hole pair densities. Blue, WSe₂ monolayer; orange, MoSe₂ bilayer; light blue, hBN; grey, graphite. **b**, Band alignment under $B = 0$ T or for the exciton binding energy E_b far exceeding the cyclotron energy E_c (layers not angle aligned). Conduction bands are shown in orange, and valence bands, in blue. Arrows, spin states; dashed lines, Fermi levels. Interlayer excitons spontaneously form when E_b exceeds the effective charge gap ($E_g - eV_b$). **c**, Same data as **a** but for high magnetic fields and high pair densities. Layer-decoupled QH states with

counterpropagating electron and hole chiral edge states emerge. **d**, Same data as **b** but for $E_b \leq E_c$. Electron and hole LLs (horizontal solid lines) are spin-split by the Zeeman effect. **e, f**, Schematic of the open-circuit measurements of R_{xx} and R_{xy} in the W layer (**e**) and drag counterflow measurements (**f**), where I_W and V_W in **e** denote the current and induced voltage, respectively, and I_{drive} and I_{drag} in **f** are the drive current in the Mo layer and the induced drag current in the W layer, respectively. **g**, R_{xx} as a function of V_g and V_b at $B = 0$ T and $T = 1.5$ K. The dashed lines separate the EI and different doping regions with i, p and n, denoting the intrinsic, hole-doped and electron-doped layers, respectively. In the grey area, R_{xx} diverges and cannot be reliably determined.

MoSe₂ bilayer and a WSe₂ monolayer separated by a thin hexagonal boron nitride (hBN) barrier (5–6 layers thick; Extended Data Fig. 1; the MoSe₂ bilayer is more robust for fabrication but behaves practically like a monolayer because electrons are polarized to one layer under a high perpendicular electric field in this study). The MoSe₂/WSe₂ heterobilayer has a type-II band alignment^{26–30,32} (Fig. 1b), with the conduction (valence) band minimum (maximum) residing in the Mo layer (W layer). The two gates allow for independent control of the net electron doping density (n) in the double layer and the electric field (E) perpendicular to the sample plane through the symmetric (V_g) and antisymmetric (Δ) parts of the two gate voltages (for symmetric gates), respectively. We apply a constant electric field to reduce the heterobilayer energy gap (from $E_g \approx 1.6$ eV (refs. 27,29,32) to $E_g \approx 0.625$ eV in device 1). We also apply a bias voltage (V_b) between the Mo and W layers to separate the electron and hole Fermi levels. When the effective charge gap of the double layer ($E_g - eV_b$) becomes smaller than the interlayer exciton binding energy (E_b), the double layer is spontaneously populated by interlayer excitons, forming an EI with a net electric polarization^{35–38} (that is, a dipolar EI). Here e is the elementary charge. The electrons in the Mo layer and holes in the W layer are coupled only through the interlayer Coulomb interactions. With negligible single-particle interlayer tunnelling (verified by negligible interlayer tunnelling currents (Extended Data Fig. 2)), the excitons in the double layers are in thermal equilibrium with an exciton chemical potential ($eV_b - E_g$). Note that the EI here refers only to a charge insulating state and does not imply spontaneous interlayer coherence.

In the presence of a strong perpendicular magnetic field B , Landau levels (LLs) emerge in the electron and hole layers (Fig. 1c,d). When the electron–hole pair density (n_p) exceeds the exciton Mott density

(n_M), the excitons dissociate into an electron–hole plasma^{27,29,35,36}, and layer-decoupled QH states are expected. On the other hand, for low pair densities and low magnetic fields, when the electron–hole cyclotron energy (E_c) is comparable to E_b , EI is expected to dominate (the electron and hole cyclotron energies are comparable in MoSe₂/WSe₂). In the interesting regime of $n_p \approx n_M$ and $E_c \approx E_b$, it was suggested in refs. 21,22 that recurring transitions between the EI and layer-decoupled QH states could emerge as a function of n_p and B . Unlike the interlayer-coherent exciton condensates in half-filled LLs in electron–electron or hole–hole Coulomb-coupled bilayers^{39–43}, in which the condensates carry chiral edge states (that is, they are QH ferromagnets) and are unstable in the zero-field limit²¹, the EI in the electron–hole double layers is stable in the zero-field limit and does not support chiral edge states because interlayer coherence is expected to gap out the counterpropagating edge states^{21,22}.

We probe the double layer under finite magnetic fields by patterning it into a Hall bar device with independent electrical contacts to the Mo and W layers. Because the electron contacts formed via bismuth evaporation in the Mo layer are less reliable, we measure the four-terminal longitudinal (R_{xx}) and Hall (R_{xy}) resistances in the W layer and keep the Mo layer in the open-circuit condition (Fig. 1e and Extended Data Fig. 3). As demonstrated by a recent study³², R_{xx} and R_{xy} are highly sensitive to interlayer Coulomb interactions. This measurement is supplemented by the drag counterflow measurement (Fig. 1f), which has been shown to directly probe the interlayer Coulomb interactions^{29,30,41} and the penetration capacitance measurement²⁷, which accesses the exciton binding energy in the EI^{27,38}. Methods provides details on the device fabrication and electrical transport and capacitance measurements. Unless otherwise specified, the sample temperature is $T = 1.5$ K.

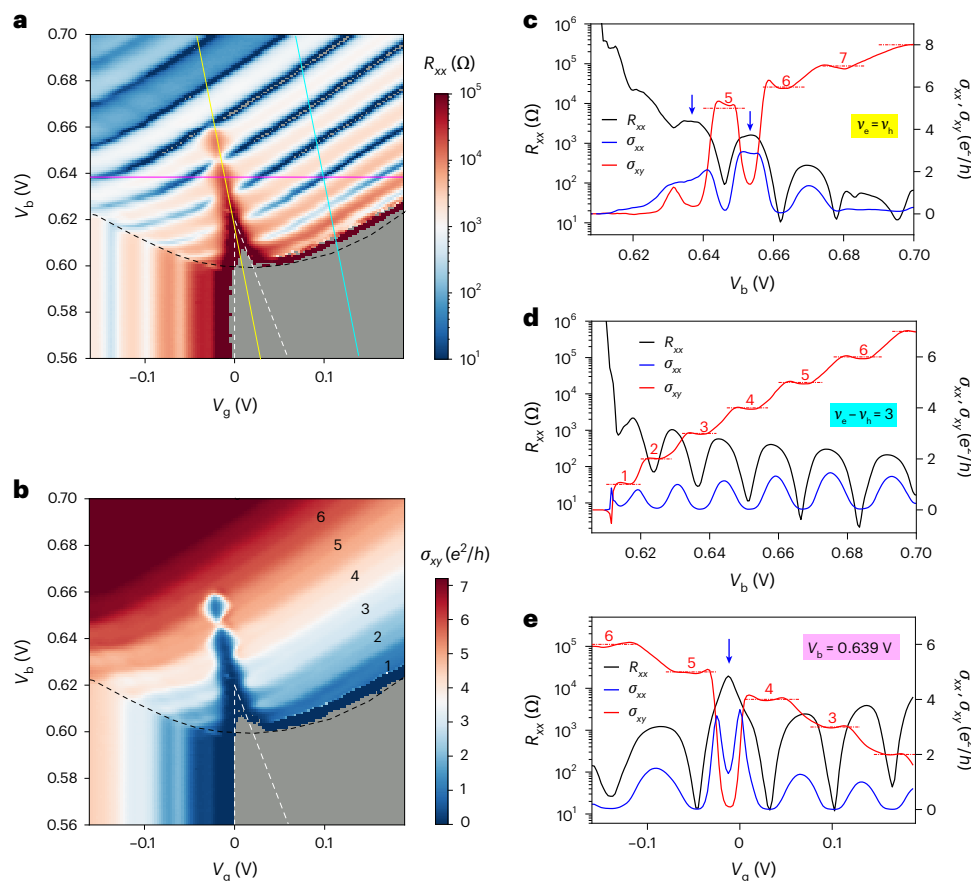


Fig. 2 | Quantum oscillations in the EI phase. **a, b**, R_{xx} (**a**) and σ_{xy} (**b**) of the W layer (with the Mo layer in the open-circuit configuration) as a function of V_g and V_b at $B = 12$ T and $T = 1.5$ K. The black and white dashed lines are the phase boundaries from the data for $B = 0$ in Fig. 1a. The EI phase is shifted and expanded by the magnetic field. Quantized $\sigma_{xy} = \frac{v_h e^2}{h}$ for $v_h = 1-6$ is identified in **b**. In the grey area,

R_{xx} and σ_{xy} cannot be reliably measured because of the diverging R_{xx} . **c-e**, R_{xx} (left axis) and σ_{xx} and σ_{xy} (right axis) along the solid yellow (**c**), cyan (**d**) and purple (**e**) lines in **a**. The QH states are characterized by R_{xx} and σ_{xx} dips and quantized σ_{xy} (horizontal dashed lines). The EI states are characterized by R_{xx} peaks and suppressed σ_{xx} and σ_{xy} . Blue arrows identify strong EI states between two integer QH states.

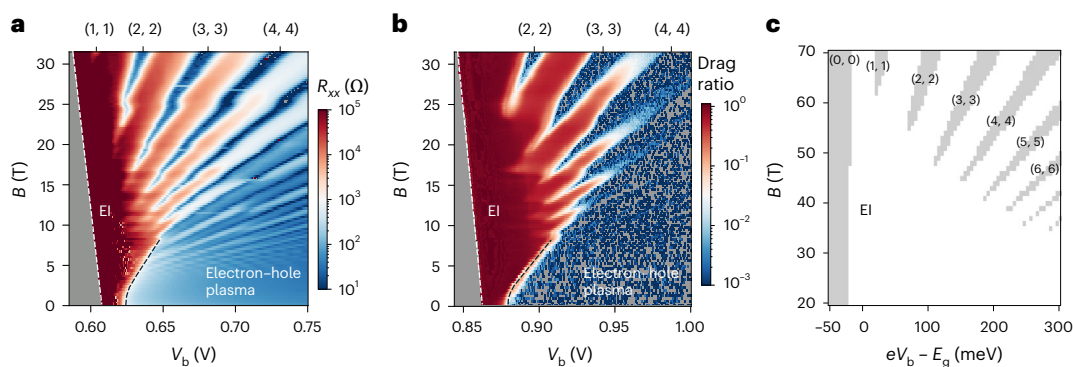


Fig. 3 | Magnetic-field phase diagram at charge neutrality. **a, b**, R_{xx} of the W layer (device 1; **a**) and drag ratio $\frac{I_{\text{drag}}}{I_{\text{drive}}}$ (device 3; **b**) as a function of V_b and B at charge neutrality and $T = 0.3$ K. The white dashed line denotes the band edge, and the black dashed line separates the EI and the electron-hole plasma phases. In the grey area (left of the white line), R_{xx} diverges and cannot be reliably measured. The EI phase

with diverging R_{xx} and large $\frac{I_{\text{drag}}}{I_{\text{drive}}}$ expands with the magnetic field. The fully filled LLs with vanishing R_{xx} and $\frac{I_{\text{drag}}}{I_{\text{drive}}}$ and $(v_e, v_h) = (1, 1), (2, 2), (3, 3), (4, 4)$ protrude into the EI phase. **c**, Mean-field phase diagram in exciton chemical potential ($eV_b - E_g$) and B at charge neutrality (Methods). White region, EI; grey, layer-decoupled QH states.

Resistivity oscillations in EI

Figure 1g shows R_{xx} of the W layer as a function of V_g and V_b at $B = 0$ T (device 1), where the gate voltage V_g tunes the net doping density n in the double layer and the bias voltage V_b mainly controls the electron-hole

pair density n_p (ref. 27). The electrostatic phase diagram shows i-i, i-n, p-i and p-n regions for the (W, Mo) layers, where i, p and n denote an intrinsic (or charge-neutral), hole-doped and electron-doped layer, respectively. As expected, R_{xx} diverges at low temperature in the i-i

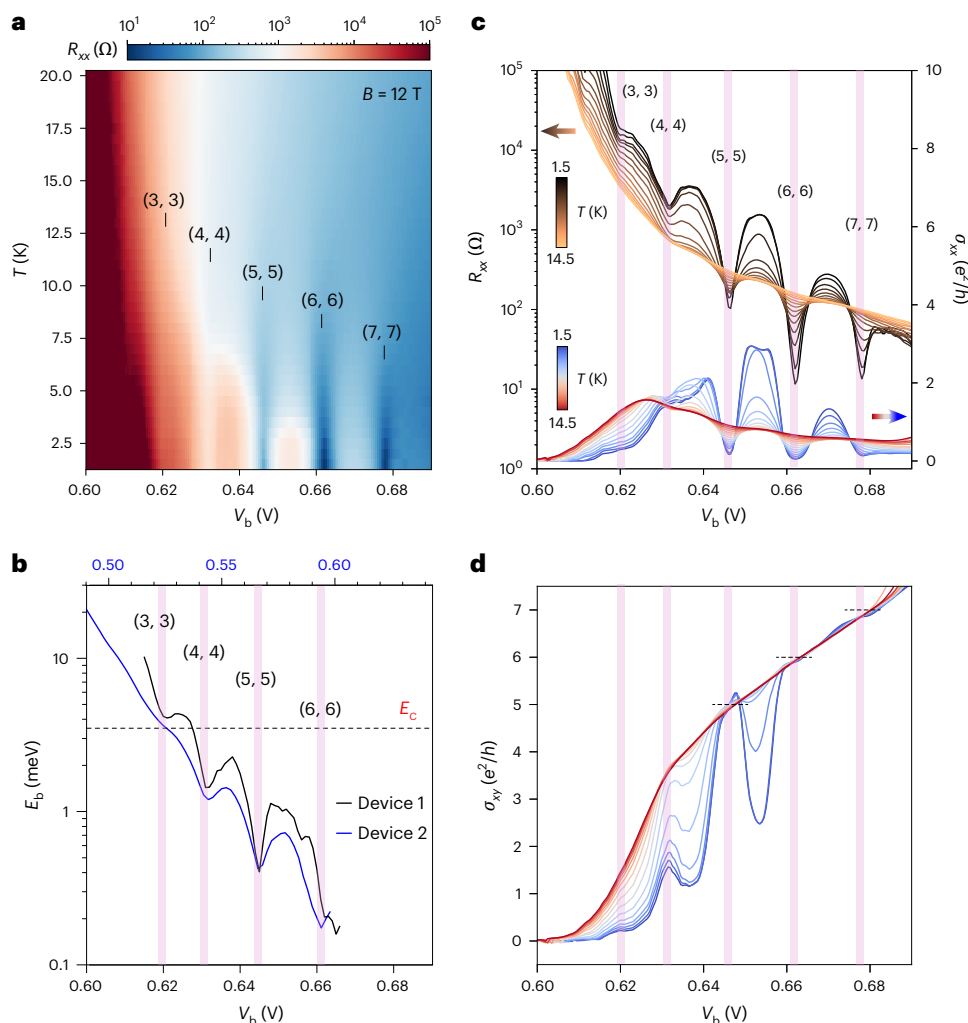


Fig. 4 | Oscillating exciton binding energy ($B = 12$ T). **a**, R_{xx} of the W layer as a function of V_b and T at charge neutrality. **b**, Exciton binding energy as a function of V_b (bottom axis for device 1 and top axis for device 2). It oscillates on a monotonically decreasing background. The horizontal dashed line marks the cyclotron energy E_c (comparable for electrons and holes). **c**, R_{xx} (left axis; **c**), σ_{xx} (right axis; **c**) and σ_{xy} (**d**) versus V_b at varying temperatures (1.5 K to 14.5 K

in 1-K step) for device 1. The dashed lines in **d** denote the quantized values. As V_b increases, the EI state (with increasing R_{xx} and decreasing σ_{xx} and σ_{xy}) transitions into the QH states (with decreasing R_{xx} and σ_{xx} and quantized σ_{xy}) at low temperatures. The fully filled LLs (ν_e and ν_h) are labelled in **a** and denoted by the vertical purple lines in **b–d**.

and i–n regions (grey shaded); the W layer is conducting only in the p–i and p–n regions (the p–i|i–i boundary is pinned to $V_g = 0$ because the W layer is grounded). R_{xx} also diverges in the EI region (the triangular i–i region that protrudes into the p–n region), in which a hole current in the W layer is not allowed because the electrons and holes are bound and the electron layer is in the open-circuit condition³². At the tip of the EI triangle, the pair density reaches the exciton Mott density, and the interlayer excitons dissociate into an electron–hole plasma^{27,29}. The results are fully consistent with earlier studies^{27,29,32}.

Next, we examine R_{xx} and σ_{xy} (Hall conductivity) as a function of V_g and V_b at $B = 12$ T (Fig. 2a,b). Results at other magnetic fields up to 31.5 T are shown in Extended Data Fig. 4. Hole LLs are observed in the p–i and p–n regions. Each fully filled LL is characterized by an R_{xx} dip and a nearly quantized σ_{xy} at $\frac{\nu_h e^2}{2\pi h}$ (see the line cuts in Fig. 2d). Here $V_{b(e)}$ is the hole (electron) LL filling factor and \hbar is the reduced Planck constant. In the p–i region, the hole LLs form vertical stripes because the hole density is independent of V_b . In the p–n region, they form diagonal stripes because the doping density in the W layer (and the Mo layer) changes with both V_g and V_b . The electron LLs in the Mo layer are

nearly invisible in R_{xx} and σ_{xy} of the W layer; they are better resolved in the drag counterflow (Fig. 5) and capacitance (Extended Data Fig. 5) measurements.

The most interesting features in the R_{xx} and σ_{xy} maps are located near the EI triangle of the phase diagram. At the bottom of the triangle ($0.60 \lesssim V_b \lesssim 0.64$ V), where the exciton binding energy is large, the diagonal LL stripes are interrupted by the EI with diverging R_{xx} and vanishing σ_{xy} (only at the highest magnetic fields (Extended Data Fig. 4), the LL stripes penetrate through the EI). Near the tip of the triangle ($0.64 \lesssim V_b \lesssim 0.66$ V), where the exciton binding energy is small, a fully filled LL can nearly penetrate through the EI without interruption even under moderate magnetic fields; on the other hand, a half-filled LL (one with an R_{xx} peak) transitions to the EI with much higher R_{xx} and strongly suppressed σ_{xy} .

Figure 2c–e shows three representative line cuts along the solid lines shown in the maps (the extracted longitudinal conductivity σ_{xx} is also included). Only a series of QH states are observed away from charge neutrality at $\nu_e = \nu_h = 3$ (Fig. 2d). At charge neutrality (Fig. 2c), the transition from the $\nu_h = 6$ QH state ($V_b \approx 0.662$ V) to the $\nu_h = 5$ QH state ($V_b \approx 0.645$ V) is interrupted by a weak EI near $V_b \approx 0.653$ V; it shows

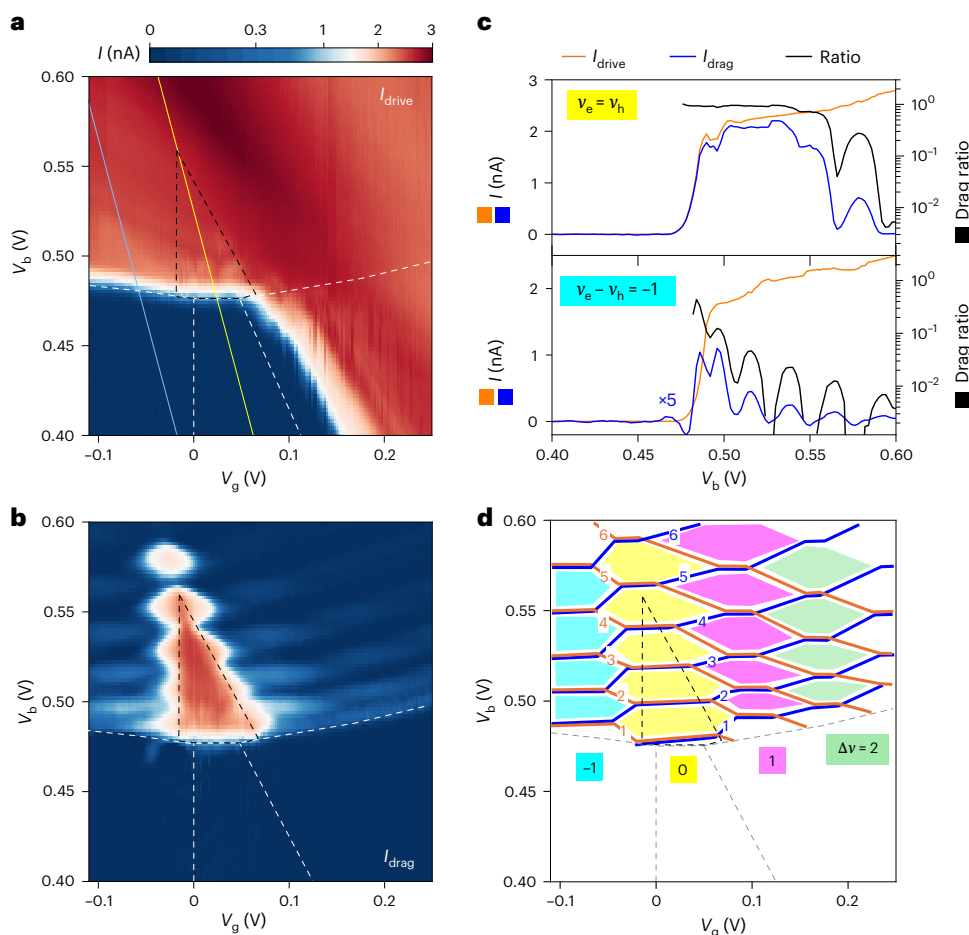


Fig. 5 | Finite-angular-momentum excitonic correlations. **a, b**, Drive current (I_{drive}) in the Mo layer (**a**) and drag current (I_{drag}) in the W layer (**b**) as a function of V_g and V_b at $B = 12$ T and $T = 1.5$ K. Near-perfect Coulomb drag is observed in the EI region shown schematically by the black dashed lines (weaker states above the triangle are not included at this temperature). Substantial Coulomb drag is also observed outside the EI region with partially filled LLs, indicating the presence of excitonic correlations with finite angular momentum. **c**, Line cuts in **a** and **b** (left axis) and drag ratio $I_{\text{drag}}/I_{\text{drive}}$ (right axis) along the solid yellow line with $v_e = v_h$ (top)

and cyan line with $v_e - v_h = -1$ (bottom) in **a**. An enhanced drag ratio indicates stronger interlayer excitonic interactions. The layer-decoupled QH states exhibit a substantial drop in the drag ratio. **d**, Phase diagram for the QH states in each layer (orange and blue lines for the Mo and W layers, respectively) constructed from **b** (see the main text). The regions with $\Delta v = v_e - v_h = -1, 0, 1$ and 2 are shaded in cyan, yellow, purple and green, respectively. The EI state dominates the $\Delta v = 0$ region. The dashed lines in **a**, **b** and **d** denote the boundaries of different doping regions from electrostatics and the EI from Coulomb drag.

enhanced R_{xx} and suppressed σ_{xy} and σ_{xx} (on top of the wide peak). Only the EIs with diverging R_{xx} and vanishing σ_{xx} and σ_{xy} are stable ($V_b \lesssim 0.64$ V). In Fig. 2e, an EI with a sharp dip in σ_{xx} near $V_g \approx -0.01$ V, which interrupts the transition from the $v_h = 5$ QH state ($V_g \approx -0.05$ V) to the $v_h = 4$ QH state ($V_g \approx 0.03$ V), is also illustrated by a line cut at constant $V_b \approx 0.64$ V.

We examine the magnetic-field dependence of R_{xx} at charge neutrality in Fig. 3a (along the yellow solid line (Fig. 2a)) up to $B = 31.5$ T at 0.3 K. With increasing field, the EI region expands. On one hand, the exciton Mott transition or the metal–insulator transition (black dashed line) moves to higher V_b in a hyperbolic fashion due to exciton diamagnetic shift⁴⁴. On the other hand, the onset for exciton injection (white dashed line) shifts linearly to lower V_b due to the exciton Zeeman effect. We obtain an interlayer exciton g -factor of -20 , in agreement with earlier optical studies⁴⁵. LLs emerge in the electron–hole plasma region for $B \gtrsim 3$ T. They disperse with V_b slightly nonlinearly because the interlayer capacitance depends on V_b (ref. 27). At high fields, the EI phase with large R_{xx} is interrupted by LLs with R_{xx} dips ($v_e = v_h = 1, 2, 3$ and 4). The onset field for the LLs decreases with increasing v_e or v_h . The distinct horizontal stripes in the phase diagram are caused by the LLs in the graphite gates, which are capacitively coupled to the

electron–hole double layer^{9,10}; they are independent of V_b because the W layer is grounded.

We further study the temperature dependence of the quantum oscillations at constant $B = 12$ T. Figure 4a shows R_{xx} as a function of V_b and temperature. Figure 4c displays line cuts at the representative temperatures. Figure 4c,d also includes σ_{xx} and σ_{xy} (Extended Data Fig. 6 shows additional data). Recurring transitions between the EI and QH states are observed as V_b increases. As the temperature decreases, R_{xx} increases, and σ_{xx} and σ_{xy} decrease for the EI states; R_{xx} and σ_{xx} decrease, and σ_{xy} approaches a quantized value for the QH states. At the boundary separating the two states, these quantities are nearly temperature independent. The temperature dependence of the oscillation amplitude of R_{xx} is analysed in Extended Data Fig. 7. It follows the Lifshitz–Kosevich formula for the QH states and substantially deviates from this formula for the EI states. Quantum oscillations are also observed in the penetration capacitance, from which we extract the exciton binding energy as a function of V_b (Methods and Extended Data Fig. 5). The results from two different devices (devices 1 and 2) in Fig. 4b are similar. The binding energy oscillates as a function of V_b on a monotonic decreasing background; the local minimum corresponds to a QH state.

The results above demonstrate transitions tuned by the magnetic field and pair density (controlled by V_b) between the EI and QH states, which give rise to the observed quantum oscillations in the EI region of the phase diagram. E_b decreases continuously with pair density due to screening^{27,29,46}, whereas E_c increases with B . When E_b becomes comparable to or smaller than E_c , the EI transitions to layer-decoupled QH states when both layers are in the fully filled LLs^{21,22}. The EI phase returns when the LLs are partially filled until the pair density exceeds the Mott density. Beyond the Mott density, excitons dissociate into an electron–hole plasma and only layer-decoupled LLs are present. In this picture, the frequency of the quantum oscillations in $1/B$ is set by the size of the electron–hole Fermi surface (Extended Data Fig. 8).

We perform mean-field calculations for the ground-state energy density of the electron–hole double layer²¹ to compare with experiment (Methods). The theoretical phase diagram (Fig. 3c) qualitatively captures the experimental phase diagram (Fig. 3a). A fan of layer-decoupled QH states at integer $\nu_e (= \nu_h)$ merges at high magnetic fields, and their onset field decreases with increasing ν_e or ν_h . However, the scale of the magnetic field in the mean-field result is substantially higher because the density-dependent exciton binding energy due to screening and the associated exciton Mott transition have not been taken into account. Future studies including these effects are required to quantitatively describe the experimental results.

Quantum oscillations in Coulomb drag

Finally, we perform the drag counterflow measurements to further examine the EI-to-QH transitions. We drive an a.c. bias current (I_{drive}) in the Mo layer and measure the drag current (I_{drag}) in the W layer²⁹ (Fig. 1f), keeping interlayer tunnelling negligible (Extended Data Fig. 3). The drag ratio $\frac{I_{\text{drag}}}{I_{\text{drive}}}$ at low temperature, as shown for device 3 in Fig. 3b, provides a measure for the interlayer Coulomb coupling²⁹. In particular, near-perfect Coulomb drag ($\frac{I_{\text{drag}}}{I_{\text{drive}}} \approx 1$) is observed for the EI phase; near-zero drag is observed for the layer-decoupled QH states ($\nu_e = \nu_h = 2, 3$ and 4) and the electron–hole plasma. The results are fully consistent with the phase diagram inferred from R_{xx} in Fig. 3a.

We further examine Coulomb drag in the presence of an electron–hole density imbalance. Figure 5a,b shows I_{drive} and I_{drag} in the Mo and W layers, respectively, as a function of V_g and V_b for device 2 at $B = 12$ T. The Mo layer is turned on electrically only in the i–n and p–n regions. A drag current in the W layer with nearly identical magnitude but opposite sign with respect to I_{drive} is observed in the triangular EI region. Quantum oscillations are observed in I_{drag} near the EI phase boundary and beyond. Figure 5c shows line cuts for the currents together with their ratio along the $\nu_e = \nu_h$ and $\nu_e - \nu_h = -1$ lines (yellow and blue, respectively; Fig. 5a). Near-perfect Coulomb drag is observed at $\nu_e = \nu_h$ for $V_b \lesssim 0.55$ V; the drag ratio drops sharply and exhibits quantum oscillations with increasing V_b . A large but imperfect drag (with ratio up to about 0.5) is observed at $\nu_e - \nu_h = -1$ near the onset of electron–hole injection; the drag ratio also drops sharply and shows quantum oscillations with increasing V_b .

We construct a phase diagram in V_g and V_b for layer-decoupled QH states (ν_e, ν_h) by tracing zero drag (Fig. 5d). The regions with $\nu_e - \nu_h = -1, 0, 1$ and 2 are shaded. The EI with near-perfect Coulomb drag dominates the $\nu_e = \nu_h$ region, except that near the tip of the triangle with $\nu_e - \nu_h = 4, 5$ and 6. The presence of substantial Coulomb drag (with ratio up to about 0.5) at partially filled LLs in the $\nu_e - \nu_h = -1, 1$ and 2 regions suggests the presence of interlayer excitonic correlations with angular momentum quantum of $-\hbar, \hbar$ and $2\hbar$, respectively²¹. The result suggests a tendency to stabilize EIs with finite-angular-momentum excitons, as suggested by mean-field calculations²⁴. However, the imperfect Coulomb drag shows the presence of ionized electrons and holes possibly from thermal and/or quantum fluctuations. Further studies under higher magnetic fields and/or with stronger excitonic binding are required to fully establish the finite-angular-momentum EIs.

Conclusion

We observe resistivity and Coulomb drag quantum oscillations in a dipolar EI based on Coulomb-coupled MoSe₂/WSe₂ electron–hole double layers. The oscillations originate from phase transitions between the competing EI and layer-decoupled QH states^{21,22}. Our results demonstrate a highly tunable platform for studying quantum oscillations in correlated insulators and pave the way for explorations in several directions. To name a couple, the finite-angular-momentum excitonic correlations present a possibility to realize the QH effect for excitons. Studying how the collective excitations in the EI would evolve in a phase transition from the EI to QH states, in which there are only single-particle excitations, will provide insights into the nature of the phase transition.

Online content

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Methods

Device design and fabrication

The device and contact geometry have been described in refs. 27,29,32. The optical images of devices 1 and 2 are shown in Extended Data Fig. 1a,b, respectively. The top and bottom graphite gates are outlined by the dashed and solid red lines, respectively. The WSe₂ monolayer (green) and MoSe₂ bilayer (blue) are separated by a thin hBN barrier (1.5–2 nm) in the transport channel (shaded red) and by a thick hBN barrier (10 nm) in the exciton contact regions (shaded pink). A natural MoSe₂ bilayer is chosen because it does not crack as easily as a monolayer during the fabrication process. Under a high perpendicular electric field as used in this study, electrons in the bilayer are polarized to one layer and the bilayer functions effectively as a monolayer. To achieve high doping densities at the metal–semiconductor contacts for ohmic contacts at low temperatures, Pt–WSe₂ contacts are gated only by the top gate; similarly, Bi–MoSe₂ contacts are gated only by the bottom gate. During the measurements, Δ was maintained constant (3 V for device 1 and 5.5 V for device 2). Here $\Delta \equiv \frac{V_{\text{tg}} - V_{\text{bg}}}{2}$ is the antisymmetric part of the top- and bottom-gate voltages V_{tg} and V_{bg} , respectively; it is proportional to the perpendicular electric field (the symmetric part of the gate voltages, $V_g \equiv \frac{V_{\text{tg}} + V_{\text{bg}}}{2}$, controls the net charge density in the channel).

The devices were fabricated by the layer-by-layer dry transfer method^{27,29,32,47}. In short, all the individual layers were first exfoliated by Scotch tape onto 285-nm SiO₂/Si substrates and screened by an optical microscope for appropriate thickness and geometry before stacking. Layers were picked up sequentially using a polymer stamp made of a thin layer of polycarbonate on a polypropylene-carbonate-coated polydimethylsiloxane block. The completed stack was released onto pre-patterned Pt electrodes on SiO₂/Si substrates to form contacts to the W layer and to the gate electrodes. The polymer residue was removed using chloroform and isopropanol. Next, separate contacts for the W layer were defined by etching the top graphite electrode using electron-beam lithography patterning (Nabity) and oxygen plasma reactive ion etching (Oxford PlasmaLab 80 Plus). Finally, contacts to the Mo layer were fabricated by another electron-beam lithography patterning followed by Bi evaporation in a thermal evaporator⁴⁸. The main results have been reproduced in three devices. Extended Data Fig. 9 shows additional data from device 3.

Electrical measurements

The transport properties of the electron–hole double layers were examined using two measurement configurations: the open-circuit R_{xx} and R_{xy} measurements (Fig. 1e) and the drag counterflow measurement (Fig. 1f), which reflect the charge and exciton transport properties, respectively^{29,32}. Extended Data Fig. 2a,b shows the corresponding circuit diagrams. In the open-circuit geometry (device 1; Figs. 1–3), the Mo layer is kept in the open-circuit configuration, that is, no electron current (and, therefore, no exciton current) can flow; four-terminal R_{xx} and R_{xy} measurements are performed on the W layer using the standard lock-in technique. Here R_{xx} and R_{xy} measure the transport properties of the unbound holes in the W layer³². There are a total of eight contacts in the W layer defined by the etched top graphite gate (pins 1–8). To obtain R_{xx} , a small a.c. bias voltage of 0.15 mV (root mean square (r.m.s.)) was applied between pins 2 and 6 at 11.33 Hz, and the bias current out of pin 6 and the longitudinal voltage drop between pins 1 and 5 were measured simultaneously. To obtain R_{xy} , a small a.c. bias voltage of 0.15 mV (r.m.s.) was applied between pins 1 and 4 at 11.33 Hz, and the bias current out of pin 4 and the voltage drop between pins 2 and 6 were measured simultaneously. Other longitudinal and Hall measurement configurations gave similar results.

In the drag counterflow geometry (devices 2 and 3; Figs. 3 and 4), both layers are kept in the closed-circuit configuration so that excitons can flow in the transport channel. An a.c. bias current is driven in the

Mo layer and the drag current is measured in the W layer (Fig. 1f). The drag ratio $\frac{I_{\text{drag}}}{I_{\text{drive}}}$ at low temperature reflects the exciton population fraction in the system²⁹. In particular, $\frac{I_{\text{drag}}}{I_{\text{drive}}} = 1$ and 0 correspond to pure exciton and pure charge transport, respectively. An a.c. bias voltage of 10 mV (r.m.s.) at 7.33 Hz was applied to the Mo layer through a 1:1 voltage transformer. The voltage transformer was connected to a 10-k Ω potentiometer to distribute the a.c. voltage on the two ends of the Mo layer; this step minimized the a.c. coupling between the Mo and W layers^{42,43}. The d.c. interlayer bias voltage V_b was applied to the middle of the potentiometer; this kept both contacts in the Mo layer at the same d.c. potential and maintained a 10-mV a.c. voltage drop between them²⁹. The drive current I_{drive} was measured by monitoring the voltage drop across a 150-k Ω resistor connected in series with the Mo layer; the drag current I_{drag} was measured by an ammeter connected in series with the W layer.

All the electrical measurements were carried out in a closed-cycle ⁴He cryostat (Oxford TeslatronPT) with temperature down to 1.5 K and magnetic field up to 12 T. All the currents and voltages were measured by lock-in amplifiers (Stanford Research Systems SR830 and SR860). In the voltage measurements, the signals were first sent to a preamplifier (Ithaco DL1201) with an input impedance of 100 M Ω before being measured by the lock-in amplifier. The measurement results are largely independent of the excitation amplitude (3–20 mV) and frequency (7–37 Hz).

Capacitance measurements

Details of the capacitance measurements have been described in ref. 27. The penetration capacitance (C_p) of the dual-gated devices 1 and 2 was measured under $B = 12$ T by applying an a.c. bias voltage of 5 mV (r.m.s.) at 737 Hz to the top gate and measuring the induced charge carrier density on the bottom gate by a GaAs high-electron-mobility transistor through a low-temperature capacitance bridge⁴⁹. The resulting C_p as a function of V_g and V_b is shown in Extended Data Fig. 5. The exciton binding energy for each V_b (Fig. 4c) was obtained by integrating the normalized C_p with respect to V_g over a small window centred at charge neutrality, $E_b \approx \int (C_p/C_{\text{gg}}) dV_g$, where C_{gg} is the gate-to-gate geometrical capacitance²⁷.

Mean-field calculations

To obtain the phase diagram shown in Fig. 3c, we performed mean-field calculations using the self-consistent Hartree–Fock approximation described in ref. 21, and assumed a uniform carrier distribution in our solutions. The single-particle part of the Hamiltonian consists of LLs from the two semiconductor layers; for simplicity, we assumed equal electron and hole cyclotron energies (a good approximation given the similar electron and hole masses of $\sim 0.4m_0$, where m_0 is the free electron mass). The LL energy in the conduction (valence) band increases (decreases) with the level index. The bias voltage V_b controls the effective energy difference between the conduction band minimum and the valence band maximum. We considered the screening effects from the gate electrodes on both intralayer and interlayer Coulomb interactions between charge carriers. In momentum (\mathbf{q}) space, the intralayer and interlayer Coulomb interactions are

$V_A(\mathbf{q}) = \frac{2\pi e^2}{\epsilon q} \tanh(qD)$ and $V_E(\mathbf{q}) = V_A(\mathbf{q})e^{-qd}$, respectively. The factor $\tanh(qD)$ comes from screening from the gate electrodes. Here $d = 1.3d_0$ and $D = 1.3D_0$ are the effective distances between the two semiconductor layers and between the two gates, respectively ($d_0 = 1.8$ nm and $D_0 = 8$ nm denoting the geometrical distances). The factor of 1.3 accounts for the anisotropic dielectric constant of hBN ($\epsilon \approx 5.2$). We also increased the dielectric constant by 50% to account for the correlated screening effect. Finally, we evaluated the Hartree contribution to the interaction as the potential energy of the capacitor and the exchange integrals following ref. 21.

Data availability

All data are available in the article. Source data are provided with this paper.

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Acknowledgements

This work was primarily supported by the Department of Energy (DOE), Office of Science, Basic Energy Sciences (BES), under award number DE-SC0019481 (electrical measurements and theoretical modelling) and DE-SC0022058 (device fabrication). We also acknowledge support from the David and Lucile Packard Foundation Fellowship (K.F.M.) and Kavli Institute at Cornell (KIC) Engineering Graduate Fellowship (P.X.N.). A portion of this work was performed at the Cornell NanoScale Facility, an NNCI member supported by National Science Foundation (NSF) Grant NNCI-2025233, and at the National High Magnetic Field Laboratory, which is supported by NSF Cooperative Agreement No. DMR-2128556 and the State of Florida. Growth of the hBN crystals was supported by the Elemental Strategy Initiative of MEXT, Japan, and CREST (JPMJCR15F3), JST.

Author contributions

P.X.N. and R.C. fabricated the devices, performed the measurements and analysed the data. B.Z. and A.H.M. provided theoretical support for the measurements. K.W. and T.T. grew the bulk hBN crystals. K.F.M. and J.S. designed the scientific objectives and oversaw the project. All authors discussed the results and commented on the paper.

Funding

Open access funding provided by Max Planck Society.

Competing interests

The authors declare no competing interests.

Additional information

Extended data is available for this paper at

<https://doi.org/10.1038/s41563-025-02334-3>.

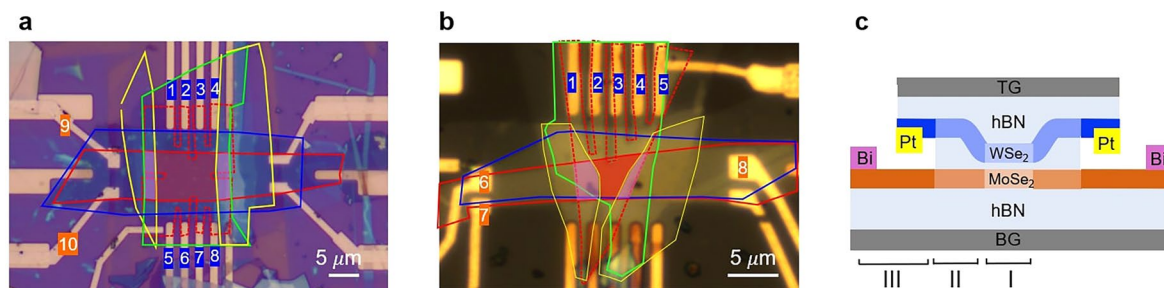
Supplementary information The online version contains supplementary material available at <https://doi.org/10.1038/s41563-025-02334-3>.

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Peer review information *Nature Materials* thanks the anonymous reviewers for their contribution to the peer review of this work.

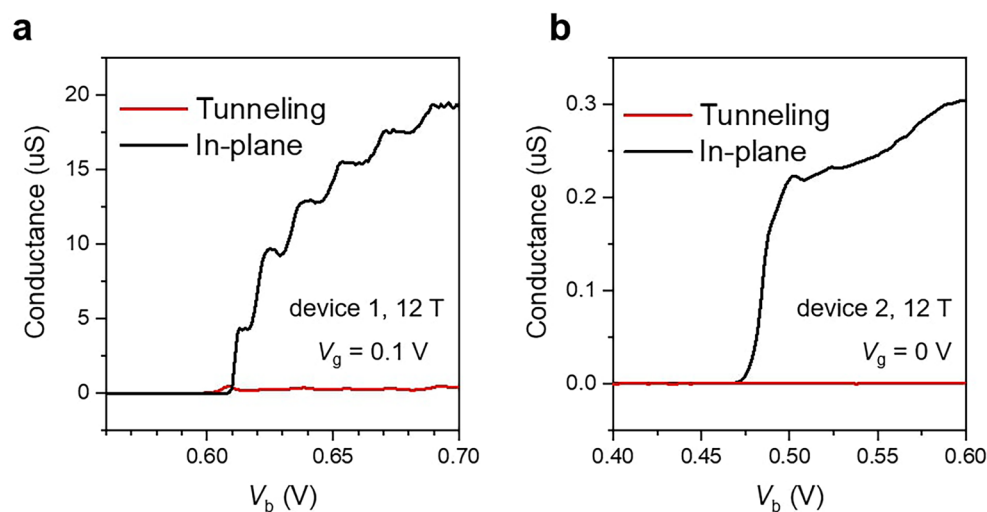
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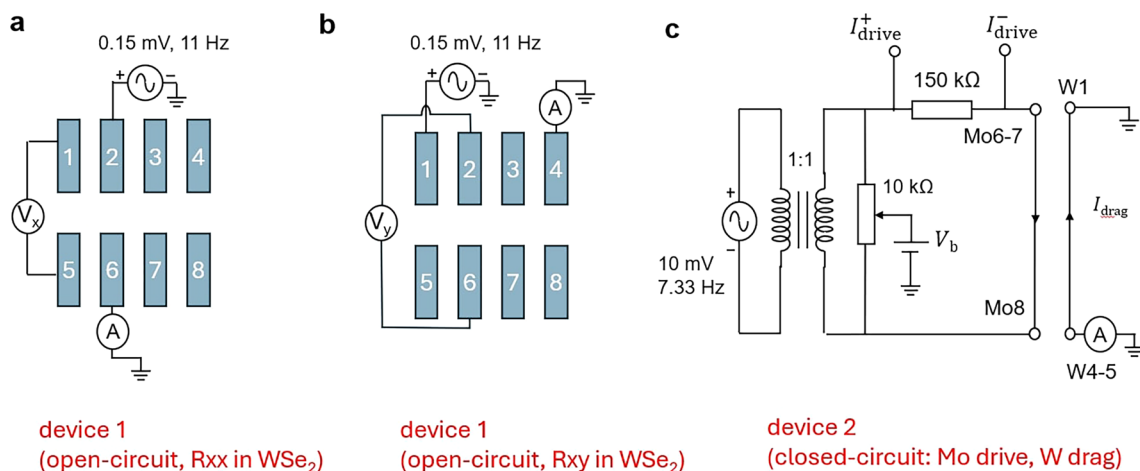
Extended Data Fig. 1 | Device images. a,b, Optical micrographs for device 1 (**a**) and 2 (**b**). The top gate (red dashed line), bottom gate (red line), W-layer (green line), Mo-layer (blue line) and the exciton contact hBN layers (yellow lines) are outlined. The red- and pink-shaded areas denote the device channel and exciton contact regions, respectively. The contact electrodes to the Mo- and W-layers are numbered in orange and blue, respectively. **c**, Schematic cross section of the

devices showing the doping profile. Region I, II and III are the channel, the exciton contact and the metal-semiconductor contacts, in increasing order of doping concentration and darkness of the color (orange for electron doping, blue for hole doping). TG, BG, Pt and Bi denote top gate, bottom gate, platinum electrode and bismuth electrode, respectively.



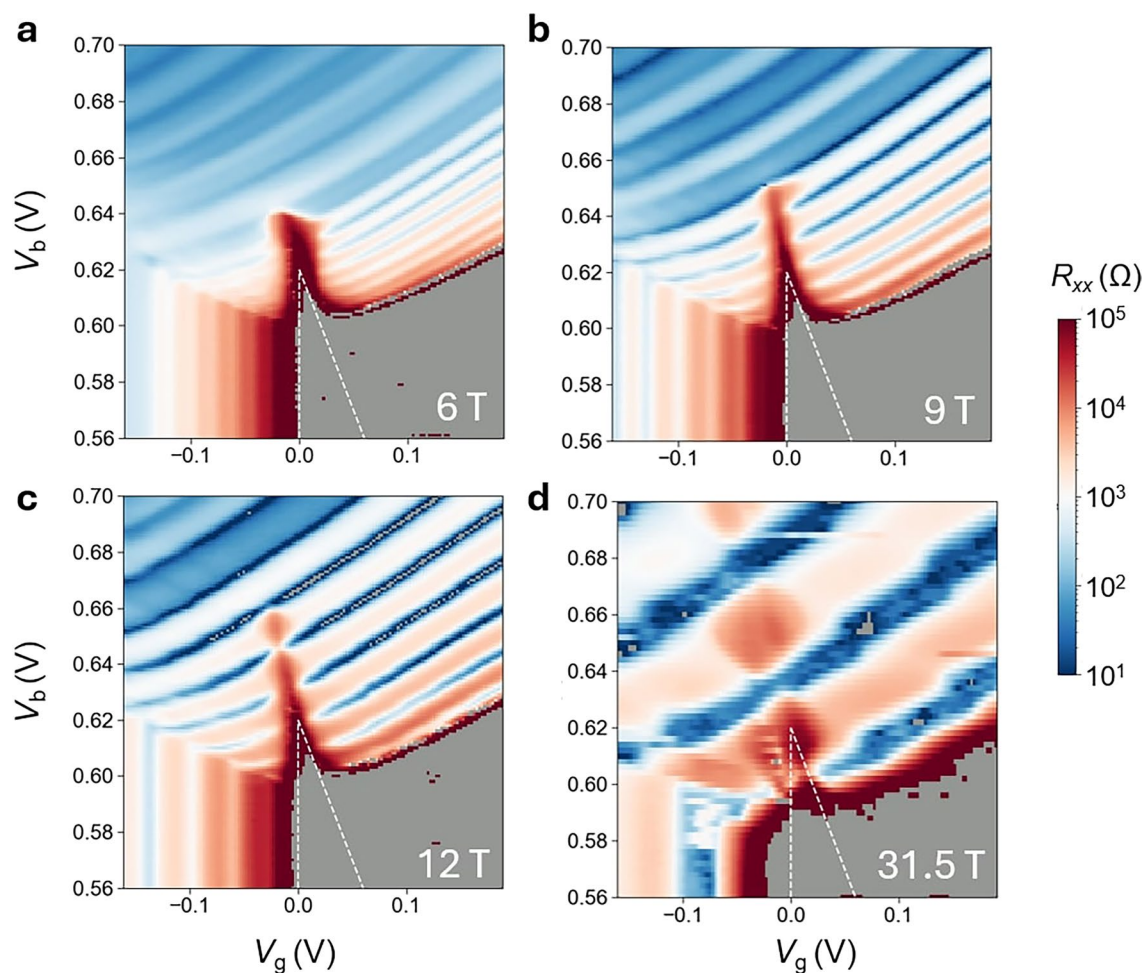
Extended Data Fig. 2 | Negligible interlayer tunneling conductance. a,b, Interlayer tunneling conductance (red) and two-terminal in-plane conductance of the Mo-layer (black) as a function of V_b for device 1 at $V_g = 0.1$ V (a) and device 2

at $V_g = 0$ V (b). In the relevant *pn* and EI regions (that is when the Mo-layer is turned on electrically), both devices show tunneling conductance about 1-2 orders of magnitude smaller than the in-plane conductance.



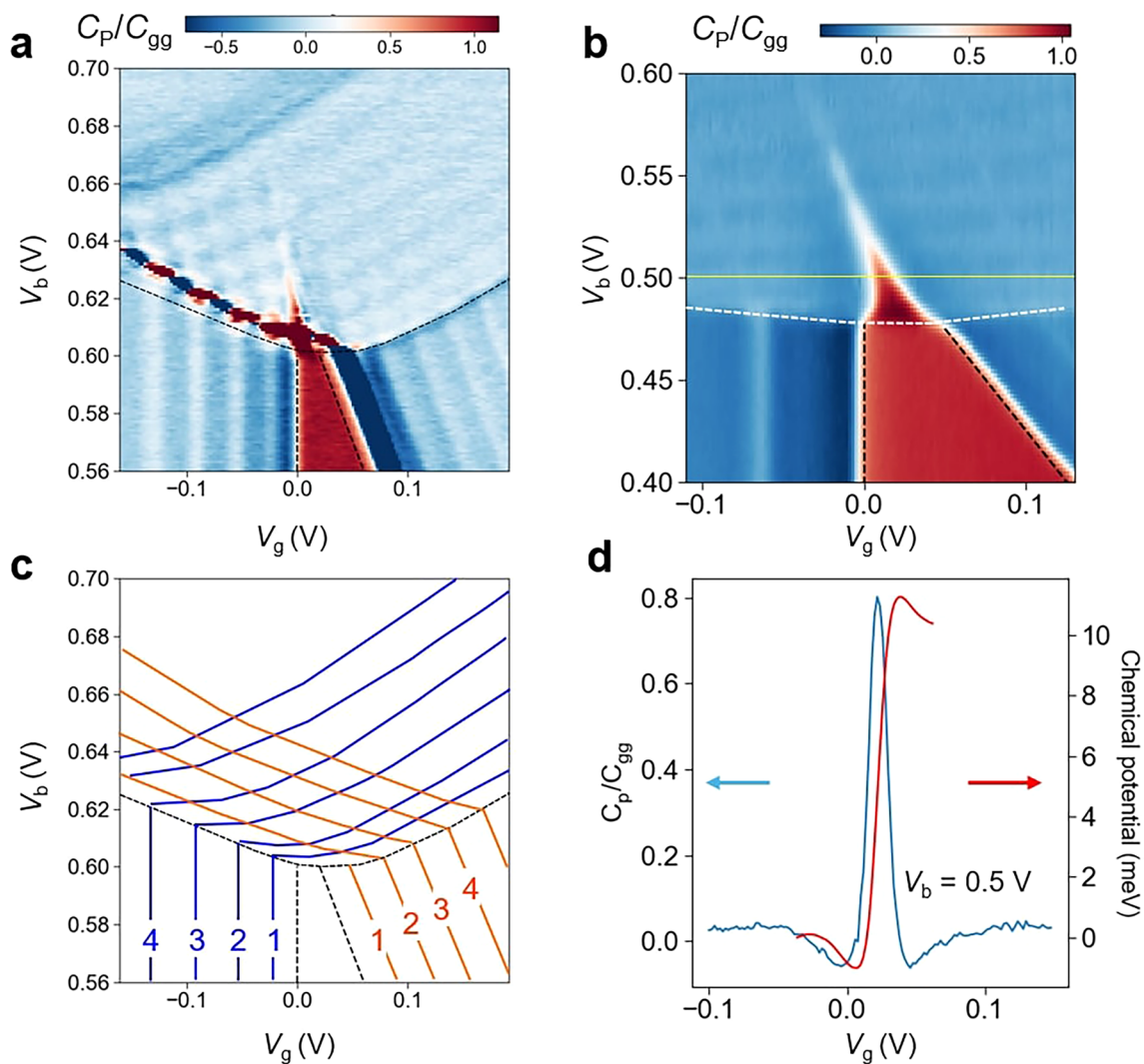
Extended Data Fig. 3 | Measurement circuit diagrams. a,b, Open-circuit measurement diagram for R_{xx} (**a**) and R_{xy} (**b**) in device 1. Only the pins in the W-layer are shown. The Mo-layer is in open-circuit; only pin 9 (one of the Mo-layer contacts) is connected to apply a DC interlayer bias V_b . **c**, Closed-circuit measurement diagram for the drag counterflow studies in device 2. An AC electron current is biased in the Mo-layer through a 1:1 transformer. V_b is applied

(through the midpoint of a 10 kΩ potentiometer) to both the source (shorted pins 6 and 7, Mo6-7) and drain (pin 8, Mo8) in the Mo-layer. The potentiometer position is tuned to minimize the AC interlayer coupling. In the W-layer, pin 1 (W1) is grounded and the hole drag current is measured by an ammeter connected to shorted pin 4 and 5 (W4-5).



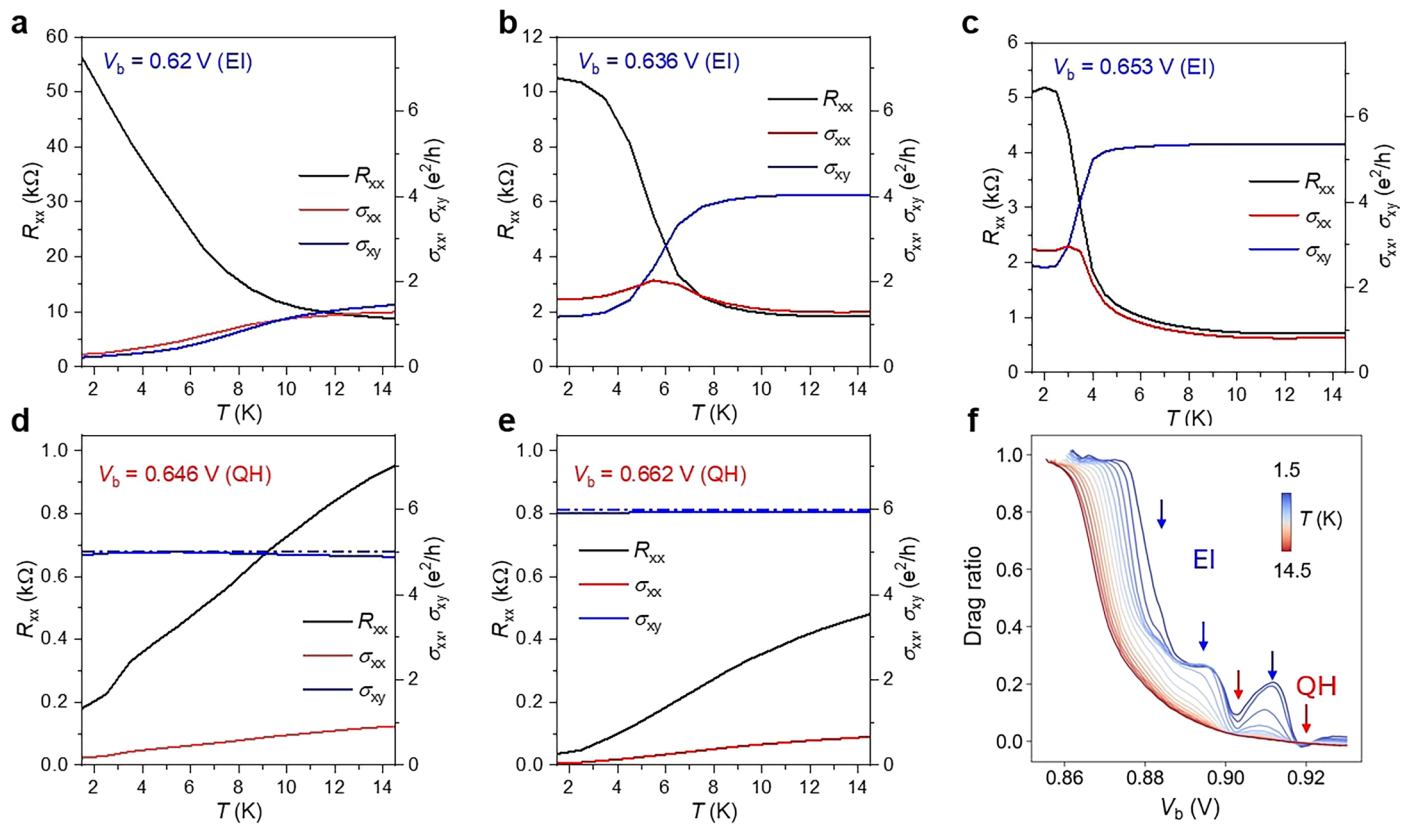
Extended Data Fig. 4 | Magnetic-field evolution of R_{xx} . **a–d**, R_{xx} of the W-layer (with the Mo-layer in open-circuit) as a function of V_g and V_b at $B = 6$ T (**a**), 9 T (**b**), 12 T (**c**) and 31.5 T (**d**). The dashed lines locate the band edges under zero magnetic field. R_{xx} diverges and cannot be reliably measured in the grey area. The

dips in R_{xx} reflect the fully filled LLs. The voltage spacing between consecutive dips increases with B as the LL degeneracy $\Delta n_{LL} = \frac{eB}{h}$ increases. At $B = 31.5$ T, the lowest LL penetrates through the triangular EI region.



Extended Data Fig. 5 | Penetration capacitance measurements. a, b. The normalized penetration capacitance C_P/C_{gg} as a function of V_g and V_b at $B = 12$ T and $T = 1.5$ K for device 1 (**a**) and 2 (**b**). LLs from both the W- and Mo-layers can be observed, especially in device 1. The electronic incompressibility of the EI oscillates as V_b increases at charge-neutrality. **c.** Integer-filled LLs for the Mo-

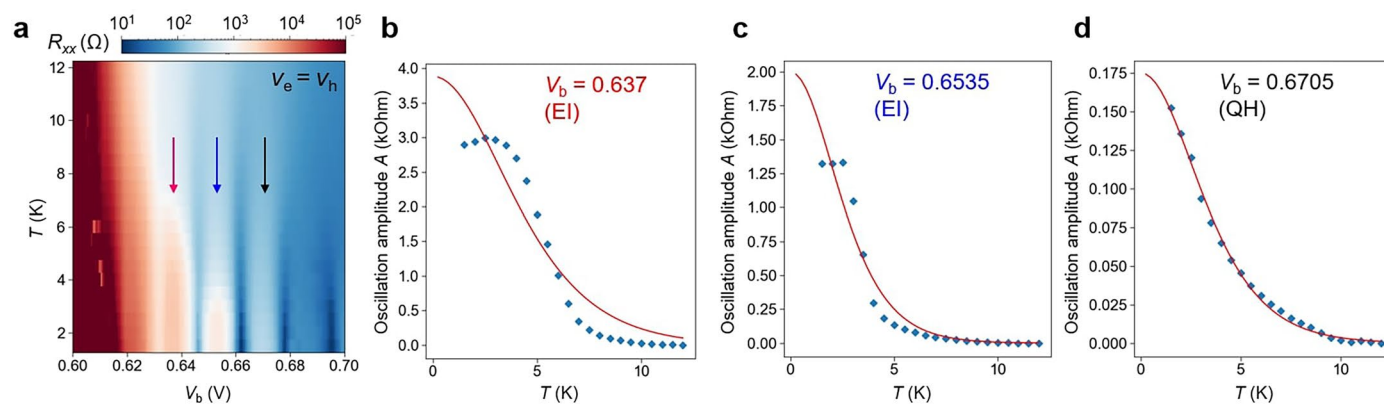
(orange) and W-layer (blue) extracted from the data in **a, d**. C_P/C_{gg} (blue, left axis) and the extracted electron chemical potential (red, right axis) as a function of V_g at $V_b = 0.5$ V (yellow solid line in **b**). The chemical potential is obtained by integrating C_P/C_{gg} with respect to V_g (see Methods). The exciton binding energy is equal to the jump in the chemical potential for the incompressible EI state.



Extended Data Fig. 6 | Temperature dependence of R_{xx} , σ_{xx} , σ_{xy} and drag ratio.

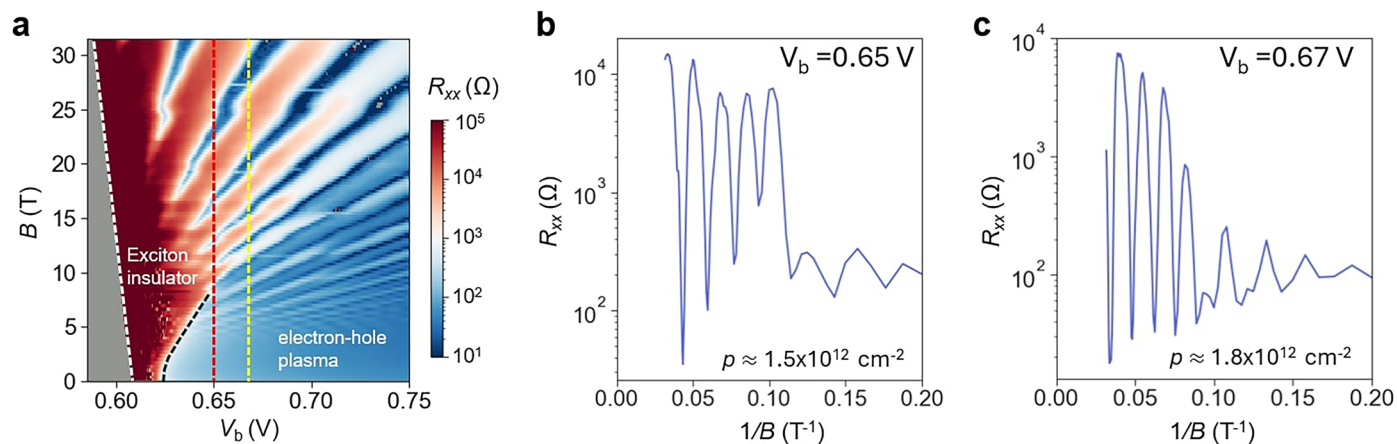
a-e. Temperature dependence of R_{xx} (left axis), σ_{xx} and σ_{xy} (right axis) (device 1) at $v_e = v_h$ for the EI at $V_b = 0.62$ V (**a**), 0.636 V (**b**) and 0.653 V (**c**) and for the QH states at $V_b = 0.646$ V (**d**) and 0.662 V (**e**). Blue dashed-dotted lines in **d,e** mark

the expected quantized values for σ_{xy} . **f.** Drag current ratio (device 3) as a function of V_b at $v_e = v_h$ for temperature varying from 1.5 K to 14.5 K in 1 K step. Blue (red) arrows mark the EI (QH) states with enhanced (suppressed) drag current ratio.



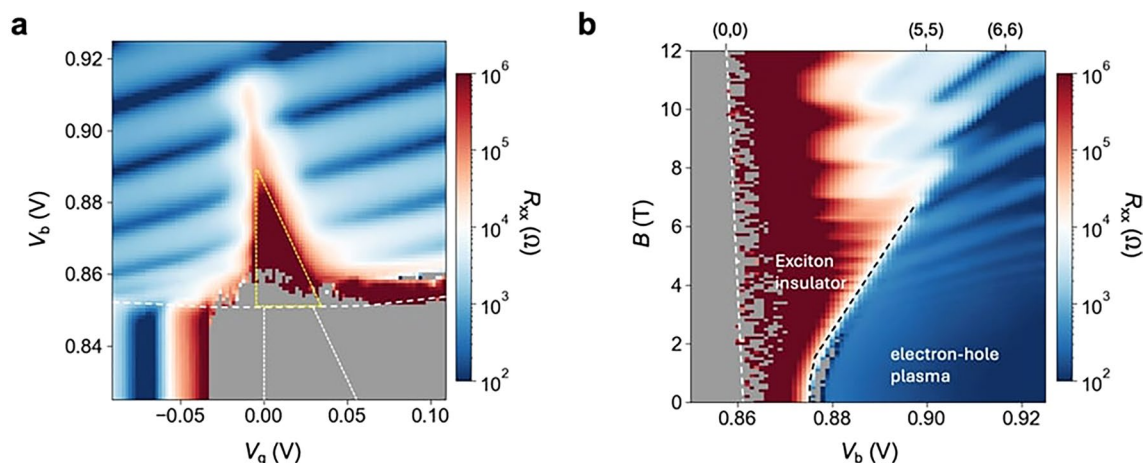
Extended Data Fig. 7 | Temperature dependence of the quantum oscillation amplitude. **a**, R_{xx} of the W-layer as a function of V_b and T at charge neutrality (copy of Fig. 4a of the main text). **b–d**, Temperature dependence of the oscillation amplitude (blue symbols) for three representative V_b 's marked by arrows in **a**: $V_b = 0.637$ V (**b**), $V_b = 0.6535$ V (**c**) and $V_b = 0.6705$ V (**d**). The oscillation amplitude at each temperature was extracted by subtracting from the resistance

$R_{xx}(T = 12\text{ K})$, at which quantum oscillations are no longer observable. Solid red lines are the Lifshitz-Kosevich (LK) fits. Good agreement is observed for the QH state in **d**; the extracted effective mass is consistent with the reported mass for monolayer WSe_2 . Significant deviation from the LK formula is observed for the EI phase in **b** and **c**.



Extended Data Fig. 8 | Periodic quantum oscillations in $1/B$. **a**, R_{xx} of the W-layer as a function of V_b and B at charge neutrality and $T = 0.3$ K (copy of Fig. 3a of the main text). The EI phase with diverging R_{xx} expands with B-field. **b,c**, Line cuts of **a** at fixed $V_b = 0.65$ V (red dashed line) and 0.67 V (yellow dashed line). The

periodicity at high B-fields is half of that at low B-fields. The two-fold spin-valley degeneracy is removed by the Zeeman effect at high B-fields, thus doubling the periodicity. The hole density p was determined from the periodicity in $1/B$, which is set by the hole Fermi surface.



Extended Data Fig. 9 | Quantum oscillations in device 3. a, R_{xx} of the W-layer as a function of V_g and V_b at $B = 12$ T and $T = 1.5$ K. The triangular region enclosed by the yellow dashed lines is the EI region. The white dashed lines are the electrostatic phase boundaries at $B = 0$ T. **b**, R_{xx} as a function of V_b and B at charge neutrality (that is $v_e = v_h$) and $T = 1.5$ K. The EI boundary (black dashed line)

expands with magnetic field. The fully filled LLs that protrude into the EI phase at high fields are identified as $(v_e, v_h) = (5, 5)$, $(6, 6)$; the band edge (white dashed line) is labeled as $(v_e, v_h) = (0, 0)$. In the grey-shaded area, R_{xx} diverges and cannot be reliably measured (**a,b**).